Vibrational dynamics in lead halide hybrid perovskites investigated by Raman spectroscopy†

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Lead halide perovskite semiconductors providing record efficiencies of solar cells have usually mixed compositions doped in A- and X-sites to enhance the phase stability. The cubic form of formamidinium (FA) lead iodide reveals excellent opto-electronic properties but transforms at room temperature (RT) into a hexagonal structure which does not effectively absorb visible light. This metastable form and the mechanism of its stabilization by Cs+ and Br− incorporation are poorly characterized and insufficiently understood. We report here the vibrational properties of cubic FAPbI3 investigated by DFT calculations on phonon frequencies and intensities, and micro-Raman spectroscopy. The effects of Cs+ and Br− partial substitution are discussed. We support our results with the study of FAPbBr3 which expands the identification of vibrational modes to the previously unpublished low frequency region (Δ<500 cm−1).

Our results show that the incorporation of Cs+ and Br− leads to the coupling of the displacement of the A-site components and weakens the bonds between FA+ and the PbX6 octahedra. We suggest that the enhancement of α-FAPbI3 stability can be a product of the release of tensile stresses in the Pb–X bond, which is reflected in a red-shift of the low frequency region of the Raman spectrum (Δ<200 cm−1).

Introduction

Lead halide perovskites (LHPs = A[Pb]X3) have attracted the curiosity of researchers owing to their outstanding optoelectronic properties such as a sharp absorption edge, high absorption coefficients, the large diffusion length of free charge carriers, and low recombination rates.1,4,5 Furthermore, the band gap tunability,3–7 the small difference between the band gap size and the open circuit voltage,8 easy processing, and the high defect tolerance9,10 of LHPs make these compounds suitable for a variety of applications including light emitting devices,11 solar cells,3,12,13 phototransistors,14,15 lasers,16,17 and detectors.18–21 Among various LHPs, formamidinium (CH(NH2)2+ = FA+) lead iodide (FAPbI3) is of particular interest for solar cell applications due to its narrow band gap of around 1.55 eV, its improved thermal stability compared to that of methylammonium (CH3NH3+ = MA+) lead iodide (MAPbI3) and the easier solution processability compared to CsPbI3.22–25 The main challenge for this material is the structural instability; at room temperature (RT) it transforms into the non-photoactive yellow δ-phase in 1 to 10 days depending on the environment.25,26 A common way to circumvent this is to combine different cations on the A-site or halides on the X-site featuring quinary CsFA1−x PbI6−yBrx composition with x and y about 10% each. This strategy has been shown to improve the phase stability in bulk, microcrystalline and nanocrystalline forms. In solar cells, this is translated into improved photo and moisture stability under environmental conditions and reduction of trap density, which consequently increases the efficiency by more than 1%,3,13,20,27–29

Even though impressive progress in synthesis and device engineering has been made, some fundamental properties of LHPs remain poorly investigated. Particularly, the understanding of the lattice dynamics of LHPs is crucial for the further optimization of their performance due to the unusually high softness of LHPs compared to conventional semiconductors30–32 and the additional dynamic effects caused by the non-spherical geometry of organic A-cations. Their dipole moments in combination with the X-ion migration33 and the reorientation of A-cations within the BX6 octahedral frame34 result in a structural phase transition.35
Raman spectroscopy has already disclosed the lattice dynamics for some LHPs. The experimental Raman spectra of LHPs have been supported with Density Functional Theory (DFT) calculations only for MAPbX₃ (X = I and Br). The interesting range of the vibrational spectrum of these materials is 10–3100 cm⁻¹ where the most pronounced peaks are correlated with the motion of the PbX₆ octahedra and the reorientation of the MA⁺ cation. These peaks appear in the spectra below and above 200 cm⁻¹, respectively.³⁶⁻³⁹ Dynamic disorder of MA⁺ causes splittings of independent harmonic modes, resulting in a larger number of Raman peaks at high frequencies.³⁷ The variation of halogens in MAPbX₃ shifts the Raman peaks in accordance to the Pb–X bond strength.³⁸,³⁹

There are experimentally measured Raman spectra of FAPbBr₃ and CsPbBr₃ up to 3500 cm⁻¹ and 320 cm⁻¹, respectively, but the specific modes have not been ascribed for the whole spectrum.³⁶⁻⁴² For FAPbBr₃, the attribution is well-made for molecular modes (≫ 500 cm⁻¹), associating them with the Raman modes of the isolated FA⁺ molecular ion.⁴³ For CsPbBr₃, a general description of modes was done on the basis of atomic trajectories, which reveals that Cs⁺ atoms perform a head-to-head motion, which is the displacement of two neighboring Cs⁺ atoms towards the same face, along the (100) directions. Comparative studies of MAPbX₃ and CsPbX₃ demonstrated a number of correlating Raman peaks representing the analogous motions for both compounds.³⁶,⁴²

Despite the existence of molecular dynamics simulations performed for FAPbI₃,⁴⁴,⁴⁵ its vibrational behavior and internal dynamics have not been correlated with experimental data so far. Only one Raman peak at 110 cm⁻¹ has been experimentally determined.²⁵ There are also no experimental data for the mixed FA-based compounds at all. Therefore, the effect of Cs⁺ and Br⁻ doping in the lattice dynamics also remains poorly understood.

