# Constraining close binary evolution with post common envelope binaries 

vorgelegt von<br>Diplom-Physiker Ada Nebot Gómez-Morán aus Oviedo, Spanien

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Vorsitzender: Prof. Dr. M. Dähne
Berichter: PD Dr. A. D. Schwope
Berichter: Prof. Dr. H. Rauer

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A mi familia

## Zusammenfassung

Doppelsterne die aus einem Weißen Zwerg und einem Hauptreihenstern bestehen (WDMSSysteme) sind ideal, um aus ihrer Beobachtung aktuelle Theorien der Doppelsternentwicklung abzuleiten. In bislang verfügbaren Stichproben sind alte Doppelsterne mit kalten Weißen Zwergen deutlich unterrepräsentiert. Wir haben eine Durchmusterung durchgeführt, die besonders der Identifizierung und Charakterisierung dieser bislang fehlenden Systeme durch Farbselektion und spektroskopische Identifikation gewidmet war. Die neue Stichprobe umfasst 277 gesicherte WDMS-Systeme und 24 weitere Kandidaten mit unsicherer kompakter Komponente. Die kombinierten Spektren wurden in ihre Komponentenspektren zerlegt und die Sternparameter bestimmt. Die so gefundene Temperarturverteilung der Weißen Zwerge zeigt ein Maximum bei deutlich niedrigeren Temperaturen als bislang verfügbare Stichproben, ist jedoch verträglich mit der Verteilung isolierter Weißer Zwergsterne. Ebenso zeigen die Massenverteilungen einzelner Weißer Zwerge und der neuen WDMS-Stichprobe ein Maximum bei 0.6 Sonnenmassen. Im Vergleich zu früheren enthält die neue Stichprobe einen deutlich höheren Anteil Sterne vom frühen Spektraltyp M, ist aber immer noch nicht vollständig unbiased. Es wird eine untere Grenze für die Raumdichte abhängig von der Entfernung von der galaktischen Ebene zu $0.1-2 \times 10^{-4} \mathrm{pc}^{-3}$ bestimmt. Die räumliche Verteilung der neuen Objekte entspricht einer Skalenhöhe von ~ $100-150 \mathrm{pc}$ der galaktischen Scheibe.

Mit Hilfe einer Radialgeschwindigkeitsanalyse spektroskopischer Daten wurden enge Doppelsterne identifiziert, die die Entwicklungsphase einer gemeinsamen Einhüllenden durchlaufen haben. Ich bestimme eine sichere untere Grenze von $13 \%$ dieser sogenannten post common envelope binaries - PCEBs unter den WDMS-Systemen. Der Anteil der PCEBs nimmt deutlich mit abnehmender Masse der Sekundärsterne zu, insbesondere beim Übergang zu vollkonvektiven Begleitsternen. Diese Zunahme bestätigt das bislang umstrittene Modell der unterbrochenen magnetischen Bremsung, wonach der Drehimpulsverlust bei vollkonvektiven Spättypsternen deutlich reduziert werden sollte.

Aus spektroskopischen und photometrischen Folgebeobachtungen wurde die Bahnumlaufzeit von 16 WDMS Doppelsternen im Bereich von $P_{\text {orb }} 2.8$ Stunden bis zu 2 Tagen bestimmt und die Umlaufzeiten aller übrigen PCEBs zumindest eingeschränkt. Es wurden 7 Kandidaten mit langen und 15 Kandidaten mit kurzen Umlaufzeit gefunden. Die beobachtete Verteilung der Umlaufzeiten der PCEBs enthält wesentlich weniger langperiodische Systeme als durch Populationssynthese vorhergesagt wurde. Wahrscheinlich handelt es sich hier um einen Auswahleffekt, für Rückschlüsse auf die Effektivität der common-envelope Phase sind vollständige Stichproben notwendig. Eines der neu gefundenen Systeme zeigt Bedeckungen des Weißen Zwerges durch den Begleiter, dieses System wird in bezug auf die Sternparameter detailliert untersucht.

Es wird des weiteren der Einfluss der Doppelsternnatur auf die stellare Aktivität des Sekundärsterns studiert. Der Anteil aktiver Sterne steigt zu späten Spektraltypen an, im Einklang mit Untersuchungen an Feldsternen. Der Anteil aktiver Sterne unter den frühen M-Sternen ist jedoch signifikant höher als bei den Feldsternen, was auf eine charakteristisch höheres Alter der Feldsterne zurückgeführt werden kann. Die Mehrzahl der PCEB-Systeme enthält aktive Sekundärsterne mit einer größeren Äquivalentbreite der $\mathrm{H} \alpha$-Linie als bei Feldsternen gefunden wird, eine Tatsache, die zur Suche nach PCEBs unter WDMS-Systemen herangezogen werden kann.


#### Abstract

White dwarf/main sequence binaries (WDMS) are ideal systems to constrain current theories of binary star evolution. In current samples old binaries containing cold white dwarfs are significantly underrepresented. We performed a survey dedicated to identify and characterize the missing population of old white dwarf/main sequence binaries. A total of 277 white dwarf/main sequence binaries and 24 candidates were identified. We obtain their stellar parameters using a spectral decomposition method. The obtained white dwarf temperature distribution peaks at lower temperatures than previous samples but at the same temperature than the distribution of SDSS single white dwarfs. Compared to previous SDSS WDMS sample, the distribution of secondary star spectral types is slightly broader containing more early M companions, but the SEGUE WDMS population is still biased towards late spectral type secondary stars. The white dwarf mass distribution peaks at $M_{\mathrm{wd}} \sim 0.6 \mathrm{M}_{\odot}$ similar to that of single white dwarfs. A lower limit for the space density of $0.1-2 \times 10^{-4} \mathrm{pc}^{-3}$ was derived, depending on the distance from the galactic plane. The spatial distribution is in agreement with a scale-height of $\sim 100-150 \mathrm{pc}$.

From a statistical analysis of the radial velocities measured from the SDSS sub-exposures and from own spectroscopic follow-up observations we detect those binaries that have gone through a common envelope phase. I derived a lower limit to the post-common envelope binary - PCEB fraction of WDMS binaries of $\sim 13 \%$. The fraction of PCEBs increases with decreasing mass of the secondary star, and has a steep increase at the boundary where the secondary star becomes fully convective. This indicates that the angular momentum loss is less efficient at later spectral types, and according to predictions of binary population synthesis studies, in agreement with the disrupted magnetic braking law.

From spectroscopic and photometric follow-up observations we measured the orbital period of 16 WDMS binaries, in the range $2.8 \mathrm{~h}<P_{\text {orb }}<2 \mathrm{~d}$. We constrain further the orbital periods of the remaining PCEBs, finding 7 long orbital period ( $>1$ day) candidates and 15 short orbital period candidates ( $<1$ day). The observed orbital period distribution of PCEBs presents a sharp drop around 1 day, even though it is biased towards short orbital periods this drop might indicate a lower efficiency of the CE phase than thought. One of the systems is eclipsing, and we present an in-depth study of its stellar and binary parameters.

We study the influence of binarity in the stellar activity, finding that the fraction of active stars increases with the spectral type, a result found for single field red dwarfs, though we find a higher fraction at earlier spectral types. This result can be explained by the lower age of the WDMS compared with single stars of the same spectral type. The majority of the PCEBs contain active secondaries, and at a given spectral type the $\mathrm{EW}(\mathrm{H} \alpha)$ is higher than for wide WDMS binaries.


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## Chapter 1

## Introduction


#### Abstract

Most of the stars in the Galaxy are born in binary or multiple systems (Abt 1983). Many exotic objects like millisecond pulsars, Galactic black hole candidatess, LMXBs, CVs and symbiotic stars, are descendant of binary stars. The standard candles, supernovae type Ia, are also a product of close binary evolution. With the discovery of the first binary pulsar by Russel A. Hulse and Joseph H. Taylor, Jr., Einstein's general relativity prediction on how compact objects loose angular momentum due to gravitational wave emission can be tested against alternative theories. Finding that made Hulse and Taylor win the Nobel Prize in 1993 and with the space mission LISA we will be able to proof. Despite the relevance of binary stars our understanding of their evolution is still incomplete. The mentioned systems have in common that they all went through a common envelope (CE) phase. To answer the main questions of close binary evolution we focus our study in one type of binaries that suffered from a CE phase: white dwarf main sequence binaries (WDMS). We choose these objects becuase they are very numerous, so that we can make a good analysis based on large samples; unlike cataclysmic variables they have no accretion so that we can derive easily the stellar parameters of the two components; and the individual evolution of the components is well understood.


### 1.1 WDMS components and their individual evolution

To know how the spectral energy distribution (SED) of WDMS binaries is and how they evolve it is needed to know how the SED looks like for the individual components and to understand how the evolution is for single stars. The last becomes evident when asking the question when do stars enter the CE phase? This depends on the initial orbital separation and also on the initial masses. Stars on the main sequence expand so to answer this question we need to know how much they do it dependent on their mass. We now proceed to describe the most relevant characteristics of the SED of the red dwarf and the white dwarf and secondly we briefly describe their evolution.


Figure 1.1: DA and DB white dwarf template SDSS spectra with HI and HeI absorption lines marked (left). M0, M3 and M6 templates created with SDSS spectra of red dwarfs with several molecular absorption bands and lines marked (right).

### 1.1.1 The red dwarf

Low mass stars ( $<0.5 \mathrm{M}_{\odot}$ ) represent a large fraction of all the stars in the Galaxy. Their temperatures and gravity are in the ranges $2800-3800 \mathrm{~K}$ and $4.2-5.5$ respectively. Due to their low temperatures, their spectral energy distribution is dominated by strong molecular absorption bands of titanium oxide (TiO), vanadium oxide (VO), PC and CaH in the optical, and by $\mathrm{H}_{2} \mathrm{O}$ and CO in the infrared, with almost no true continuum present. A detailed list of lines present in their spectra can be found in Kirkpatrick et al. (1991) and some of these molecular bands together with some characteristic lines are shown in Fig. 1.1 for three different spectral types, M0, M3 and M6. The strength of the titanium oxide, the vanadium oxide and the PC bands are correlated with the temperature of the star, and several indexes have beed defined and used to determine the spectral type of this cool stars (Kirkpatrick et al. 1991; Cruz \& Reid 2002; Martín et al. 1999).

## Evolution of the red dwarf

Evolutionary tracks from Baraffe et al. (1998) are shown in the Hertzsprung-Russel diagram (L$T_{\text {eff }}$ diagram) in the left panel of Fig. 1.2 for three different masses, $M_{\mathrm{sec}}=0.1 \mathrm{M}_{\odot}, M_{\mathrm{sec}}=0.3 \mathrm{M}_{\odot}$, and $M_{\text {sec }}=0.5 \mathrm{M}_{\odot}$ from left to right. Overplotted are two different isochrones, corresponding to 1 Myr (dotted) and to 1 Gyr (dashed) (we chose for the mixing length parameter $\alpha=1$ and $\mathrm{Z}=0.02$ ). In the right panel we show the associated change of the radius over the time. There is a pre-main-sequence (MS) contraction that can last from 0.1 Gyr for a $0.5 \mathrm{M}_{\odot}$ star and up to 1 Gyr for the lower mass. Due to gravitational contraction the central temperature increases and H burning starts, leading the star to a hydrostatic equilibrium if its mass is larger than $0.15 \mathrm{M}_{\odot}$. Stars below this mass don't reach H burning, since they are too dense and cold their pressure


Figure 1.2: Tracks in the $\log L-\log T_{\text {eff }}$ plane for three different masses, $\mathrm{M}=0.5 \mathrm{M}_{\odot}, 0.3 \mathrm{M}_{\odot}$ and $0.1 \mathrm{M}_{\odot}$ from top to bottom (left panel), and associated change in the radius of the star in time (right panel).
is dominated by degenerate electrons, and keep on contracting, until they reach the limit in radius of fully degenerate stars (corresponding to $T_{\text {eff }}=0 \mathrm{~K}$ ). For those stars that do reach H burning the presure is governed by its classical value, so that a decrease in radius involves a decrease in luminosity, $L \propto R^{2} T_{\text {eff }}{ }^{4}$ (from 0.001 Gy to 0.1-1 Gyr). Once the star reaches thermal equilibrium the luminosity will be dominated by nuclear reactions and further evolution of the system becomes very slow (from 0.1-1 Gyr to 10 Gyr ). During the pre-MS phase the star moves to higher temperatures and to lower luminosities. The evolution of low mass stars once they are on the MS is very slow. An isochrone of 10 Gy would be at almost the exact position of the 1 Gyr isochrone. A star with a $0.6 \mathrm{M}_{\odot}$ would increase it's radius by only by a $3 \%$.

### 1.1.2 The white dwarf

White dwarfs are the latest stage of the evolution of low and intermediate mass stars, from 0.07 to $8 \mathrm{M}_{\odot}$ (Fontaine et al. 2001). They have a typical mass of $0.6 \mathrm{M}_{\odot}$, with sizes typical of planets, making these objects have very high gravities, $\log g \sim 8$. Their luminosities cover a very broad range, from $L \sim 10^{2} \mathrm{~L}_{\odot}$ at the begining of the cooling sequence to $L \sim 10^{-5} \mathrm{~L}_{\odot}$ (see Fig. 1.6).

Evolutionary tracks from Salasnich et al. (2000) ${ }^{1}$ with $\mathrm{Z}=0.019$ and $\mathrm{Y}=0.273$ are shown in the HR diagram in the left panel of Fig. 1.3 for three masses, $\mathrm{M}=2.2 \mathrm{M}_{\odot}, 7 \mathrm{M}_{\odot}$ and $12 \mathrm{M}_{\odot}$. In the right panel of the same figure we show the associated expansion of the stars. In all cases a star expands by large factors before becoming a WD. A $2.2 \mathrm{M}_{\odot}$ star will have a radius $\sim 30$ $R_{\odot}$ at the tip of the RGB, a star with a mass of $7 \mathrm{M}_{\odot}$ will have a radius $\sim 100 R_{\odot}$ at the AGB, while a star with a mass of $12 \mathrm{M}_{\odot}$ at the AGB will have a radius of up to $\sim 1000 R_{\odot}$. This tells

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Figure 1.3: Tracks in the $\log L-\log T_{\text {eff }}$ plane for three different masses, $\mathrm{M}=12 \mathrm{M}_{\odot}, 7 \mathrm{M}_{\odot}$ and $2.2 \mathrm{M}_{\odot}$ from top to bottom (left panel), and associated change in the radius of the star in time (right panel).
us the maximum orbital separation allowed for a companion star before filling it's Roche lobe and entering the CE phase. For a secondary star of $0.5 \mathrm{M}_{\odot}$, this implies that if the binary has a $P_{\text {orb }}<100-200$ days ( $0.5-1 \mathrm{AU}$ ) the system will enter a CE phase in the RGB, systems with longer period but shorter than 2000 days ( $\sim 6 \mathrm{AU}$ ) will enter a CE while in the AGB.

A white dwarf is formed once the outer envelope of a star is expelled. The chemical composition of the core depends on the stage the WD was formed. Low mass stars, $M<2.2 \mathrm{M}_{\odot}$ will loose their H envelope in the RGB, so that they don't ignite He . The resulting WD has a core with mainly He in it (He-WD), and has $M_{\text {wd }} \sim 0.15-0.45$ (the upper limit is defined by the onset of He -flash). It is widely thought that all He -WDs are consequence of binary evolution (Marsh et al. 1995). Intermediate mass stars that loose their envelope during the AGB will have a carbon oxygen core (CO-WD) if they don't start C burning, $M<6-8 \mathrm{M}_{\odot}$. The resulting WD has $M_{\mathrm{wd}} \sim 0.45-1.1$ (the upper limit is defined by the onset of C ignition). Stars with higher masses, up to $\sim 12 \mathrm{M}_{\odot}$ will loose their envelope at the tip of the AGB and will have a core composed of oxygen and neon (ONe-WD) and their mass is in the range $M_{\mathrm{wd}} \sim 1.1-1.38 \mathrm{M}_{\odot}$.

From observations we have learnt that small amounts of H and He are left over after the mass-loss phase during the PN phase (thought to be the precursors of most of the WDs), that suround the core of the WD. The SED of white dwarfs is dominated by the continuum and some absorption lines. If only Balmer lines are present they are classified as DA, DB contain only He and DC show only a continuum. Other white dwarfs have HeII (DO), carbon features (DQ) or some metal lines (DZ) (Sion et al. 1983). Examples of DA and DB white dwarfs are shown in the left panel of Fig. 1.1 with H and He absorption lines marked. We show their location in the color-color diagram in Fig. 1.5 together with the cooling tracks from Wood (1995) (data was taken from Eisenstein et al. (2006)).


Wavelength [Angstroms] Wavelength [Angstroms]

Figure 1.4: Normalized Balmer lines, $\mathrm{H} \alpha-\mathrm{H} 7$ as a function of $T_{\text {eff }}$ (left) for a DA with $\log g=8$ and as a function of $\log g$ (right) for a DA with $T_{\text {eff }}=20000 \mathrm{~K}$. We used the DA models from Koester et al. (2005).


Figure 1.5: Color-color diagram for a sample of WDs from Eisenstein et al. (2006) and cooling tracks (lines) from Wood (1995) for four different DA masses. Different colors are used for WDs of different spectral type.

The equivalent widths of the Balmer lines depend on temperature and gravity and they are used to determine these parameters on DA white dwarfs ${ }^{2}$. In the left panel of Fig. 1.4 we plot the normalized Balmer lines from $\mathrm{H} \alpha$ to H 7 from top to bottom for three DAs with effective temperatures of 30000 K (solid line) 20000 K (dotted line) and 10000 K (dashed line), fixing $\log g=8$. In the right panel of Fig. 1.4 we plot again the normalized Balmer lines but this time for three DAs with same effective temperatures ( $T_{\text {eff }}=20000 \mathrm{~K}$ ) but different gravity, $\log g=6$ (solid line), $\log g=7$ (dotted line) and $\log g=8$ (dashed line). Colder DAs have deeper lines and, the higher the gravity the broader and shallower the line becomes. This implies that alone with the EW we are not able to discern whether a DA is cold and massive or hot and light, so we need an independent index, for instance the slope of the continuum.

## Evolution of the white dwarf

White dwarfs produce no energy by nuclear reaction in their core, and pressure from the degenerate electrons prevents further contraction, and since no other source of energy is available the fate of the WD is to cool. As consequence of degeneracy the temperature is independent of the pressure so they will evolve at constant radius. Degenerate electrons conduct heat very well, so

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Figure 1.6: HR diagram (left panel) and cooling traks (right) from Wood (1995) for four different DA masses.
that the core is isothermal, and can have temperatures in the range $T_{c}=10^{6}-10^{7} \mathrm{~K}$, only in a very thin outer layer the temperature drops to $T_{\text {eff }}=60000-6000 \mathrm{~K}$, giving rise to convection for the cooler WDs. Luminosity is produced by thermal energy from the non-degenarate ions. As the WD cools the ions loose kinetic energy, changing their state from gas to fluid and finally to solid, until the WD becomes a crystalized object, a black dwarf. In the HR diagram shown in the left panel of Fig. 1.6 we plot the evolutionary tracks from Fontaine et al. (2001) ${ }^{3}$ for 4 WDs, $0.4 \mathrm{M}_{\odot}, 0.6 \mathrm{M}_{\odot}, 1 \mathrm{M}_{\odot}$, and $1.2 \mathrm{M}_{\odot}$, from left to right. In this double logarithmic representation the luminosity is linear with the temperature and has a slope of $\sim-4$.

Most of the stars will end up becoming a WD, so that the coolest WDs can be used to estimate the age of a certain population in the Galaxy. The cooling of WDs depends on the thermal energy content of the core and how fast it is transfered from the core, through the envelope to the interstellar medium. Inmediately after the PN phase, WD are hot enough so that they can produce large amounts of neutrinos, taking with them energy and cooling the WD. Once the neutrino cooling phase has finished the cooling age depends only on the thermal energy stored in it's core and the opacity of the outer layers, of the atmosphere (Fontaine et al. 2001). Cooling tracks from Wood (1995) are shown in the right panel of Fig. 1.6 for three different DA masses. We see that the cooling depends on the mass of the white dwarf, so that if we only know the effective temperature $T_{\text {eff }}$ we will not be able to discern the cooling age of the WD.

[^2]
### 1.2 Evolution of close binary stars

The evolution of binaries depends crucially on the initial separation and the stellar masses of the components. If the initial orbital separation of the binary is small enough, as the more massive star evolves, increasing its radius untill it fills its Roche Lobe (region where the material is bound to the gravitational field of the star) when it reaches the Giant Branch or the Asymptotic Giant Branch, matter is transferred to the companion star. If the mass transfer is faster than the thermal time-scale (time a star needs to readjust to thermal equilibrium), the system enters a common envelope phase (CE), where the core of the more massive star, i. e. a white dwarf, and the companion star are surrounded by the envelope of the former. The stars start a spiral-in process, friction between the binary and the non-corotating envelope extract energy and angular momentum from the orbit, leading to a rapid decrease of the orbit. This phase is thought to happen very fast and planetary nebulae with central binary stars are probably the closest objects to the CE phase which are known (see de Marco 2009, for a review on PNe). Further evolution of the system, known as post-common envelope binary (PCEB) is driven by angular momentum loss due to gravitational radiation and to magnetic braking and it may bring the system into a semidetached configuration, i. e. a cataclysmic variable (CV). Both, the energetics of the CE phase and angular momentum loss via a magnetized stellar wind are not well understood and motivated the current project.

### 1.2.1 Common envelope phase

Although the basic idea of the CE phase has been outlined already 30 years ago (Paczyński 1976), it is still the least understood phase of compact binary evolution. We have learned from theoretical simulations that this phase might be very short ( $\sim 10^{3}$ yrs) (Hjellming \& Taam 1991). Because of the short duration the chances of observing a binary during this phase are very small, even worse it would be imposible to see the binary inside the envelope. But simulations make a prediction which can be tested, the outcome of the common envelope phase: elliptical or bipolar planetary nebula with a binary in it's center (Sandquist et al. 1998). And indeed these objects are observed (see de Marco 2009). These are very important findings but with current theories it is not possible to link the initial parameters of the binary with the outcome of the common envelope. Therefore theoretical binary population studies (Willems \& Kolb 2004) usually deal with a simple idea: a certain fraction $\alpha_{C E}<1$ of the binary's binding energy which is released in the spiraling-in process is used to unbind the CE (Webbink 1984):

$$
\begin{gather*}
E_{C E}=\alpha_{C E} \Delta E  \tag{1.1}\\
-\frac{G M_{1, i} M_{C E}}{\lambda R_{1, i}}=\alpha_{C E} \frac{G M_{c} M_{2}}{2}\left(\frac{1}{a_{i}}-\frac{1}{a_{f}}\right), \tag{1.2}
\end{gather*}
$$

leading to the relation between inital and final separations

$$
\begin{equation*}
a_{f}=a_{i} \frac{M_{c}}{M_{1, i}}\left(1+\frac{2}{\lambda \alpha_{C E} r_{L, 1}} \frac{M_{e n v}}{M_{2}}\right), \tag{1.3}
\end{equation*}
$$

where $a_{i}$ and $a_{f}$ are the initial and final orbital separation of the binary. $M_{1, i}$ and $M_{2}$ are the primary and secondary masses at the start of the $\mathrm{CE}, M_{c}$ is the mass of the primary's core and $r_{L, 1}$ is the primary's Roche lobe in units of the binary separation. It is assumed that $M_{2}$ does not change during the common-envelope phase. The structural parameter $\lambda$ is the giant envelope's binding energy parameter, and it's value depends on the initial mass of the primary and it's evolution. The higher the initial mass the deeper the envelope will be when becoming a giant and the less bound it will be to the star, also the moment in which the CE phase starts is important since in the AGB the star has a larger radius and the envelope will be less bound to the core. Some values of the structural parameter can be found in Tauris \& Dewi (2001). Davis et al. (2009) have investigated the dependency of $\alpha_{C E}$ on the secondary mass and in contrast with previous works where $\lambda$ was taken as a constant (typically $\lambda \simeq 0.5$ ) they calculate it's value from stellar evolution models. They can reproduce most of the PCEBs by models with $\alpha_{C E}>0.1$, but for one system they find a very high value $\alpha>3$, which they claim can be explained by another source of energy rather than gravitational potential energy, like for example thermal and ionization energy of the giant's envelope. But this might indicate that there are still some missing ingredients in their recipe.