In this work we investigate FAPbI₃ and FAPbBr₃ by means of Raman spectroscopy and identify the origin of the different vibrational modes with the support of DFT calculations.³⁶ The measurements were conducted on single crystal perovskites which exhibit less defects compared to their polycrystalline counterparts. Solution based growth provides an even distribution of components and a good level of the process control. We intend to understand the impact of Cs⁺ and Br⁻ incorporation into FAPbI₃ through the quantification of Raman modes and Raman shifts. A compositional cross-check is performed: single crystalline FAPbI₃ and FAPbBr₃ are compared to identify the sublattice PbX₆ modes and FA⁺ movements. Comparing FAPbBr₃ with CsPbBr₃ enables the identification of Br⁻ related vibrational modes and to differentiate between FA⁺ and Cs⁺ cations. A complex effect of the partial cation and anion substitutions is observed in relatively stable Cs₀.₁Fₐ₀.₉PbI₃ and Cs₀.₁Fₐ₀.₉PbI₂Br₀.₄ compositions. By analyzing the cooperative effects of the noticed substitutions we propose an explanation for the observed stabilization of the cubic structure at RT.

Methods

Sample preparation

Single crystalline samples of the compositions presented in Fig. 1 were prepared using the modified inverse temperature crystallization (ITC) method reported elsewhere.²⁰,²⁵,²⁶,⁴⁷

The γ-butyrrolactone (GBL) based-solutions were prepared in ambient air (RT = 17 °C) and next filtered through a 0.2 μm polytetrafluoroethylene syringe filter. The filtered precursor solution of 3 ml volume was poured into a 20 ml vial, closed with a cap, and placed into a preheated (90 °C) glycerol bath. The temperature was elevated in 5 °C h⁻¹ steps up to 130 °C maximum and kept for 3 h. The crystals formed were wiped with a filter paper and dried under ambient conditions. To grow large enough crystals of the Cs₀.₁Fₐ₀.₉PbI₃ and FAPbI₃ compositions, a previously obtained seed was introduced at 95 °C into the solution. Seeds were obtained using the method of Han et al.²⁵ by keeping a not-filtered 1 M precursor solution at 70 °C for 6 hours followed by their growth in a freshly prepared and filtered solution at 115 °C for 3 h.

Analytical methods

Powder X-ray diffraction (XRD) patterns were collected in transmission (Debye–Scherrer-geometry) with a STADI P diffractometer (STOE & Cie GmbH), equipped with a silicon strip MYTHEN 1K Detector (DECTRIS) with a curved Ge(111)-Monochromator. For the measurement, single crystals were ground and placed between adhesive tapes.

Raman spectroscopy was performed on a high-resolution LabRAM HR800 spectrometer from Horiba. It included an ultra-low frequency (ULF) unit capable of measuring Raman spectra from 10 cm⁻¹ at an excitation wavelength of 633 nm. Spectra were recorded with gratings of 600 and 1800 lines per millimeter at RT in an ambient environment. The laser beam was focused using a 50×/NA = 0.75 microscope objective, with a spot diameter of 1.03 μm and a power intensity in the range from 6 μW to 280 μW. This results in a power density in the range from 0.8 kW cm⁻² to 35.6 kW cm⁻².

We notice here that the acquisition and interpretation of Raman spectra are challenging in the case of the LHPs, due to the combination of two counteracting effects: (i) the low relative intensity of Raman scattering compared to the primary excitation power and (ii) the high rate of degradation of LHPs under laser induced heating.³⁸ For a laser wavelength λ = 532 nm, the LHPs are degraded at a beam power higher than > 10 μW. We detected degradation of FA-based LHPs at > 1 mW at an excitation wavelength λ = 633 nm. Consequently, the excitation power and integration times were optimized for each LHP to ensure good signal to noise ratios while avoiding laser induced material degradation during the measurements. To avoid parasitic light signals, the measurements were performed in the dark. Due to the onset of strong luminescence in FAPbI₃ (PL signal around λ = 827 nm), the Raman spectrum of this compound is only shown.

Fig. 1 Photographs of single crystals: (a) FAPbI₃, (b) FAPbBr₃, (c) Cs₀.₁Fₐ₀.₉PbI₃ and (d) Cs₀.₁Fₐ₀.₉PbI₂Br₀.₄.
up to 200 cm$^{-1}$. The same limitation applies for mixed compounds at frequencies above 1200 cm$^{-1}$. For CsPbBr$_3$, the spectra were found to be informative up to 400 cm$^{-1}$. Despite the limitation in the measured range, the source at $\lambda = 633$ nm gives the sharpest peaks and lowest noise. A less energetic excitation source ($\lambda = 830$ nm) also excites FAPbI$_3$, emitting photoluminescence that reduces the possibility of identifiable peaks.