### 1.2.2 Post common envelope binaries

Once the common envelope is expelled, the remaining system consist of a main sequence star and a remnant of the more massive star, e.g. a white dwarf, perhaps surrounded by the ejected material that can be ionized forming a planetary nebula (Paczyński 1976; Iben \& Livio 1993). Until 2003 there were only about 30 PCEBs with well defined orbital parameters ( $P_{\text {orb }}, M_{\text {sec }}, M_{\text {wd }}$, $T_{\text {eff }}$ ). Schreiber \& Gänsicke (2003) studied these systems in detail. They realized that most of the systems contained relatively hot white dwarfs and late-type companions. These biases could be understood as a natural way of discovery, that is as blue objects which later on presented some infrared excess. They calculated the evolutionary state for all the systems, that is their age in terms of CV evolution, noticing that they had only lived a small fraction of their lifes as PCEB. That made them think for the first time that an old population characterized by cold white dwarfs should exist.

Since then, the Sloan Digital Sky Survey turned out to be very efficient at discovering new white dwarf-main sequence binaries (see Silvestri et al. 2006; Rebassa-Mansergas et al. 2007; Heller et al. 2009), but biases towards hot white dwarfs plus secondaries with late spectral types are still present. These biases can be easily understood since the WDMS binaries were discovered as a byproduct of one of the main targets of the SDSS: quasars, which resemble colors of hot white dwarfs plus late secondaries. Among these sample of WDMS binaries a fraction of them, $\sim 25 \%$ are PCEBs (Willems \& Kolb 2004), while the remaining are wide binaries, where the components never interacted and evolved as single stars.

We made a compilation of the published (until the present date, February 2010) WDMS binaries that suffered from a CE phase and in table 1.2 .2 we list their orbital periods and stellar parameters. This sample comprises $\sim 50$, covers a rather narrow range of secondary masses and
is dominated by hot white dwarfs and late secondaries, serendipitously discovered in the blue. To constrain better the CE efficiency it is much needed a sample of PCEB covering a large range in both effective temperature and in mass of the secondary.

Table 1.1: Stellar parameters of known close WDMS.

| Name | Porb [d] | Sp1 | Sp2 | $T_{\text {eff }}$ | $M_{\text {wd }}\left[\mathrm{M}_{\odot}\right]$ | $M_{\text {sec }}\left[\mathrm{M}_{\odot}\right]$ | $R_{\text {sec }}\left[R_{\odot}\right]$ | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1541-3809 | 7.7047 | DA | dM |  |  |  |  | ${ }^{\text {a }}$ |
| FS Cet | 4.23160 | DAO | M1-2.5 | $57000 \pm 2000$ | $0.57 \pm 0.03$ | $0.39 \pm 0.02$ | $0.43 \pm 0.02$ | $b$ |
| J1629+7804 | 2.89: | DA1 | M3/5 |  |  |  |  | c |
| BE UMa | 2.291166 | DAO | K3-4/5 | $4750 \pm 150$ | $0.59 \pm 0.07$ | $0.25 \pm 0.08$ | $0.72 \pm 0.05$ | d |
| 2147-1405 | 1.4972 | DA | dM |  |  |  |  | a |
| IN CMa | 1.262396 | DAO1 | M5e/5 | $52400 \pm 1800$ | $0.58 \pm 0.03$ | $0.43 \pm 0.03$ | $0.47 \pm 0.03$ | $b$ |
| 1319-2849 | 0.8758 | DA | dM |  |  |  |  | a |
| 2123-4446 | 0.8499 | DA | dM |  |  |  |  | $a$ |
| $1136+6646 \mathrm{AB}$ | 0.83607 | DAO | K4-7/5 | 70000 | 0.82 | 0.36 |  | e |
| J1016-0520AB | 0.78928 | DAO | K5-M2/5 | $55000 \pm 1000$ | $0.63 \pm 0.02$ | $0.15 \pm 0.02$ |  | $f$ |
| 2009+6216 | 0.741226 | DA2 | M5/5 | 25870 | 0.61-0.64 | 0.1845-0.1925 |  | $g$ |
| J1414-0132 | 0.727 | DA | M5 | $14065 \pm 1452$ | $0.80 \pm 0.17$ |  |  | $h$ |
| J0246+0041 | 0.726 | DA | M3 | $16600 \pm 1600$ | $0.9 \pm 0.2$ | $0.38 \pm 0.07$ | $0.39 \pm 0.08$ | ${ }^{i}$ |
| J2013+4002 | 0.705517 | DAO | M3-4/5 | $48000 \pm 900$ | $0.56 \pm 0.03$ | $0.23 \pm 0.01$ | $0.29 \pm 0.01$ | $b$ |
| EG UMa | 0.667579 | DA4 | M4-5/5 | $13125 \pm 125$ | 0.63 |  |  | j |
| J2339-0020 | 0.6560 | DA | M4 | $13300 \pm 2800$ | $0.8 \pm 0.4$ | $0.32 \pm 0.09$ | $0.33 \pm 0.10$ | i |
| UZ Sex | 0.597259 | DA3 | M3-5/5 | $17600 \pm 2000$ | $0.65 \pm 0.2$ | $0.22 \pm 0.05$ | $0.25 \pm 0.03$ | $k$ |
| HZ 9 | 0.56433 | DA2 | M5e/5 | $20000 \pm 2000$ | 0.51 |  |  |  |
| V471 Tau | 0.521183 | DA2 | K2/5 | $34500 \pm 1000$ | $0.84 \pm 0.05$ | $0.93 \pm 0.07$ | $0.96 \pm 0.04$ | ecl ${ }^{m}$ |
| J2130+4710 | 0.521036 | DA | M3.5 | $18000 \pm 1000$ | $0.554 \pm 0.017$ | $0.555 \pm 0.023$ | $0.534 \pm 0.053$ | $\mathrm{ecl}^{n}$ |
| 1334-3237 | 0.469 | DA | K2-M2/5 |  |  |  |  | $o$ |
| J1047+0523 | 0.382 | DA | M5 | $12392 \pm 1847$ | $0.38 \pm 0.20$ |  |  | $h$ |
| 1247-1738 | 0.362 | DA | M3-5/5 |  |  |  |  | o |
| DE CVn | 0.364139 | DA7 | M2/5 | 8000 | $0.51 \pm 0.02$ | $0.41 \pm 0.06$ | $0.37 \pm 0.06$ | ecl ${ }^{p}$ |
| 1432-1625 | 0.350 : | DA | M3-4/5 |  |  |  |  | $o$ |
| GK Vir | 0.344331 | DAO | M3-5/5 | $48800 \pm 1200$ | $0.51 \pm 0.04$ | 0.1 | 0.15 | ecl ${ }^{q}$ |
| 1042-6902 | 0.336785 | DA3 | M5 | $19960 \pm 400$ | $0.55 \pm 0.05$ | $0.14 \pm 0.01$ | $0.19 \pm 0.02$ | $b$ |
| J1212-0123 | 0.335871 | DA | M3-5/5 | $17700 \pm 300$ | $0.47 \pm 0.1$ | 0.26-0.29 | $0.3 \pm 0.01$ | $\mathrm{ecl}^{r}$ |
| J1724+5620 | 0.333019 | DA | M3-5 | $35800 \pm 300$ | $0.42 \pm 0.01$ | 0.25-0.38 | 0.26-0.23 |  |
| J0110+1326 | 0.332687 | DA | M3-5/5 | $25900 \pm 427$ | $0.47 \pm 0.2$ | 0.255-0.38 | 0.262-0.36 | ecl ${ }^{s}$ |
| RR Cae | 0.303704 | DAwk | M3-4/5 | 7000 | $0.44 \pm 0.02$ | $0.183 \pm 0.013$ | 0.188-0.23 | $\mathrm{ecl}^{a}$ |
| J2125-0107 | 0.289822 | DQZO | M | 90000 | 0.6 | $0.4 \pm 0.1$ | $0.4 \pm 0.1$ | $t$ |
| CC Cet | 0.286654 | DA2 | M4.5 | $26200 \pm 2000$ | $0.40 \pm 0.1$ | $0.18 \pm 0.05$ | $0.21 \pm 0.02$ | $k$ |
| 2313-3303 | 0.2795 | DA | dM |  |  |  |  | $a$ |
| 2154+4048 | 0.26772 | DA2 | M3.5/5 |  |  |  |  | $u$ |
| 1857+5144 | 0.266334 | DAO | M4-6/5 | $70000-100000$ | 0.6-1.0 | 0.15-0.30 |  | $v$ |
| J0314-0111 | 0.2633 | DA | M4 |  | $0.65 \pm 0.1$ | $0.32 \pm 0.09$ | $0.33 \pm 0.1$ | $i$ |
| LM Com | 0.258687 | DA | M4+/5 | 29300 | 0.35 | 0.17 | 0.22 | w |
| BPM 71214 | 0.201626 | DA | K2-M3/5 | $17200 \pm 1000$ | 0.77 |  |  | $x$ |
| J1042+6442 | 0.197669 | WD | M3 | 9800 |  |  |  | ${ }^{2}$ |
| J1548+4057 | 0.185518 | DA | M6/5 | $11700 \pm 820$ | 0.614-0.678 | 0.146-0.201 | 0.166-0.196 | $\mathrm{ecl}^{s}$ |
| MS Peg | 0.173666 | DA2 | M3-5/5 | 22170 | $0.48 \pm 0.02$ | $0.22 \pm 0.02$ | $0.27 \pm 0.02$ | w |
| J1529+0020 | 0.1651 | DA | M5 | $14100 \pm 500$ | $0.40 \pm 0.04$ | $0.25 \pm 0.12$ | $0.26 \pm 0.13$ | $i$ |

Table 1.1: continued.

| Name | Porb [d] | Sp1 | Sp2 | $T_{\text {eff }}$ | $M_{\mathrm{wd}}\left[\mathrm{M}_{\odot}\right]$ | $M_{\sec }\left[\mathrm{M}_{\odot}\right]$ | $R_{\text {sec }}\left[R_{\odot}\right]$ | Ref. |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| IR Peg | 0.164 | DO1 | M3/5 |  | $0.61 \pm 0.02$ |  | $y$ |  |
| QS Vir | 0.150758 | DA | M2-5/5 | $14085 \pm 100$ | $0.78 \pm 0.04$ | $0.43 \pm 0.04$ | $0.42 \pm 0.02$ | $\mathrm{ecl}^{z}$ |
| J0908+0604 | 0.149438 | DA2.8 | M3/5 | $17500 \pm 500$ | $0.35 \pm 0.04$ | 0.32 | 0.33 | $\mathrm{ecl}^{\text {a }}$ |
| LTT 560 | 0.148 | D | M5/5 | $\sim 7500$ | $0.52 \pm 0.12$ | $0.19 \pm 0.05$ | 0.11 | $b 2$ |
| J1151-0007 | 0.1416 | DA | M6/5 | $10400 \pm 200$ | $0.6 \pm 0.1$ | $0.19 \pm 0.08$ | $0.19 \pm 0.1$ | $i$ |
| J0303+0054 | 0.134438 | DC | M4-5/5 | $i 8000$ | $0.878-0.946$ | $0.224-0.282$ | $0.246-0.27$ | $\mathrm{ecl}^{s}$ |
| NN Ser | 0.130080 | DAO1 | M4.75/5 | $55000 \pm 8000$ | $0.54 \pm 0.05$ | $0.15 \pm 0.008$ | $0.174 \pm 0.009$ | $\mathrm{ecl}^{c 2}$ |
| J1435+3733 | 0.125630 | DA3.6 | M4-5/5 | $12500 \pm 488$ | $0.48-0.53$ | $0.19-0.246$ | $0.218-0.244$ | $\mathrm{ecl}^{s}$ |
| 2237+8154 | 0.123681 | DA | M3.5 | $11500 \pm 1500$ | $0.47-0.67$ | $0.2-0.4$ |  | $d 2$ |
| 1606+0153 | 0.1182 | DA | dM |  |  |  | $a$ |  |
| J0052-0053 | 0.11396 | DA | M4 | $16000 \pm 4400$ | $1.2 \pm 0.4$ | $0.32 \pm 0.09$ | $0.33 \pm 0.1$ | $i$ |
| HR Cam | 0.103063 | DA2.7 | M/5 | 19000 | $0.41 \pm 0.01$ | $0.096 \pm 0.004$ | $0.125 \pm 0.02$ | $f 2$ |
| 01373457 | 0.0803 | DA | L8 |  | 0.39 | $0.053 \pm 0.0006$ | $g^{2}$ |  |