Expecting exclusively molecular (FA$^+$) modes in Zone III, we considered the FAPbBr$_3$ compound as a reference. Besides, among FA-based LHPs, only this compound is experimentally characterized by Raman spectroscopy in the literature.$^{40}$

**Computational details**

DFT based total energy and force calculations were performed using the Vienna Ab initio Simulation Package (VASP) code.$^{49}$ The projector augmented (PAW) potentials$^{50,51}$ that describe electron–ion interactions were constructed such that the 5d electrons of Pb, 4s and 4p electrons of Br, and 5s and 5p electrons of I are treated as valence electrons. The plane-wave cutoff energy was set to 700 eV. A force convergence criterion of 1 meV Å$^{-1}$ and an energy convergence of 10$^{-6}$ eV were used for all geometry optimizations. A Gamma-centered Monkhorst–Pack set of $k$-points of $6 \times 6 \times 6$ was used for Brillouin zone integration. To take the weak van der Waals interactions into account, the optB88-vdW functional$^{52}$ with default setting of the VASP was used. Cubic phases of FAPbI$_3$ and FAPbBr$_3$ perovskite compounds with experimentally measured lattice parameters (6.36 and 5.99 Å, respectively) were considered. Spin-polarized calculations for the primitive cells and $2 \times 2 \times 2$ cells showed no change in the atomic configuration, therefore, the rest of the calculations were performed on primitive cells. First-principles lattice dynamics (phonon spectrum) calculations were performed for the cubic phases of FAPbI$_3$ and FAPbBr$_3$ by diagonalizing the Hessian matrix within the Harmonic approximation.$^{53}$ We used the finite difference method to calculate the force constants. The eigenvectors of the Hessian matrix give the normal modes of the vibrations of the atoms, whereas the eigenvalues represent their frequencies. After obtaining the normal modes, Raman intensities (activities) of these modes were obtained by calculating the change in polarizability (macroscopic dielectric tensor) of each normal mode. Diagonalization of the Hessian matrix gives imaginary frequencies if the structure is not well optimized. Hence, we first optimized the atomic structures with a rather tight convergence criterion as mentioned above.

**Results and discussion**

**Theoretical Raman spectra of FAPbBr$_3$ and FAPbI$_3$**

DFT calculations were performed to attribute the modes in the case of poorly investigated FAPbBr$_3$ and FAPbI$_3$. To validate our model, we performed DFT calculations for MAPbI$_3$ (see Fig. S1, ESI$^\dagger$) and our results were found to be in good agreement with the data published previously.$^{37}$ The calculated Raman spectra of FAPbX$_3$ are shown in Fig. 2. The modes of the high frequency range (500–3500 cm$^{-1}$) for some FA-based compounds were also explored experimentally$^{40,43}$ and our DFT data agree well with the experimental data for FAPbBr$_3$.$^{40}$

Raman spectra of hybrid perovskites are usually analyzed in three spectral ranges which correspond to different sources of vibrations.$^{37}$ The low-energy range from 10 to 50 cm$^{-1}$ (Zone I)
contains PbX₆ sublattice modes. Zone II, from 50 to 500 cm⁻¹, corresponds to the coupled modes, which appear exclusively in LHPs. They present the FAPbX₆ molecular reorientation of FA⁺ influenced by the PbX₆ octahedral framework. Zone III, the high-energy zone from 500 to 3500 cm⁻¹, includes individual molecular modes. It is worth noticing that all modes are affected by the coupling, however, this coupling is the source of the vibration only in Zone II. The modes of Zones I and III are present in isolated octahedra and isolated molecules, respectively.

The following results are structured in accordance with these three zones. We explain the modes of Zones I and III by comparison with theoretical modes from the literature. The modes of Zone II are extensively explained due to the absence of references in the literature.

In Zone I, our calculations show peaks related to the octahedral modes, which are twist and distortion vibrations characteristic for the Oh symmetry (see Fig. S2, ESI†). For FAPbI₃, the twist mode is present at 16, 20 and 22 cm⁻¹ and the distortion mode is present at 33 and 35 cm⁻¹. For FAPbBr₃, these modes are present at 30 and 31 cm⁻¹ and at 34, 44 and 63 cm⁻¹, respectively.

A comparison between our calculated modes of Zone I with experimental Raman modes cannot be made due to the lack of Raman data of FAPbX₆ compositions in the literature. We can directly compare FAPbX₆ with other hybrid LHPs, such as MAPbI₃, considering that the molecular response does not affect the frequencies of the octahedral modes significantly. This is a consequence of the lower mass of the molecules compared to the inorganic frame (FA⁺ = 46 u. compared to PbX₆ = 1000 u.). The modes of MAPbI₃ were thoroughly ascribed on the basis of DFT calculations and corroborated by experiments. According to these data the peak associated with the octahedral twist in iodide appears at energies below 30 cm⁻¹, whereas the octahedral distortion peak appears between 30 and 50 cm⁻¹. In bromide, these modes shift about 15 cm⁻¹ to higher frequencies. This happens due to the higher strength of the Pb–Br bond (0.66 in the Pauling scale) compared to Pb–I (0.33 in the Pauling scale) as well as due to the smaller atomic mass of Br (79.9 u.) compared to I (126.9 u.). The latter impacts peak positions as ω = \sqrt{k/m}, according to the harmonic oscillator model. This model is the solution of the Schrödinger equation that describes the atomic vibrations in a system. For a simple scheme, in a diatomic molecule the frequency of the vibration “ω” depends directly on “m”, that represents the reduced mass, and “k”, that represents the spring constant, which is related to the strength of the chemical bond between the involved atoms.

Modes in Zone II for FAPbX₆ have not been described in the literature so far. For this zone, our calculations showed mainly six modes which are (a) in-plane rotation around the center of mass, (b) in-plane rotation around corner hydrogen, (c) out-of-plane rotation around the N–N axis, (d) molecular translation, and (e) asymmetric and (f) symmetric out-of-plane bending of H₂N–C–NH₂ (see Fig. 3). The 2D representation of the HP modes shown in the figure is a schematization of the 3D models of the vibrations given by DFT calculations, in which the displacements are represented by arrows. FAPbI₃ reveals these modes at 60, 61, 63, 97, 429, and 494 cm⁻¹, whereas FAPbBr₃ peaks (excluding mode b) appear at 11, 77, 102/121, 368 and 474 cm⁻¹, respectively.

As we can observe, the substitution of the halide is not reflected in a unidirectional shift of the modes. Thus, the large shift of mode (a) in FAPbI₃ at 60 cm⁻¹ as compared to 11 cm⁻¹ in FAPbBr₃ may be related to the following fact: the plane in which the rotation takes place is parallel to the crystallographic plane in FAPbBr₃ but slightly tilted in the case of FAPbI₃ due to the larger free space of the last one. The absence of mode (b) in FAPbBr₃ may be explained by the smaller size of the unit cell that makes unfavorable such a notable shift of FA⁺. Modes (c) and (d) shift from the iodide to bromide in accordance to the halide mass difference, however modes (e) and (f) do not follow this rule. Mode (e) is governed by displacements of hydrogen atoms at the corners of the FAPbI₃ unit cell (see Fig. 3e), whereas, in FAPbBr₃, these hydrogen atoms remain almost static while Br⁻ ions displace (figure is not presented in this work). We suggest that the magnitude of the displacement of the hydrogen atoms is a consequence of the interaction H ↔ X, which is lower for X = I⁻ than X = Br⁻. Therefore, it stipulates a higher frequency of mode (e) for FAPbI₃ than for FAPbBr₃, whose Raman peaks are present at 429 cm⁻¹ and 368 cm⁻¹, respectively. The higher energy of mode (f) in FAPbI₃ is expected to originate from the larger free space provided by the PbI₆ octahedra that allow the FA⁺ molecules to vibrate without valuable interactions with the surrounding halides as compared to FAPbBr₃.

For Zone III, we compare our calculations of the Raman modes with the specific modes of the isolated FA⁺ ions, disclosed in the theoretical work of Kucharska et al. In this work, they present 18 internal modes according to the C₃ᵥ symmetry of the FA⁺ molecule, distributed as Γ = 7A₁ + 2A₂ + B₁ + 3B₂. Our calculations are slightly red-shifted with respect to the isolated cation. This phenomenon is already known for MAPbX₆, in which the molecular modes are shifted around 200 cm⁻¹ for MAPbI₃ and 350 cm⁻¹ for MAPbBr₃. The dependency of the shift magnitude with the halide is due to the formation of hydrogen bonds or other non-covalent interactions, resulting from the difference in electronegativity. Our predicted Raman modes for FAPbI₃ and FAPbBr₃ differ on average ca. 50 cm⁻¹ from the isolated cation. According to Kucharska et al., FA⁺ molecular modes should appear above 521 cm⁻¹. Our DFT calculations predict modes already at 507 and 510 cm⁻¹ for FAPbI₃ and FAPbBr₃, respectively.

Experimental Raman spectra of the FA-based compounds

Following the discussion of DFT calculations, we focus next on the experimental Raman modes of FAPbI₃ and FAPbBr₃. In accordance with the previously established order, we discuss the experimental phonon modes in spectral ranges. The Raman spectra of the LHPs containing FA⁺ are shown in Fig. 4. Supporting experimental data for MAPbI₃ and CsPbBr₃ compounds are provided in the ESI† (Fig. S3).

In Zone I of the experimental spectrum, FAPbI₃ and FAPbBr₃ present the twist and distortion modes represented by a
single peak. The absence of splitting peaks indicated a cubic structure for both of them.

Compared to the other LHPs, FAPbBr₃ shows broad modes that basically reflect low octahedral activity. This is likely due to the stronger Pb–Br bonds than the Pb–I bonds and the closer-to-unity Goldschmidt Tolerance Factor (GTF) ensuring better fit of FA⁺ to the octahedral cage and therefore a less flexible lattice.