[^3]
### 1.2.3 Evolution into CVs

Further evolution of the system, driven by angular momentum loss due to gravitational wave radiation (GR) and magnetized stellar wind, magnetic braking (MB), will bring the system into semicontact. The secondary star fills it's Roche lobe, and mass transfer starts, forming a CV. The evolutionary time scale for a PCEB to become a CV can be determined by the sum of the GR time scale and the MB time scale, for which we have to assume a certain AML prescription. While GR is well established, MB is still in debate. CVs evolve from long to short orbital periods. At long orbital periods, $P_{\text {orb }}>3$ hours, the secondary stars are sufficiently massive so as to have a radiative core and angular momentum via MB is supposed to be efficient. Once the donor secondary star becomes fully convective, $P_{\text {orb }} \simeq 3$ hours, magnetic braking is not efficient and the AML via MB stops. The secondary then has time to relax to its thermal equilibrium and mass transfer ceases, becoming a detached CV. The only mechanism leading to AML is emission of gravitational waves. Evolution happens in a much longer time scale giving rise to the observed orbital period gap. At $P_{\text {orb }} \sim 2$ hours the secondary star fills its Roche lobe again and mass transfer restarts, so that a CV is again visible. The orbital period continues decreasing until the secondary star becomes a degenerate brown dwarf at around 80 minutes, and at this point the orbital period starts to increase, this systems are known as bouncers. This is the so called disrupted magnetic
braking law (DMB) and was firstly proposed by Verbunt \& Zwaan (1981). The DMB was put into question since although it could explain the observed mentioned gap, observations of single low mass stars do not show any evidence for such a discontinuity (Pinsonneault et al. 2002). Also DMB predicts a minimum $P_{\text {orb }} 10 \%$ shorter than the observed value and also a pile-up and spike of systems at short orbital periods. Other magnetic braking laws have been proposed, but none of them can explain the presence of a gap in the $\mathrm{CV} P_{\text {orb }}$ distribution. Recently Gänsicke et al. (2009) have discovered the spike of CV at short orbital period, demonstrating that our picture of the CV orbital period was not complete and pointing again to the validity of the DMB.

### 1.2.4 Aim and layout of the thesis

The work presented in this thesis forms part of a large collaboration that has been working in the last years looking for answers to the main questions of close binary evolution: What is the efficiency of the CE phase removing AM from the orbit? What is the strength of magnetic braking, and does MB get disrupted when the secondary star becomes fully convective? The work presented in this thesis focuses in a well defined sample of WDMS, representing the older population of WDMS binaries. By finding the PCEBs among the WDMS binary sample, measuring their stellar and binary parameters and comparing with the outcome of binary population synthetic studies we aim to answer these questions.

This thesis is structured in the following way. We firstly describe the first dedicated WDMS binary survey, with a detailed analysis of all the systems found, meaning that we estimate fundamental stellar parameters and compare with other studies of WDMS. This sample combined with the most complete SDSS-database from Rebassa-Mansergas et al. (2009) provides the database for testing the current prescriptions of the CE phase and for constraining magnetic braking. We examine the systems and look for those that went through a CE phase, and estimate the orbital period of some of them. We analyze the activity-binarity relation searching for a possible enhancement in close binaries. We describe in detail the relevance of eclipsing binaries and analyze a serendipitously discovered one. We finish by summarizing the main results. Individual chapters are organized like normal journal papers becuase they either are published as such or will be submitted soon.

## Chapter 2

## White dwarf/main sequence binaries identified within SEGUE

White dwarf/main sequence binaries (WDMS) are ideal systems to constrain current theories of binary star evolution. In current samples of these systems old binaries containing cold white dwarfs are significantly underrepresented. As partners of SEGUE we performed a survey especially dedicated to identify and characterize the missing population of old white dwarf/main sequence binaries. On 240 spectroscopic plates our color selection algorithm selected 9531 candidates of which 431 have been observed spectroscopically. Among these we find 277 white dwarf/main sequence binaries and 24 candidates resulting in a success rate of $\sim 70 \%$. For the identified binaries we obtain the stellar parameters, such as the spectral types of the main sequence secondary stars, the distances, the white dwarf temperatures, and the masses using a spectral decomposition method. The obtained white dwarf temperature distribution peaks at lower temperatures than previous samples but at the same temperature as the distribution of SDSS single white dwarfs. Compared to previous WDMS sample, the SEGUE WDMS distribution of secondary star spectral types is slightly broader containing more early M companions. Although covering a larger parameter space than previous samples, the SEGUE WDMS population is still biased towards late spectral type secondary stars. The white dwarf mass distribution peaks at $M_{\text {wd }} \sim 0.6 \mathrm{M}_{\odot}$ similar to that of single white dwarfs but contains significantly more high mass white dwarfs. The distances to the WDMS in our sample range from 50 to 1500 pc. For the space density of WDMS we derive a lower limit of $0.1-2 \times 10^{-4} \mathrm{pc}^{-3}$ depending on the distance from the galactic plane. The spatial distribution of the SEGUE WDMS sample is in agreement with a typical scale-height of $\sim 100-150 \mathrm{pc}$.

### 2.1 Introduction

WDMS represent the most numerous compact binaries in the universe. The population of WDMS binaries consists of two types of systems which differ due to their evolutionary history. Accord-
ing to recent binary population synthesis calculations more than $75 \%$ are wide binaries in which the stellar components evolve like single stars (Willems \& Kolb 2004). Virtually all of the remaining $\leq 25 \%$ suffered from common envelope evolution when the more massive star left the main sequence. This population of PCEBs represents the largest population of close compact binaries.

The first survey identifying large numbers of WDMS is the Sloan Digital Sky Survey (SDSS): based on SDSS imaging and some DR $1{ }^{1}$ spectra Smolčić et al. (2004) identified a new stellar locus in color-color diagrams, i.e. the WDMS binary bridge. Later, the SDSS turned out to be also very efficient in spectroscopically identifying new unresolved WDMS binaries, e.g. Silvestri et al. (2006) published a list of $\sim 747$ new WDMS binary systems found in SDSS/DR4 and later Silvestri et al. (2007) published a list of more than 1200 systems based on SDSS/DR5. The latest and biggest compilation based in the DR 6 has been done by Rebassa-Mansergas et al. (2009). A significant fraction of these WDMS are PCEBs. These large WDMS sample hide a significant fraction of PCEBs. Since 2007 we run an extensive follow-up program of WDMS discovered by the SDSS to identify a large sample of PCEBs (Rebassa-Mansergas et al. 2007, 2008; Schreiber et al. 2008; Nebot Gómez-Morán et al. 2009; Pyrzas et al. 2009). The final goal of this project is to derive clear constraints on theories of magnetic braking and common envelope evolution as suggested by Schreiber \& Gänsicke (2003); Nelemans \& Tout (2005); Politano \& Weiler (2006); Davis et al. $(2008,2009)$. To obtain the desired constraints it is essential that the used sample of WDMS binaries covers a large range of secondary star spectral types and white dwarf temperatures to avoid obtaining a biased sample of PCEBs.

In this chapter we describe a WDMS survey we carried out as a part of SEGUE (Yanny et al. 2009). It has been especially designed to identify the old population of WDMS binaries that is underrepresented in previous samples. The outline of the chapter can be described as follows. In Sect. 2.2 we discuss color selection algorithms of WDMS and present our criteria to identify systems containing cold white dwarfs before we present the final SEGUE-WDMS sample in Sect.2.3. Then we derive the stellar parameters of the WDMS binaries using a spectral decomposition method in Sect. 2.4 and discuss the obtained distributions (Sect.2.5). Finally, in Sect. 2.6 and 2.7 we analyze the completeness of our survey and derive constraints on the space density and the scale height of the WDMS population in our galaxy.

### 2.2 White dwarf/main sequence binary color selection

Since the identification of the WDMS bridge (Smolčić et al. 2004), several attempts have been made to develop color selection criteria to select WDMS candidates using the ugriz magnitudes provided by the SDSS. In the following we review those critically and present our own selection criteria especially designed to identify old WDMS.

[^4]

Figure 2.1: ugriz color-color diagrams to discuss WDMS target selection algorithms. Quasars and single stars are shown in yellow and grey respectively. Based on data provided by Pickles (1998), Bergeron (private communication), and using the empirical color transformations presented by Jordi et al. (2006), we calculated colors for WDMS binaries. The calculated colors cover the spectral types from K0 to M6 for the main sequence star and effective temperatures of the white dwarf from 6000 to 60000 K . In the above color-color diagrams tracks from K0 to M6 are shown for five effective temperatures of the white dwarf: 40000 K (blue), 30000 K (cyan), 20000 K (green), 15000 K (magenta), 10000 K (red). Grey shaded in the upper panels are the color cuts used by Raymond et al. (2003) and Silvestri et al. (2006) until 2005. Obviously these cuts lead to the detection of only a small part of the WDMS population as especially the "blue" cut (left panel) selects mainly systems with hot white dwarfs ( $T_{\text {eff,WD }} \gtrsim 15000 \mathrm{~K}$ ) and/or late type secondary stars (later than $\sim$ M3). Our SEGUE-WDMS color cuts are especially designed to identify WDMS systems containing cold white dwarfs (grey shaded region in the bottom panels) and select most WDMS with cold white dwarf $T_{\text {eff,WD }} \leq 20000 \mathrm{~K}$. However, for $T_{\text {eff,WD }} \leq 10000 \mathrm{~K}$ and/or very early spectral types (earlier than $\sim$ M0), the WDMS colors are too close to the main sequence to be selected (lower end of the red line).

### 2.2.1 Expected WDMS ugriz colors

To understand possible biases of the SDSS sample of WDMS and to develop efficient color selection criteria, we calculate ugriz colors for WDMS binaries. Using Pickles (1998) we determine the Johnson UBVRI magnitudes of K - and M dwarfs. Combining this with $U B V R I$ colors for white dwarfs (Bergeron, private communication) and using the empirical color transformation provided by Jordi et al. (2006), we derive ugriz colors for WDMS binaries for a broad range of white dwarf temperatures ( $T_{\text {eff,WD }}=6000-60000 \mathrm{~K}$ ) and secondary spectral types (K0-M6).

Figure 2.1 shows the loci of the calculated WDMS colors in three different color-color dia-
grams. We used the entire range of secondary spectral types and five different effective temperatures of the white dwarf ( $T_{\text {eff,WD }}=40000 \mathrm{~K}$ (blue), 30000 K (cyan), 20000 K (green), 15000 K (magenta), and 10000 K (red)). For late M-dwarfs the WDMS systems are located near the white dwarf region (located at the top and to the left in all the three color-color diagrams) while they are close to the main sequence for early K stars. For hot white dwarfs the binary colors are similar to those of a main sequence star only for the earliest secondary stars (K0) we considered (blue line). Conversely, if the white dwarf is rather cold, the binary colors may be hardly distinguishable from those of main sequence stars even for early M-dwarf secondary stars (red line).

### 2.2.2 The bias of the SDSSI sample

The top panel of Fig. 2.1 also shows the selection criteria presented in (Raymond et al. 2003) and (Silvestri et al. 2006). In each plot, the selected regions are shaded. The selection criteria are apparently based on the idea that a WDMS system has to be red (MS) and blue (WD) at the same time. Consequently, they selected a "blue" region in the $u-g$ versus $g-r$ plot (left panel) and a "red" region in the $r-i$ versus $i-z$ diagram (right panel). A combination of the "blue" and "red" cuts is shown in the $g-r$ versus $r-i$ plot (middle panel). Comparing the color-cuts with our theoretical WDMS colors it becomes obvious that these selection criteria cover only a small fraction of possible WDMS colors. In $u-g$ versus $g-r$ (left) they select mainly systems with hot white dwarfs and/or late type secondaries. While most of the blue and cyan lines are inside the "blue" criterion, large parts of the other lines are outside the cut. This means that most WDMS containing white dwarfs colder than $\sim 20000 \mathrm{~K}$ are not selected. In addition, systems with moderately hot white dwarfs ( $\sim 20000-30000 \mathrm{~K}$ ) and early M-dwarf secondary stars are also not "blue" enough. In contrast, the "red" cuts applied by Silvestri et al. (2006) (shown in the $r-i$ versus $i-z$ plot, right panel of Fig. 2.1) select most of the WDMS containing white dwarfs colder than $\sim 40000 \mathrm{~K}$. Significant parts of the blue and cyan lines are outside the "red" condition. Finally, as the "red" and "blue" criteria have been combined with a logical AND, the target selection used by Silvestri et al. (2006) leads to a sample of WDMS heavily biased towards hot white dwarfs ( $T_{\text {eff,wD }} \gtrsim 15000 \mathrm{~K}$ ) and late type secondary stars (later than $\sim \mathrm{M} 3$ ).

In reality, the SDSS sample of the 749 WDMS systems presented by Silvestri et al. (2006) is somewhat less biased than one would expect according to the color selection. The reason for this is obvious: as stated by Silvestri et al. (2006) many WDMS systems have been targeted as quasar (QSO) candidates. Hence, the part of the WDMS bridge overlapping with the QSO region (yellow in Fig.2.1) is well covered by SDSSI. However, the SDSSI QSO selection algorithm explicitly excludes the color-color space of WDMS containing cold white dwarfs (see Richards et al. 2002, Fig. 7) and hence the strong bias towards hot white dwarfs and late type secondaries remains. Fortunately, Silvestri et al. (2006) finally revised their selection algorithm during 2005 and future SDSS samples of WDMS as that one from Rebassa-Mansergas et al. (2009) are less biased towards hot WDs.

### 2.2.3 WDMS color selection within SEGUE

The Sloan Extension for Galactic Understanding and Exploration (SEGUE) is the part of SDSS II which specifically targets stars in the Milky Way to map the structure and stellar makeup of the Milky Way Galaxy. The main science goal of SEGUE is to constrain how Milky Way formed and evolved. Therefore SEGUE is scanning the sky outside of the North Galactic Cap in a pattern that includes scans that pass through the Galactic plane to uniformly probe the Milky Way at all accessible longitudes and latitudes.

As partners of SEGUE we run a sub-project identifying the missing WDMS population, i.e. those containing cold white dwarfs. We developed special ugriz color-cuts to select those systems on each SEGUE plate-pair ( $\sim 7 \mathrm{deg}^{2}$ ). The bottom panel of Fig. 2.1 shows the SEGUE-WDMS selection criteria as black lines. We use:

$$
\begin{aligned}
& u-g<2.25 \\
& g-r>-19.78(r-i)+11.13 \\
& g-r>-0.2 \\
& g-r<1.2 \\
& i-z>0.5 \text { for } r-i>1.0 \\
& r-i>0.5 \\
& i-z>0.68(r-i)-0.18 \text { for } r-i<=1.0 \\
& r-i<2.0
\end{aligned} \quad 15<g<20 .
$$

The main cuts are in $g-r$ and $r-i$. Clearly, we will only select few systems with hot white dwarfs as significant parts of the blue line are outside our criteria. In addition, WDMS consisting of both cold white dwarfs ( $T_{\text {eff }}$ WD $\lesssim 10.000 \mathrm{~K}$ ) and early type secondaries (earlier than $\sim \mathrm{M} 0$ ) will not be detected, as they are too close to the main sequence (lower part of the red line). However, according to the calculated WDMS colors one clearly expects to identify substantially more WDMS containing cold white dwarfs and early type secondaries, i.e. exactly those systems that are extremely underrepresented in the SDSS I sample.

Our criteria have been optimized by performing extensive tests with data release 4 (DR4). Combining our final color-criteria with the standard clean-photometry flag-setting and requesting the psf-errors to be below 0.2 we find 3713 candidates in DR4. With the footprint area of DR4 ( $6670 \mathrm{deg}^{2}$ ) this gives an average 3.9 candidates per plate pair (covering $7 \mathrm{deg}^{2}$ ). Among these 293 systems were observed spectroscopically and we identify 187 WDMS and 21 WDMS candidate systems which gives an expected success rate of $\sim 64 \%$. The DR4 candidates and targets are shown in Fig. 2.2. Apparently, while the candidates (green) cover the total area we selected in color-color space, those systems with SDSS I spectrum (red) cluster close to the QSO region. This has been expected, as most of them have been selected for spectroscopy as QSO candidates.

Somewhat surprising, 10 of the 187 WDMS we identified during our target selection tests (see Sect.2.2.3) with DR4 have not been published in the corresponding DR4 or DR5 WDMS or white dwarf catalogues (Silvestri et al. 2006, 2007; Eisenstein et al. 2006). This incompleteness inspired us to apply our color-selection to DR5 without any flag restrictions to determine the definite number of WDMS inside our criteria using DR5. We find 437 systems that have been


Figure 2.2: WDMS target selection tests with data release 4 (DR4). As in Fig. 2.1 stars and quasars are in grey and yellow respectively. Applying our color selection to DR4 we get 3247 candidates (red) that cover the cold white dwarf region of the WDMS bridge. 283 of these systems have been selected for spectroscopy (green) among these we find 201 WDMS. Most of the spectroscopic targets (green) are close to the QSO region because they were selected as QSO candidates. This further demonstrates the bias of the SDSS I sample.
observed spectroscopically. Among these are 276 WDMS and 36 WDMS candidates. Of the 276 WDMS 45 have not been published so far. In Table 2.1 we provide the ugriz colors, plate and fiber numbers as well as times of observations of these 45 WDMS. Apparently, the published SDSS catalogues of WDMS are not complete and probably about $\sim 20 \%$ WDMS are missing. Obviously, a separate analysis of the WDMS content of DR6 (Adelman-McCarthy et al. 2007) and DR7 (Abazajian et al. 2009) seems to be a worthwhile exercise and part has been presented in Rebassa-Mansergas et al. (2009) (Rebassa-Mansergas et al 2010, in preparation).

### 2.2.4 Comparison of selection criteria

We have applied our selection criterium to the expected ugriz colors of WDMS binaries for spectral types in the range K6 - M6 and for effective temperatures of the white dwarf in the range $10^{3}-10^{5} \mathrm{~K}$ to see what area of the effective temperature-spectral type plane we expect to cover. We have also applied the selection criterium defined by Silvestri et al. (2006), and also their revised version, in the same ranges of spectral type and effective temperatures. In Fig. 2.3 we show the coverage in the effective temperature-spectral type plane of our selection criterium (left panel), that one from Silvestri et al. (2006) (middle) and their revised criterium (right).

We cover a broad range in the effective temperature of the white dwarf, $6000-10^{5} \mathrm{~K}$ and in the spectral type of the secondary star, M0 to M6. While we cover earlier spectral types than M2, this are not covered by Silvestri et al. (2006) in either criteria. We expect to detect cold white dwarfs ( $<15000 \mathrm{~K}$ ), while they would only be detected by Silvestri et al. (2006) in case they contain later spectral type secondaries than M6. Although in their revised criterium they do cover cold white dwarf temperatures for earlier spectral types than M6, the spectral type is still limited to later spectral types than M2.


Figure 2.3: Coverage in the effective temperature-spectral type plane of our selection criterium (left), that one from Silvestri et al. (2006) (middle) and their revised criterium (right).


Figure 2.4: The position of the SEGUE WDMS binaries in ugriz color-space. Apparently, in contrast to the spectroscopic DR4 sample shown as green dots in in Fig. 2.2, the SEGUE WDMS sample includes significantly more WDMS binaries close to the main sequence, i.e. systems containing cold white dwarfs.

### 2.3 The SEGUE white dwarf/main sequence binary sample

In October 2005 SEGUE incorporated the color selection given in Sect. 2.2.3 with the goal of targeting on average 5 WDMS candidates and up to 10 WDMS per plate-pair. Until the end of SEGUE in mid-2008 116 plate-pairs and 8 single SEGUE-plates with WDMS target selection according to our criteria have been observed. In addition to the color criteria we requested clean photometry ${ }^{2}$ for the selection of our targets. According to DR7 9531 systems fulfilled the target selection criteria. However, one should note that 7619 of these candidates are on 12 plates that have been oriented towards the galactic plane ${ }^{3}$, where reddening is very high, and the success rate of our selection criterium should be low, since we did not correct for reddening. Of the

[^5]9531 available candidates 431 stars have been observed spectroscopically and among these we identify 277 WDMS and 24 WDMS candidates. Two WDMS (SDSSJ135643.56-085808.9 and SDSSJ135930.96-101029.7) have been found on plate 2716, spectroscopic plate that has not been published via DR7. Although the spectra of these two systems is not available via DR7 we had access to it and we made use of them for the completeness analisys ${ }^{4}$. The WDMS 'candidate' category refers mostly to spectra containing a main sequence star with a strong blue excess which cannot clearly be identified as originating from a white dwarf. Dividing the number of spectra taken by the number of identified WDMS and WDMS candidates results in a overall success rate of $64 \%$. Table 2.2 lists the number of candidates, the spectra taken according to our selection criteria, teh number of identified WDMS binaries, and the number of systems for which spectra were taken but are outside the selection criteria, the success rate, and galactic coordinates of the center of the plate, the space density, the reddening and the error on the density, for the 116 plate-pairs and the 8 single plates with WDMS target selection that have been observed in SEGUE. Table 2.3 lists on our WDMS and candidates systems, the corresponding plate numbers, date of the observation, their ugriz magnitudes and their errors. An excerpt of Tables 2.3 and 2.2 are now given while the full tables are available in the appendix.

Fig. 2.4 shows the positions of our SEGUE WDMS in color-color space. The background in the three panels are again single stars (grey) and quasars (yellow) from DR4. Our selection criteria have been designed for the measured ugriz magnitudes, i.e. not reddening corrected. However, 14 SEGUE plate pairs and 2 single plates i.e. those with plate numbers $<2377$ that belong to target selection version 3.3, accidently used reddening corrected magnitudes for the selection of WDMS candidates. Therefore 31 WDMS of the 301 identified WDMS or WDMS candidate systems are located slightly outside our criteria.

Fig. 2.5 shows the positions of our WDMS candidates in galactic and equatorial coordinates. One of the big advantages of SEGUE is that it covers a wide range of galactic latitudes and, as we will see later, this gives an idea of the spatial distribution of the galactic population of WDMS. Table 2.3 lists the 301 WDMS and WDMS candidate systems, the corresponding plate as well as fiber numbers, the dates of observation (MJD) and the measured ugriz magnitudes.