Zone II is analyzed in two sub-zones: a high-coupling range (50–200 cm⁻¹) and a low-coupling one (200–500 cm⁻¹). The spectrum of FAPbI₃ in the high-coupling range shows a sharp peak at 114 cm⁻¹ and two broad peaks at 63 cm⁻¹ and 96 cm⁻¹. The spectrum of FAPbBr₃ presents broad peaks in this range. In the low-coupling range, the spectrum of FAPbBr₃ shows a sharp peak at 308 cm⁻¹ and a broad peak at 470 cm⁻¹.

Assigning the modes of this zone is especially challenging. The experimentally visible modes of FAPbX₃ are more frequent than those theoretically predicted in the first sub-zone. Such a difference may be caused by a non-uniform disposition of FA⁺ to the octahedral cage and therefore a less flexible lattice.

Fig. 3 Schematic representation of the HP modes existing in FAPbI₃ according to our DFT calculations: (a) in-plane rotation around the center of mass, (b) in-plane rotation around corner hydrogen, (c) out-of-plane rotation around the N–N axis, (d) FA⁺ translation along the C–H bond, (e) H₂N–C–NH₂ asymmetric out-of-plane bending and (f) H₂N–C–NH₂ symmetric out-of-plane bending. Red colors represent changed positions. In cases (e) and (f) the N–H and C–H bonds project beyond the figure plane that is shown in the perspective view (thicker-closer).

To validate the attribution of the experimental modes of FAPbX₃ to the mode description given by the DFT calculations, we compare the coupled modes for FAPbI₃ and MAPbI₃. It is worth remarking significant differences between MA⁺ and FA⁺ for further discussion (Fig. S4, ESI†). In the FA⁺ ion, the positive charge is delocalized between two nitrogen atoms, whereas in MA⁺ it remains only on the –NH₃⁺ group. The N–C–N chain becomes more rigid and deflects with an interatomic angle of 125° due to proton embedding.⁵⁸ According to theoretical calculations, FA⁺ possesses a much lower dipole moment (0.21 D) than MA⁺ (2.29 D).⁵⁹ The experimentally determined value for MA⁺ is quite low –0.854 D⁶⁰ resulting in an expected dipole moment of the FA⁺ cation close to zero. Finally, FA⁺ adopts a planar symmetrical structure.⁶¹ Such 2D disposition and weaker polarization enables FA⁺ to vibrate out-of-plane without significant interactions with the surrounding sublattice PbX₆. Therefore, the associated Raman modes may present higher frequencies compared to analogous modes of MAPbX₃.

Taking into account these differences we can now compare the corresponding coupled modes. In the case of MAPbI₃ (see Fig. S2a, ESI†) these modes derive from the active reorientation of MA⁺, which mainly rotates in a cone around N (58, 66 cm⁻¹) with a period of 0.3 ps.⁴⁴ Other coupled modes represent rotation in a cone around C and N (117, 133 cm⁻¹), molecular
translations (69, 75, 81 and 92 cm\(^{-1}\)), rotation around C-N (128 cm\(^{-1}\)) and C-N torsion (315 cm\(^{-1}\)).\(^{37}\) The molecular reorientation of FA\(^+\) is distinctly slower and therefore the corresponding modes shift to lower frequencies. In contrast to that, a dominating movement of the molecules in FAPbI\(_3\) is a single roll-over with a time constant of 2 ps. The C-H bonds remain parallel to the \{100\} planes.\(^{34,62}\) Analogous modes of rotation around C or N and C-N torsion are not expected in FAPbI\(_3\) due to the rigid N-C-N frame. Translation modes in MAPbI\(_3\) are expected at lower frequencies as compared to FAPbI\(_3\). The main reason is the stronger ionic bonding between MA\(^+\) and X\(^-\) because MA\(^+\) has a larger dipole moment and a smaller size than FA\(^+\). The large size, rigidity and twist of a dipole moment stipulate slower rotation of FA\(^+\) around the N-N

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**Fig. 4** Raman spectra of FA-based single crystals at RT with an excitation wavelength \(\lambda = 633\) nm, divided into three zones according to the vibration source. Excluded ranges do not exhibit any noticeable Raman lines or are hidden due to strong luminescence. Color lines represent measured spectra, black dashed lines are fits to the spectra and gray lines indicate fitted peaks with Lorentzian line shape.
Table 1 Classification of Raman peaks of FA-based compounds according to DFT calculations by Kucharska et al.\textsuperscript{43} for isolated FA\textsuperscript{+} and DFT calculations by Leguy et al.\textsuperscript{37} for MAPbI\textsubscript{3}. Experimental Raman modes (indicated by \*) are based on the work of Wang et al. for FAPbBr\textsubscript{3}.\textsuperscript{40} Mode frequencies labeled "$\pi$" indicate broad and/or weak shoulder-like peaks without sharp peak-maximum.

<table>
<thead>
<tr>
<th>Literature</th>
<th>Description</th>
<th>DFT-FAPbI\textsubscript{3}</th>
<th>FAPbI\textsubscript{3}</th>
<th>Cs\textsubscript{0.1}FA\textsubscript{0.9}PbI\textsubscript{3}</th>
<th>Cs\textsubscript{0.1}FA\textsubscript{0.9}PbI\textsubscript{3}:Br\textsubscript{0.4}</th>
<th>FAPbBr\textsubscript{3}</th>
<th>DFT-FAPbBr\textsubscript{3}</th>
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<td>19,29\textsuperscript{37}</td>
<td>Octahedral twist</td>
<td>16, 20, 22</td>
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<td>15</td>
<td>20$^\pi$</td>
<td>30, 31</td>
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<tr>
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<td>Octahedral distortion</td>
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<td>43</td>
<td>40</td>
<td>32</td>
<td>58$^\pi$</td>
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<td>63$^g$</td>
<td>52$^g$</td>
<td>50$^g$</td>
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<tr>
<td>105$^\ast$</td>
<td>Out-of-plane rotation around N–N axis</td>
<td>63</td>
<td>96$^g$</td>
<td>89$^g$</td>
<td>78$^g$</td>
<td>84$^\pi$</td>
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<td>64,75,81,92</td>
<td>FA$^+$ Translation</td>
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<td>114</td>
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<td>118$^\pi$</td>
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<td>1789$^\ast$</td>
<td>NH$_2$:C–H scissoring + C–N asym. Stretching</td>
<td></td>
<td>1875</td>
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axis in contrast to more frequent MA$^+$ rotations around the C–N axis. In this way, we attributed the experimental modes of FAPbI$\textsubscript{3}$ at Zone II and correlated them with the DFT calculated data (see Table 1). Analogously, we attribute the Raman modes for FAPbBr$\textsubscript{3}$. As discussed before, the exception is the “in-plane rotation” mode, which is restricted due to the more compact lattice structure.

For the Raman modes of FAPbBr$\textsubscript{3}$ at Zone III, we found close agreement between the experimental data and the results from DFT calculations (see Table 1). It is worth noticing that the frequencies of those modes are only slightly shifted with respect to the phonon modes of the isolated FA$^+$, which indicates a weak interaction between the molecules and the PbBr$_6$ octahedra.

To summarize, we have identified the vibrational modes existing in FAPbI$\textsubscript{3}$ above 200 cm$^{-1}$ using DFT calculations. Additionally, we have correlated the DFT results with experimental data obtained for FAPbBr$\textsubscript{3}$ single crystals. Table 1 summarizes all modes discussed above and lists their attribution based on the experimental spectra shown in Fig. 2 and 4.

Effect of the partial Cs$^+$ and Br$^-$ substitutions

Following the previous discussion, we focus on the effect of partial substitution of FA$^+$ by Cs$^+$ and I$^-$ by Br$^-$ on the vibrational behaviour of LHPs and the stabilization of the cubic form. We refer here to XRD and PL measurements (Fig. S5 and S6, ESI†) of the chosen mixed compounds to support the comparison of the Raman spectra (Fig. 5).

In analogy to the Raman spectra, we compare the XRD patterns of FAPbI$\textsubscript{3}$ and the mixed compounds (Fig. S5, ESI†). Due to the similarity of the patterns, we fit them to the phase-structure of FAPbI$\textsubscript{3}$ with the incorporation of Cs$^+$. The substitution of I$^-$ by Br$^-$ results in the expected decrease of the lattice constant due to the smaller size and more electronegative character of the incorporated halide.

For further consideration we assume a homogeneous distribution of Cs$^+$ and Br$^-\textsubscript{-}$ in the mixed compositions, which is indirectly proven by the PL measurements (Fig. S6, ESI†) due to the absence of a secondary peak related to separated cesium-rich or bromide-rich zones. We also expect no symmetry change with respect to the cubic FAPbI$\textsubscript{3}$.

We discuss first the Raman spectrum of Cs$_{0.1}$FA$_{0.9}$PbI$\textsubscript{3}$. Within the range between 15 and 200 cm$^{-1}$, it demonstrates a slight red-shift with respect to the spectrum of FAPbI$\textsubscript{3}$: the modes observed at 40 and 109 cm$^{-1}$ of the mixed compound appear at 43 and 114 cm$^{-1}$ in FAPbI$\textsubscript{3}$, respectively (see Fig. 5). The observed shift of phonon modes to lower frequencies correlates with the previously suggested release of stresses in the FAPbI$\textsubscript{3}$ single crystals upon Cs$^+$ substitution. The magnitude of this reduction is probably not valuable enough to represent the prolonged stabilization of the cubic structure, which is observed in the degradation of this compound after a few weeks.

In Zone I, the appearance of the twist modes at 13 and 21 cm$^{-1}$ implies some local distortion due to the incorporation of the Cs$^+$ cation. Indeed, it can be expected that the heavier and more electronically spherical Cs$^+$ atoms should have notably stronger ionic interaction with the PbX$_6$ framework than the FA$^+$ molecules.