### 2.4 Stellar parameters

We use the same method, templates, and spectral models as Rebassa-Mansergas et al. (2007) to determine the stellar parameters of the SEGUE-WDMS binaries. In brief, the method can be described as follows: we fit the WDMS spectrum using grids of observed M-dwarf and white dwarf template spectra. Our white dwarf library consists of 488 high S/N DA from DR6 (Adelman-McCarthy et al. 2007) covering the entire parameter space of the effective temperature and the gravity and 222 DB spectra taken from Eisenstein et al. (2006). The M-dwarf templates are based on several hundred M-dwarf spectra also taken from DR6. These spectra have been

[^6]Table 2.1: During our target selection tests we identified 45 so far unpublished WDMS binaries that are in DR5 and fullfill our target selection criteria.

|  |  |  |  |  |  |  |  |  |  | 1ber |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 20.186 |  |  |  |  |  |  |  |
| 05 | 0524.40 | 232411.6 |  |  | 17.225 | 16 |  |  |  | 17 |
|  |  |  | 0.08 |  |  |  |  |  |  | 220 |
| SDSSJ093236.83+053026.6 | 93236.83 |  | 19.822 | 18.320 |  | 16.414 |  | 52644 | 992 | 175 |
| SDSSJ095250.11+324328.8 | 5250.11 | +32 4328.8 | 20.810 | 19.492 | - | 17.541 | 6 | 53 | 945 | 20 |
| SSJ095250.98+055636.9 | 95250.98 | +05 5636.9 | 20.339 | 18.948 | 17 | 17. | 16.663 | 527 | 994 | 117 |
| J100255.48+424320.9 | 0255.48 | 424320.9 | 0.068 | 19.51 | 18.8 | 17. | 16.755 | 52672 | 217 | 538 |
| SSSJ103152.46+362832.8 | 2. |  | 19.648 | 18.974 | 18.118 | 17.039 | 55 |  | 73 | 65 |
| . 2 | 104142.56 | 391900.2 | 0.121 | 19.758 |  |  |  |  |  |  |
| SSJ104459.32+360554.7 | 4459.32 | 36 0554.7 | 8.61 | 17.870 | 17.160 | 15 | 999 | 53463 | 2090 | 73 |
| SSJ105853.18+390018.2 | 05853.18 | +39 0018.2 | 0.265 | 19.48 | 18.61 | 17 | 16.873 | 53 | 988 | 80 |
| SSJ110736.88+612232.8 | 0736.88 | 232.8 | 20.091 | 38 | 17.669 | 仡 | 06 | 52286 | 774 | 55 |
| . 8 | 3833.13 |  | 20.315 | 19.468 | 18.669 |  |  |  | 12 | 62 |
| J114046.44+331843.0 |  | 331843. | 0.019 | 18.988 |  |  | 16.013 |  | 097 | 10 |
| $114509.77+381329.2$ | 14509.77 | +38 | 7.64 | 16 | 16 | 15.068 | 6 |  | 1997 | 91 |
| SSJ115031.25+365416.1 | 15031.25 | +365416.1 | 8.45 | 18.301 | 17.88 | 17.079 | 16.553 | 53 | 035 | 419 |
| J120455.42+133715.7 | 2455.42 | 133715.7 | 19.959 | 19.540 | 19.248 | 18.268 | 3 | 53467 | 1764 | 39 |
| SSSJ121010.13+334722.9 | 21010.13 | +33 4722.9 | 8.42 | 7.26 | 16.478 | 25 |  | 53498 | 2089 | 02 |
| SSJ121356.86+363531.0 | 1256.8 | 363531.0 | 8.18 | 17.786 |  | 16.37 | 15.982 |  | 105 | 546 |
| 8.7 | 1928.05 | 161158.7 | . 78 | 18.123 | 17.723 | 16 | 15.845 |  |  | 569 |
| SSJ122544.63+381605.3 | 22544.63 | +38 1605.3 | 20.734 | 19.824 | 19.172 | 18.133 | 500 | 53466 |  | 277 |
| SSJ122604.78+375827.5 | 22604.78 | 375827.5 | 9.54 | 18.372 | 17.315 | 15.875 | 14.982 | 53466 | 1992 | 231 |
| SSJ122634.97+322020.8 | 2634.97 | 322020.8 | , | 9.48 | 19 | 18.00 | 225 | 53472 |  | 315 |
| $3.80+380858.6$ | 3223.8 | 380858 |  |  |  |  | 6 |  |  | 76 |
| $3.64+144955.5$ | 0403.64 | 55.5 | 20.566 | 20.18 | 20.069 | 19.372 | 9 | 53498 | 771 | 632 |
| J134624.89+021734.2 | 34624.89 | -02 1734.2 | . 59 | 18.36 | 17.423 | 16.153 | 15.838 | 52026 | 530 | 79 |
| SSJ134901.85+020136.5 | 34901.85 | 020136.5 | 0.402 | 8.58 | 17.5 | 16.92 | 16.538 | 52026 | 530 | 00 |
| SSJ140816.84+331448.4 | 40816.84 | 331448 | 0.247 | 19. | 18.541 |  | 8 | 53471 | 839 | 253 |
| SDSSJ140949.55+433911.4 | 09 | 43 | 0.289 | 19.14 | 18 | 17.089 | 16.404 | 53115 | 46 | 20 |
| J143649.61+323734.1 | 3649.61 | +323734.1 | . 489 | . 060 | 16.256 | 15.608 |  |  | 841 | 78 |
| J151714.96+423924.7 | 51714.96 | 423924.7 | 7.85 | 7.477 | 16.843 | 15.904 | 15.304 | 53433 | 1678 | 440 |
| SSJ152116.97+420159.2 | 152116.97 | 420159.2 | 19.28 | 0 | 18.863 | 18.264 | 9 | 534 | 1678 | 63 |
| +430528.9 | 23 | 528.9 |  |  |  |  | 6 | 53433 | 1678 | 616 |
| J152517.89+362945.2 | 52517.89 | +3629 45.2 | . 956 | . 007 | 17.204 | 06 | 15.361 | 53470 | 1400 | 135 |
| SJ154605.27+370854.3 | 54605.27 | +370854.3 | 20.487 | 095 | 18.064 | . 002 |  | 52875 | 1416 | 58 |
| SSJ155022.11+323548.5 | 55022.1 | 323548.5 | 8.77 | 17.790 | 16.74 | 15.525 |  | 52825 | 1404 | 18 |
| SSJ160136.70+050527.9 | 160136.70 | +0505 27.9 | 8.246 | 18.30 | 17.896 |  | 16.99 | 53494 | 837 | 431 |
| SDSSJ160645.02+284725.9 | 160645.02 | +28 4725.9 | 19.206 | .845 | 18.72 | . 03 | 17.417 | 534 | 1578 | 104 |
| SSSJ160824.57+285524.9 | 160824.57 | +2855 24.9 | 20.395 | 19.753 | 19.352 | 18.400 | 17.730 | 349 | 1578 | 72 |
| DSSJ160915.97+273559.4 | 160915.97 | +27 3559.4 | 18.466 | 18.023 | 17.643 | 16.695 | 16.023 | 349 | 1577 | 252 |
| SDSSJ161505.51+235746.3 | 161505.51 | +23 5746.3 | 19.356 | 18.569 | 18.010 | 17.079 | 16.456 | 53520 | 657 | 515 |
| SDSSJ162051.70+343815.3 | 162051.70 | +34 3815.3 | 19.964 | 18.491 | 17.457 | 16.410 | 15.840 | 52522 | 057 | 195 |
| DSSJ163020.19+305254.5 | 163020.19 | +30 5254.5 | 20.634 | 19.384 | 18.227 | 17.021 | 16.345 | 53463 | 685 | 496 |
| DSSJ164131.77+212727.2 | 164131.77 | +21 2727.2 | 20.419 | 18.862 | 1 | 仡 614 |  | 53149 | 570 | 178 |
| DSSJ204117.49-062847.0 | 204117.49 | -0628 47.0 | 19.325 | 19.059 | 18.47 | 17.8 | 7. | 521 | 63 | 47 |

Table 2.2: Number of candidate, spectra taken according to our selection criteria, number of identified WDMS binaries, number of systems for which spectra were taken but are outside the selection criteria, success rate, galactic coordinates, space density, reddening and error on the density, for the 116 plate-pairs and 8 single plates with WDMS target selection that have been observed in SEGUE. See appendix for a complete version of the table.


Table 2.3: Plate number, Fiber number, MJD of the observation, and ugriz colors of the 301 WDMS and WDMS candidate systems identified with SEGUE.

| System | Plate | Fiber | MJD | u | $\sigma_{u}$ | g | $\sigma_{g}$ | r | $\sigma_{r}$ | i | $\sigma_{i}$ | z | $\sigma_{z}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SDSSJ000250.64-045041.6 | 2630 | 439 | 54327 | 19.846 | 0.042 | 19.728 | 0.021 | 19.464 | 0.018 | 18.569 | 0.014 | 17.903 | 0.022 |
| SDSSJ0013000.74+385205.4 | 2336 | 7 | 53712 | 20.128 | 0.039 | 19.030 | 0.017 | 17.935 | 0.011 | 17.203 | 0.012 | 16.762 | 0.016 |
| SDSSJ014143.68-093811.7 | 2865 | 170 | 5449 | 19.663 | 0.037 | 19.377 | 0.022 | 18.931 | 0.015 | 18.012 | 0.019 | 17.435 | 0.022 |
| SDSSJ023438.48+244535.6 | 2399 | 75 | 53764 | 21.155 | 0.108 | 20.012 | 0.021 | 18.851 | 0.016 | 18.040 | 0.014 | 17.524 | 0.017 |
| SDSSJ025555.87+352830.2 | 2378 | 538 | 53759 | 18.370 | 0.023 | 17.559 | 0.014 | 16.519 | 0.009 | 15.550 | 0.007 | 14.992 | 0.013 |
| SDSSJ030247.65+372125.9 | 2443 | 185 | 54082 | 20.634 | 0.071 | 19.589 | 0.014 | 18.444 | 0.012 | 17.749 | 0.012 | 17.367 | 0.018 |
| SDSSJ030716.44+384822.8 | 2441 | 564 | 54065 | 20.642 | 0.075 | 19.039 | 0.126 | 17.861 | 0.316 | 16.698 | 0.201 | 16.056 | 0.122 |
| SDSSJ030956.31+411049.2 | 2397 | 255 | 53763 | 24.598 | 1.009 | 18.405 | 0.030 | 16.976 | 0.014 | 15.777 | 0.011 | 14.979 | 0.009 |
| SDSSJ032140.00+415307.5 | 2417 | 633 | 53766 | 21.078 | 0.135 | 20.582 | 0.076 | 19.490 | 0.024 | 18.345 | 0.012 | 17.674 | 0.018 |
| SDSSJ042053.72+064922.4 | 2826 | 526 | 54389 | 20.922 | 0.071 | 19.755 | 0.019 | 18.055 | 0.012 | 17.175 | 0.011 | 16.231 | 0.013 |
| SDSSJ070322.17+664908.0 | 2337 | 419 | 53740 | 19.973 | 0.044 | 18.642 | 0.019 | 17.512 | 0.011 | 16.366 | 0.015 | 15.712 | 0.020 |
| SDSSJ070628.57+383650.2 | 2943 | 204 | 54502 | 20.217 | 0.049 | 19.412 | 0.016 | 18.507 | 0.011 | 17.554 | 0.015 | 16.984 | 0.016 |

## Galactic coordinates



Equatorial coordinates


Figure 2.5: Position of the plate-centers (black) and identified WDMS binaries (red) in galactic and equatorial coordinates. In contrast to SDSSI and the Legacy survey, SEGUE observed a large number of plates at low galactic latitudes.
classified using the templates of Beuermann et al. (1998). For each spectral subtype the best $10-20$ spectra have been averaged and scaled in flux to match the surface brightness at $7500 \AA$.

In a first step the best match of the SDSS WDMS spectrum to a WD and MS combination of the just described templates is determined. We used an evolutionary strategy based on a weighted $\chi^{2}$ to find the best solution. This allows to determine the spectral type of the secondary and using the spectral type-radius relation from Rebassa-Mansergas et al. (2007) and the apparent
magnitude of the scaled template we derive a first estimate of the distance to the M star, $d_{\text {sec }}$. We subtract the best-fitted M-dwarf template spectrum, and determine the parameters of the white dwarf via $\chi^{2}$ minimization in a $\log g-T_{\text {eff }}$ grid of DA model spectra from Koester (2008), based on the atmosphere code described in Finley et al. (1997), to the Balmer lines of the remaining WD. We use $\mathrm{H} \beta-\mathrm{H} \epsilon$, and avoid using $\mathrm{H} \alpha$ since it might contain some residual emission from the red dwarf (see left panel of Fig. 2.6). As we have seen in chapter 1 the solution is bivalued, giving two solutions, a 'hot' and a 'cold' solution, shown in the right upper panel of Fig. 2.6. In order to discern between these two solutions, we fit template DA to the continuum from 3850-7150 $\AA$, avoiding the reddest part of the white dwarf since it might contain some residual flux from the M star. With the $\log g-T_{\text {eff }}$ combination and using an updated version of Bergeron et al. (1995) we estimated the mass and the radius of the white dwarf. Combining with the flux scaling factor this gives us a second estimate of the distance, $d_{\mathrm{wd}}$, through the relation between the observed flux ( $F_{o b s}$ ) and the astrophysical flux at the surface of the WD as given by the model $\left(F_{e m}\right), F_{o b s}=F_{e m}\left(R_{\mathrm{wd}} / d_{\mathrm{wd}}\right)^{2}$.

In some cases it is not possible to distinguish between the 'hot' and the 'cold' solution using the spectrum plus lines. However, as the hot solution predicts significantly more UV flux than the cold solution, we can identify the correct fit by comparing the predicted UV flux with NUV and FUV magnitudes measured by GALEX. An example is given in Fig. 2.6 and 2.7. While the decomposition of the spectrum of SDSSJ134008.04+082248.4 does not provide a unique solution, comparing the predicted UV fluxes with GALEX data clearly favors the cold solution. Among the 301 systems identified as WDMS or candidates we find that 230 systems have GALEX counterparts withing a 0.05 arc minutes radius search.

We found 277 clear WDMS and 24 candidates that have a dM star and some excess in the blue. Among the WDMS 193 contain DAs, there are 14 systems where the DA nature is a bit dobious and we labelled as DA:/dM and for which we decided not to give stellar parameters for the white dwarf, $15 \mathrm{DB} / \mathrm{dM}, 20 \mathrm{DC} / \mathrm{dM}$, and $35 \mathrm{WD} / \mathrm{dM}$. Table 2.4 lists the obtained stellar parameters of the 193 SEGUE WDMS binaries containing DA white dwarfs and the secondary star spectral type for all the 277 clear WDMS binaries and 24 candidates (abridged version is shown in Table 2.4 a full table is available in the appendix). We also identified 2 new CVs (Szkody et al. 2009) and one low accretion rate magnetic binary (Schwope et al. 2009). The most likely scenario for the later systems is that accrete they accrete matter from the stellar wind of the secondary star. These type of binaries are thought to be precursors of magnetic CVs (Webbink \& Wickramasinghe 2005; Schmidt et al. 2005; Vogel et al. 2007).

### 2.5 Distributions

In this section we briefly discuss the distributions of the obtained parameters and compare our results with those obtained by Silvestri et al. (2006), and Eisenstein et al. (2006). While our decomposition method has shown to work quite well in most cases, in some cases the obtained

[^7]

Figure 2.6: Top panel: two component fit to SDSSJ134008.04+082248.4 and to SDSSJ094402.18+614307.9. The top panel shows the WDMS spectrum (black line) and the white dwarf and the M-dwarf templates (dotted lines), while the lower panel shows the residuals to the fit. Bottom panels: spectral fit to the white dwarf in SDSSJ134008.04+082248.4 and in SDSSJ094402.18+614307.9 obtained by subtracting the best-fit M-dwarf template from the SDSS spectrum. Top left panels: normalized $\mathrm{H} \beta$ to $\mathrm{H} \epsilon$ line profiles (top to bottom, gray lines) along with the best-fit white dwarf model (black lines). Top right panels: 3,5 , and $10 \sigma \chi^{2}$ contour plots in the $T_{\text {eff }}-\log g$ plane. The black contours refer to the best line profile fit, the red contours to the fit of the whole spectrum. The solid line indicates the location of maximum $\mathrm{H} \beta$ equivalent width in the $T_{\text {eff }}-\log g$ plane, dividing it into "hot" and "cold" solutions. The best-fit parameters of the "hot" and "cold" normalized line profile solutions and of the fit to the $3850-7150 \AA$ range are indicated by red and black dots, respectively. Bottom panels: the white dwarf spectrum and associated flux errors (gray lines) along with the best-fit white dwarf model (black lines) to the $3850-7150 \AA$ wavelength range (top) and the residuals of the fit (gray line, bottom). Apparently, the fit to the continuum for SDSSJ134008.04+082248.4 does not indicate whether the "hot" or the "cold" solution should be prefered. In such cases GALEX data was helpful identifying the best fit (see text and Fig.2.7).


Figure 2.7: Predicted flux of the "hot" (red) and "cold" (blue) solution for SDSSJ134008.04+082248.4 and SDSSJ094402.18+614307.9 at optial and UV wavelengths. NUV and FUV fluxes provided by GALEX clearly show that the "cold" solution is the correct one.
parameters are relatively uncertain. To avoid incorporating large numbers of uncertain values we not only show distributions of all systems but also those including only systems having uncertainties less than $25 \%$. Fig. 2.8 shows the distributions of white dwarf temperatures, masses, and secondary spectral types for the whole sample (solid lines) and for systems with uncertainties lower than $25 \%$ and effective temperature higher then 12000 K (dashed lines).

Table 2.4: Stellar parameters of the 277 WDMS systems identified with SEGUE and for the 24 candidates. For the 84 binaries containing a DB, DC, or unclear white dwarf spectral type, only some parameters obtained for the secondary star are given, this is also true for the candidates.

| System | Type | $T_{\mathrm{eff}}$ | $\sigma_{T_{\mathrm{eff}}}$ | $\log g$ | $\sigma_{\log g}$ | $M_{\mathrm{wd}}$ | $\sigma_{M_{\mathrm{wd}}}$ | $d_{\mathrm{wd}}$ | $\sigma_{d_{\mathrm{wd}}}$ | Sp2 | $d_{\mathrm{sec}}$ | $\sigma_{d_{\mathrm{sec}}}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SDSSJ000250.64-045041.6 | DB/dM |  |  |  |  |  |  |  |  | 3 | 797 | 157 |
| SDSSJ000356.93-050332.7 | DA/dM | 17106 | 438 | 8.07 | 0.10 | 0.66 | 0.06 | 285 | 19 | 4 | 386 | 114 |
| SDSSJ000453.93+265420.4 | DA/dM | 18974 | 1594 | 7.97 | 0.33 | 0.60 | 0.20 | 683 | 142 | 3 | 1037 | 204 |
| SDSSJ000504.91+243409.6 | DA/dM | 13127 | 2160 | 8.16 | 0.34 | 0.71 | 0.22 | 304 | 70 | 4 | 350 | 103 |
| SDSSJ000531.09-054343.2 | DA/dM | 13127 | 657 | 7.91 | 0.14 | 0.56 | 0.08 | 129 | 11 | 4 | 167 | 49 |
| SDSSJ000559.87-054416.0 | DA/dM | 31128 | 921 | 7.89 | 0.21 | 0.59 | 0.12 | 692 | 99 | 2 | 553 | 132 |
| SDSSJ000651.91+284647.1 | DA/dM | 12976 | 688 | 7.83 | 0.21 | 0.51 | 0.12 | 343 | 44 | 3 | 420 | 83 |
| SDSSJ000829.92+273340.5 | DA/dM | 15782 | 1481 | 7.73 | 0.37 | 0.47 | 0.20 | 615 | 131 | 2 | 656 | 156 |
| SDSSJ000935.50+243251.2 | DA/dM | 14393 | 4221 | 8.58 | 0.68 | 0.98 | 0.32 | 347 | 162 | 2 | 479 | 114 |
| SDSSJ003804.41+083416.9 | DA/dM | 8673 | 255 | 7.73 | 0.59 | 0.45 | 0.35 | 216 | 69 | 3 | 223 | 44 |
| SDSSJ010341.59+003132.6 | DA/dM | 21535 | 1234 | 7.76 | 0.21 | 0.50 | 0.11 | 849 | 113 | 2 | 1159 | 276 |
| SDSSJ010448.50-010516.7 | cand |  |  |  |  |  |  |  |  | 3 | 339 | 67 |
| SDSSJ010704.58+005907.9 | cand |  |  |  |  |  |  |  |  | 1 | 1063 | 208 |
| SDSSJ011123.90+000935.2 | DA/dM | 15071 | 547 | 7.72 | 0.13 | 0.47 | 0.06 | 458 | 36 | 2 | 654 | 156 |
| SDSSJ011932.38-090219.1 | DA/dM | 15601 | 1500 | 8.44 | 0.35 | 0.89 | 0.20 | 497 | 126 | 2 | 629 | 150 |
| SDSSJ013000.74+385205.4 | DA:/dM |  |  |  |  |  |  |  |  | 1 | 805 | 158 |
| SDSSJ014143.68-093811.7 | DC/dM |  |  |  |  |  |  |  |  | 3 | 642 | 126 |
| SDSSJ014147.33-094200.3 | cand |  |  |  |  |  |  |  |  | 3 | 490 | 96 |
| SDSSJ014232.59-083528.4 | DA/dM | 9187 | 148 | 8.77 | 0.18 | 1.08 | 0.10 | 113 | 17 | 3 | 428 | 84 |
| SDSSJ020351.29+004025.0 | DA/dM | 10918 | 589 | 7.98 | 0.45 | 0.59 | 0.28 | 420 | 115 | 3 | 501 | 99 |
| SDSSJ021145.57+071831.1 | DA/dM | 19193 | 1301 | 8.09 | 0.26 | 0.67 | 0.16 | 700 | 123 | 3 | 758 | 149 |
| SDSSJ023438.48+244535.6 | WD/dM |  |  |  |  |  |  |  |  | 1 | 1141 | 223 |

### 2.5.1 White dwarf temperatures

The distribution of white dwarf effective temperature is shown in the top left panel of Fig. 2.8. The measured white dwarf temperatures are less accurate if the white dwarf is very cool. Therefore several of the oldest systems have errors exceeding the $25 \%$ criterion (dashed histogram in Fig.2.8). As expected, our selection criteria select mostly cold white dwarfs and our distribution peaks roughly at 10000 K while the distribution published by Silvestri et al. (2006) has a broader peak at a higher temperature, 17500 K . The difference between the two distributions is straight forward to understand if one takes into account the different selection algorithms applied (see Sect.2.2.3).

A detailed comparison with previously published samples is shown in Fig.2.9. The upper left panel compares the white dwarf temperature in our sample with the single DA white dwarfs listed by Eisenstein et al. (2006). We selected from their Table $11{ }^{6}$ systems flagged as 1 in their autofit quality flag and removed double entries and systems with companions. Both distributions are normalized to facilitate comparison. The solid line represents the effective temperature of the WDs in our SEGUE WDMS sample while Eisenstein's distribution of single white dwarfs

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Figure 2.8: The distributions of white dwarf temperatures (upper left), $\log g$ (upper right), secondary star spectral types (lower left) and white dwarf masses (lower right). In all cases except the secondary spectral types we plot only the parameters of WDMS containing DA white dwarfs (solid lines) and the distributions of the primary's parameters for systems with $T_{\text {eff }}<12000 \mathrm{~K}$ and with relative errors smaller than $25 \%$ (dashed lines). In general, the white dwarf temperature distribution peaks at $\sim 10000 \mathrm{~K}$ i.e. at significantly lower temperatures than in previously published WDMS samples (e.g. Silvestri et al. 2006) but looks quite similar to those of single white dwarfs identified with SDSS (Eisenstein et al. 2006). The distributions of $\log g$ and the white dwarf mass are broader than those of single stars and the expected peaks at $M_{\mathrm{wd}}=0.6 \mathrm{M}_{\odot}$ and $\log g \sim 8$ are less pronounced. Finally, the distribution of spectral types in the bottom left panel is broader than the one published earlier for WDMS from SDSS I (Silvestri et al. 2006) and peaks at $M 3$ instead of M4. Comparing our distribution with those of single low mass stars (West et al. 2004) we find general agreement for systems later than M3 but our sample contains less systems with M0 - M2 companions.
is drawn with a dashed line. Apparently, the two distributions are quite similar, the peak at low temperatures is only slightly less pronounced for the white dwarfs in the SEGUE binaries. The single star distribution also has a larger tail extending to very high temperatures which we don't see in the SEGUE WDMS sample as most systems containing hot white dwarfs are excluded by our color cuts (see Sect. 2.2.3).