The influence of the incorporation of the Cs$^+$ atoms and the effect on the modes of Zone II are analyzed according to the Cs$^+$ atoms displacement from the A-position, considering that they

$6.293$ Å for Cs$_{0.1}$FA$_{0.9}$PbI$_{3}$:Br$_{0.4}$. The comparison of the reported lattice constants of the pure compounds FAPbI$_3$ (6.3620 Å$\textsuperscript{6}$) and CsPbI$_3$ (6.242 Å$\textsuperscript{6}$) in cubic form suggests a continuity of the phase-structure of FAPbI$_3$ with the incorporation of Cs$^+$. The substitution of I$^-$ by Br$^-$ results in the expected decrease of the lattice constant due to the smaller size and more electronegative character of the incorporated halide.
are contained in a FAPbI\textsubscript{3} matrix. For this, we compared the mixed compound Cs\textsubscript{0.1}FA\textsubscript{0.9}PbI\textsubscript{3} with CsPbBr\textsubscript{3} in which the atomic trajectories of Cs\textsuperscript{+} are known.\textsuperscript{42} In CsPbBr\textsubscript{3}, the Cs\textsuperscript{+} cations have 0.85 Å displacement in a head-to-head motion which is stabilized by a cooperative motion of Br\textsuperscript{−} ions. This means that the octahedral sub-cages that are approached by Cs\textsuperscript{+} ions expand due to Pauli repulsion forces. Therefore, the translation of Cs\textsuperscript{+} in the mixed compound is likely coordinated with the surrounding FA\textsuperscript{+} molecules to reduce the energy of the system during the distortion of the octahedral cages, which results in a shift of the corresponding translation mode from 114 cm\textsuperscript{-1} in FAPbI\textsubscript{3} to 109 cm\textsuperscript{-1}.

In the range from 200 to 500 cm\textsuperscript{-1}, we observe two modes at 250 cm\textsuperscript{-1} and 282 cm\textsuperscript{-1}. Compared to the DFT calculations of FAPbI\textsubscript{3}, they may be related to the out-of-plane FA\textsuperscript{+} bending modes which are predicted at 429 and 494 cm\textsuperscript{-1}, respectively (see Table 1). The higher energies of these modes of FAPbI\textsubscript{3} basically mean an overestimation of the FA\textsuperscript{+} bending, which may influence the FA\textsuperscript{+} bending via variations of the internal electric field. The same modes appear in FAPbBr\textsubscript{3} at 309 and 470 cm\textsuperscript{-1} respectively.

The Raman spectrum of Cs\textsubscript{0.1}FA\textsubscript{0.9}PbI\textsubscript{3} in Zone III presents peaks at frequencies in good agreement with the predicted ones by the DFT calculations of the molecular modes of FAPbI\textsubscript{3}. One noticeable difference between them is the splitting of the mode around 520 cm\textsuperscript{-1} present only for the former case. This may be related to the previously discussed lowering of symmetry. In this case, the frequency of the mode “molecular bending” depends on the position of the molecule inside the cage. This distortion in the structure was previously discussed from the presence of an additional peak for the “octahedral twist” mode.

To summarize, the effect of Cs\textsuperscript{+} substitution in the Raman spectrum of FAPbI\textsubscript{3} can be appreciated in a red-shift of the medium-frequency spectrum (<500 cm\textsuperscript{-1}) due to the release of stresses of the Pb–I bonds and the coordination of the translations of Cs\textsuperscript{+} and FA\textsuperscript{+}.

The Raman spectrum of Cs\textsubscript{0.1}FA\textsubscript{0.9}PbI\textsubscript{3}, as compared to CsPbI\textsubscript{3}, shows a red shift to higher phonon frequencies. We observe a similar unexplained red shift effect in CsPbBr\textsubscript{3} as compared to CsPbI\textsubscript{3}. For these materials, the most prominent peaks that we can ascribe to the Raman modes “distortion of the octahedra” and “translation of Cs\textsuperscript{+}” are present at 55 and 108 cm\textsuperscript{-1} in CsPbI\textsubscript{3} and at 40 and 73 cm\textsuperscript{-1} in CsPbBr\textsubscript{3} (see Fig. S3, ESI†, respectively). The structure of CsPbBr\textsubscript{3} is more compact compared to CsPbI\textsubscript{3}, as suggested by a GTF closer to 1 (0.974 vs. 0.836, respectively). Therefore, we suggest an effect of the strength release of the Pb–X bonds as in both cases a red shift is accompanied by an increase of the GTF (see Table S2, ESI†).

In Zone I, the disappearance of the second peak of the “octahedral twist” mode at 21 cm\textsuperscript{-1} of Cs\textsubscript{0.1}FA\textsubscript{0.9}PbI\textsubscript{3} suggests that the emergence of additional stresses in the PbX\textsubscript{6} structure caused by the incorporation of Cs\textsuperscript{+} somehow counteracts the distortion introduced by Br\textsuperscript{−}.

Fig. 5 Raman spectra of Cs\textsubscript{0.1}FA\textsubscript{0.9}PbI\textsubscript{3} and Cs\textsubscript{0.1}FA\textsubscript{0.9}PbI\textsubscript{2.6}Br\textsubscript{0.4} compared to those of FAPbI\textsubscript{3}, FAPbBr\textsubscript{3} and CsPbBr\textsubscript{3}. Modes of the same vibrational origin in different LHPs are compared with FAPbI\textsubscript{3} and denoted by adjacent arrows. FAPbI\textsubscript{3} Raman modes are: octahedral distortion (43 cm\textsuperscript{-1}), translation of the A–cation (114 cm\textsuperscript{-1}), sym. (429 cm\textsuperscript{-1}) and asym. (494 cm\textsuperscript{-1}) bending of FA\textsuperscript{+} (in the case of CsPbBr\textsubscript{3}, the peak at 309 cm\textsuperscript{-1} represents a second-order phonon mode), H\textsubscript{2}N–C–NH\textsubscript{3} bending (1507 cm\textsuperscript{-1}), NH\textsubscript{2} wagging (1560 cm\textsuperscript{-1}), NH\textsubscript{2} torsion + C–H out-of-plane bending (674 cm\textsuperscript{-1}), C–H out-of-plane bending + NH\textsubscript{2} rocking (1001 cm\textsuperscript{-1}) and C–N sym. stretching (1132 cm\textsuperscript{-1}). The spectra were measured at RT using an excitation laser wavelength \(\lambda = 633\) nm.
The peaks of the high-coupling range of Zone II (50–200 cm⁻¹) are red-shifted as previously discussed. In the low-coupling range (200–500 cm⁻¹), the modes at 250 and 282 cm⁻¹ expectedly shift to higher energies: 358 and 427 cm⁻¹ respectively. Similar Raman mode frequencies of 429 and 494 cm⁻¹ are found for pure FAPbI₃. This can be understood considering that the modes in this frequency range are influenced by the internal electric field which determines the strength of the coupling. A combination of the less frequent translation of Cs⁺ atoms with the stronger PbX₆ octahedral bonds results in the weakening of the interaction between FA⁻ molecules and the PbX₆ octahedra.

The Raman modes of Zone III of Cs₀.₁FA₀.₉PbI₂.₆Br₀.₄ have quite similar frequencies to the modes of Cs₀.₁FA₀.₉PbI₃. The splitting of the mode around 520 cm⁻¹ is absent in the former case, which supports the lowering of the distortion created by the incorporation of Cs⁺. Compared to FAPbBr₃, the mixed compounds do not present a peak at 740 cm⁻¹, related to the combined vibration of NH₂ torsion and C–H out plane bending and predicted for FAPbI₃ at 674 cm⁻¹. Instead, they present a broad peak around 1064 cm⁻¹ assigned to NH₂ rocking. The activation of different modes is likely a consequence of the lattice size.

In conclusion, the incorporation of Br⁻ affects the dynamics of Cs⁺, hindering the frequency of the atomic displacement due to enhanced lattice compactness. This is expressed in the red-shift of the low-frequency range (<200 cm⁻¹). A blue shift of the low-coupled modes (from 200 to 500 cm⁻¹) of Cs₀.₁FA₀.₉PbI₂.₆Br₀.₄ towards the frequencies of the Raman modes of FAPbI₃ indicates softening in the interaction of the FA⁻ molecules and the octahedra. Therefore, the structure is stabilized in a cubic form due to the reduction of the stresses in the Pb–X bonds, resulting in a more compact crystalline lattice. In this case, the frequency of cooperative translation in the A-site is hindered by the surrounding Br⁻ atoms.

**Conclusions**

We have reported the vibrational properties of formamidinium (FA)-based LHPs investigated by micro-Raman spectroscopy. The experimental spectra were presented for the first time for the cubic forms of FAPbI₃, Cs₀.₁FA₀.₉PbI₃, and Cs₀.₁FA₀.₉PbI₂.₆Br₀.₄ hybrid perovskites. Theoretical Raman spectra were obtained for FAPbBr₃ and FAPbI₃ using DFT calculations to support the identification of the experimental Raman modes.

Low frequency Raman modes of LHPs (<50 cm⁻¹ for I-based and <65 cm⁻¹ for Br-based) can be assigned to the vibrational modes of the O₆ symmetry, twist and distortion of the octahedra. Medium frequency Raman modes (from 50 to 500 cm⁻¹) of FA-containing LHPs are derived for molecular reorganization and the consequent octahedral response, which are in-plane and out-of-plane rotations, and symmetric and asymmetric out-of-plane bending. The closeness of energies of FA⁻ modes above 500 cm⁻¹ for FAPbBr₃ and the isolated FA⁻ ions denotes a low interaction between the molecules and the PbBr₆ octahedra. This is presumed to result from the neglectable dipole moment of the FA⁻ ions.

The improved stability of FAPbI₃ due to the incorporation of Cs⁺ and Br⁻ is the result of the combined effect of both components. It is explained by the release of stresses of the Pb–X bonds, which is a consequence of a more compact lattice and a less frequent displacement of the FA⁻ ions resulting from the coupling with the Cs⁺ atoms. This is expressed in the Raman spectrum as a red-shift of the octahedra related modes (<500 cm⁻¹).

**Conflicts of interest**

There are no conflicts to declare.

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