Silvestri et al. (2006) studied a sample of 747 WDMS and estimated the temperature of the


Figure 2.9: Comparison of the SEGUE-WDMS white dwarf temperatures (solid lines) with those of single SDSS white dwarfs (Eisenstein et al. 2006) (left, dashed lines) and with the sample from Silvestri et al. (2006) (right, dashed lines). The upper panels show normalized distributions to the maximum. The bottom panels show the cumulative distribution functions. While the distribution of the SEGUE WDMS white dwarf temperatures is very similar to the distribution obtained by Eisenstein et al. for single white dwarfs, the previous sample of SDSS WDMS binaries contains significantly less systems with cold white dwarfs.

DAs in their sample in a similar way (but see Rebassa-Mansergas et al. 2007, for a more detailed comparison of the applied methods). The temperature distribution of their sample peaks at 20000 K , while ours peaks around 10000 K (see Fig. 2.9 left panel). While different to the SEGUE and the single star sample at low temperatures ( $T_{\text {eff, WD }} \lesssim 20000 \mathrm{~K}$ ), the sample presented by Silvestri et al. resembles the single star distribution at higher temperatures.

Another way of representing and comparing the data is using cumulative distributions. In the bottom panels of Fig. 2.9 we show the cumulative distributions of our sample (solid line) and those from Eisenstein et al. (2006) (left panel) and from Silvestri et al. (2006) (right panel) (both plotted with dashed lines). To compare in a quantitative way the $T_{\text {eff }}$ of the different datasets we made use of the Kolmogorov-Smirnov statistics (KS-test) ${ }^{7}$. The KS-test for systems between

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Figure 2.10: White dwarf masses versus $T_{\text {eff }}$ for the sample of 193 WDMS that contain DAs.

7500 K and 50000 K gives a maximum deviation for the cumulative functions of 0.12 between this study and Eisenstein et al. (2006) at a significance level of $2 \sigma$ and of 0.21 between our sample and the one from Silvestri et al. (2006) at a significance level of $4 \sigma$. If we select systems with higher temperatures than 10000 K , then the KS-test gives a maximum distance of 0.07 in the cumulative distributions between this study and Eisenstein et al. (2006) and a significance of $39 \%$. While the result between our sample and the one from Silvestri et al. (2006) is 0.19 and $3 \sigma$ for the distance and for the significance level respectively.

The above result clearly shows that our selection criteria works as expected and we reached one of our main goals: the SEGUE WDMS sample is significantly less biased with respect to white dwarf temperatures (i.e. to the age of the systems) than previous samples of SDSS-WDMS.

### 2.5.2 White dwarf masses and $\log g$

The distribution of the masses of the 193 DA white dwarfs primaries in our sample is given in the lower right panel of Fig. 2.8. Compared to the recent analysis of single SDSS white dwarfs by De Gennaro et al. (2008) the mass distribution of the white dwarfs in the SEGUE WDMS is

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Figure 2.11: White dwarf $\log g$ versus $T_{\text {eff }}$ for the sample of 193 WDMS that contain DAs (open circles) and that one of Eisenstein et al. (2006) (dots).
significantly broader, i.e. the peak at $M_{\mathrm{wd}} \sim 0.6 \mathrm{M}_{\odot}$ is less pronounced. This difference is partly explained by the fainter limiting magnitude in our sample that implies a larger uncertainty of the white dwarf masses in our sample which directly transform into a broader distribution.

The mean mass of the entire sample is $M_{\mathrm{wd}}=0.69$ and has a standard deviation of 0.23 $\mathrm{M}_{\odot}$, while the peak is at a significantly lower mass, $0.59 \mathrm{M}_{\odot}$ with a FWHM of $0.47 \mathrm{M}_{\odot}$ (see Fig. 2.12). Liebert et al. (2005) draw the $M_{\mathrm{wd}}$ distribution for a sample of 348 white dwarfs, covering a temperature range from 100000 K to 7000 K . They find a mean of $0.603 \pm 0.134 \mathrm{M}_{\odot}$ and a peak at $0.572 \mathrm{M}_{\odot}$, with a FWHM of $0.188 \mathrm{M}_{\odot}$. Our values differ significantly from these, being in all cases superior. The high mass tail of our $M_{\text {wd }}$ distribution is dominated by WD with low temperatures (see Fig. 2.10). If we select systems with $T_{\text {eff }}$ larger than 12000 K the mean of the 135 left systems is $0.62 \pm 0.19 \mathrm{M}_{\odot}$, the peak shifts to $0.54 \mathrm{M}_{\odot}$ and the FWHM is then 0.35 $\mathrm{M}_{\odot}$ (see Fig. 2.12), a bit narrower but still broader than for single white dwarfs. The tail towards massive white dwarfs is then less significant. And if we also restrict to systems with uncertainties in the white dwarf parameters of less than $25 \%$ (see Fig. 2.8) then the mean based on 55 systems is 0.61 and it's standard deviation is $0.12 \mathrm{M}_{\odot}$, value closer to that found by Liebert et al. (2005).

In Fig. 2.11 we compare the $\log g$ versus effective temperature distribution with that one of field white dwards from Eisenstein et al. (2006). Eisenstein et al. (2006) cut their distribution at $\log g=9$ so for higher gravities we can not compare our results. Still we can see that for lower effective temperatures of teh white dwarf the gravity seems to be correlated with it. For white dwarfs with effective temperature higher than around 12500 K the gravity becomes independent


Figure 2.12: White dwarf masses for the entire sample (left) and for systems with $T_{\text {eff }}<12000 \mathrm{~K}$. Gaussian fits are over-plotted with dashed lines and each plot contains information about the position of the peak, the FWHM, the mean mass and the standard deviation.
as expected. White dwarfs with temperatures between 25000 K and 12500 K in our sample are distributed as field white dwarfs. Hotter systems than 25500 K seem to have high masses again. This might be a bias introdued by our selection criteria and further investigation should be carried out.

In Fig. 2.13 we compare the obtained values of $\log g$ of the SEGUE WDMS white dwarfs with the single white dwarf distribution of Eisenstein et al. (2006), shown in the left panels, and the WDMS sample of Silvestri et al. (2006) in the right panels. In the upper panels we show the distributions normalized to the maximum and in the bottom panels the cumulative distributions. We draw our distributions with solid lines and with dashed lines the other two samples. In general, the three distributions are quite similar the only significant difference being the tail towards high values of $\log g$ that we find but which is missing in the other two distributions.

The KS statistics between our distribution and the one of Eisenstein et al. (2006) gives 0.1 for the maximum distance between the cumulative distributions and a significance level of $2 \%$. Between ours and the one from Silvestri et al. (2006) the KS statistics gives 0.3 and almost 0 \% for the significance level. We computed the KS statistic again using only those systems with $T_{\text {eff }}>12000 \mathrm{~K}$ and with $7<\log g<9$. It gives a maximum distance between both cumulative distribution functions of 0.08 and a $27 \%$ significance level when comparing with Eisenstein et al.


Figure 2.13: Comparing $\log g$ of the SEGUE-WDMS white dwarfs with those of single SDSS white dwarfs (Eisenstein et al. 2006) and previous WDMS samples (Silvestri et al. 2006). The SEGUE WDMS distribution looks similar to both distribution but is slightly broader and contains more high gravity white dwarfs.
(2006), and 0.54 and almost $0 \%$ significance level when comparing with Silvestri et al. (2006). We conclude that the observed long tail at high masses is due to systems with WDs with low temperatures, and according to Kepler et al. (2007) one should not trust the inferred masses for those systems.

### 2.5.3 Secondary star spectral types

The spectral type distribution of the secondary stars of our WDMS binary sample is shown in the lower right panel of Fig. 2.8. The spectral type distribution covers the range from M0 to M6. The number of systems at a given spectral type increases until spectral type M3, where it reaches a maximum, and then declines towards later spectral types, being rather symmetric. There are no WDMS binaries containing secondaries with earlier spectral type than M0 nor later than M6 as a natural consequence of our selection criterium (see Sect. 2.2).


Figure 2.14: Comparing the spectral type of the secondary stars of the SEGUE-WDMS with those of single SDSS (West et al. 2008) and previous WDMS samples (Silvestri et al. 2006). The SEGUE WDMS distribution looks similar to the distribution of Silvestri et al. (2006) but with more early type secondaries.

We compared the spectral type distribution with single dM stars from West et al. (2008) and with the WDMS binaries from Silvestri et al. (2006), see Fig. 2.14. We find that the secondary spectral type distribution of our sample of WDMS binaries is narrower than for single dM stars (see left panel of Fig. 2.14), but broader than the distribution drawn for a sample of WDMS binaries by Silvestri et al. (2006). The peak at M3 is also present in field dM stars, while for the previous sample from Silvestri et al. (2006) it shifts to M4. Our sample compared with that of single low mass stars contains less systems with M0-M2 and late type companions. This indicates that our sample is still biased towards low mass secondaries. But we find more early type secondaries than in previous WDMS binary samples, hence, the goal of our target selection algorithm to establish a WDMS sample less biased towards late type secondary stars has been reached.

To compare the distributions in a quantitative manner we performed $\chi^{2}$-tests. We obtained a value of 101.47 when comparing with the distribution from West et al. (2008), and 97.10 when comparing with Silvestri et al. (2006). So it seems that our distribution is very likely to be differ-
ent from that one of field $M$ stars and from that one from the sample from Silvestri et al. (2006). Biases in our distribution are still present, and their influence is discussed in detail in Sect. 2.6,

### 2.5.4 Distances

We compare the two distances derived from our deconvolution process, $d_{\mathrm{sec}}$ and $d_{\mathrm{wd}}$. It seems that there are two trends, systems with $d_{\mathrm{wd}}>500 \mathrm{pc}$ seem to have systematically $d_{\mathrm{wd}}>d_{\mathrm{sec}}$, while the opposite is true for systems with $d_{\mathrm{wd}}<500 \mathrm{pc}$. A significant fraction of the systems has $d_{\mathrm{sec}}>d_{\mathrm{wd}}$ by more than $1.5 \sigma$ (red dots in Fig. 2.15 , similar results have been obtained previously by Rebassa-Mansergas et al. (2007) and Schreiber et al. (2008). Activity faking a too early a spectral type which leads to a too large distance estimate has been suggested as the cause of this trend by (Rebassa-Mansergas et al. 2007).

To explain the opposite trend at larger distances, we first did take into account the effect of reddening in our estimates of the distances. We used Schlegel dust maps (Schlegel et al. 1998) 8 to derive the extinction for each system and applied a correction to the distance. Of course, since the extinction values in Schlegel's map only depend on the galactic latitude and longitude (and not on the distance), the distance corrections should be interpreted as an upper limit on the effect of extinction on the distance determination. As nearby stars are less affected by reddening, we applied the reddening correction only to systems with $d_{\mathrm{wd}}>500 \mathrm{pc}$. Inspecting the left panel of Fig. 2.15 we see that the effect in some cases is far from being negligible but it can certainly not explain the observed discrepancy.

In the right panel of Fig. 2.15 we compare $d_{\mathrm{wd}}$ and $d_{\mathrm{sec}}$ for those sytems having system parameters with errors less than $25 \%$. Here, the effect of reddening was not taken into account, since most of the remaining systems have $d_{\mathrm{wd}}<500 \mathrm{pc}$ and correcting for the galactic reddening would probably lead to underestimating the distances. Apparently, in the right panel the discrepancy at large distances disappears thereby indicating that at very large distances the parameters from fitting the white dwarf spectrum are not reliable. In contrast, the disagreement at short distances remains. This means that the larger values of $d_{\text {sec }}$ are not caused by uncertainties related to noisy spectra which is in agreement with the interpretation that magnetic activity is causing the effect (see above and Rebassa-Mansergas et al. 2007).

### 2.5.5 Secondary masses

As shown e.g. in Rebassa-Mansergas et al. (2008) and as just discussed in the context of our distance estimates, activity seems to make a significant fraction of late type secondary stars appearing as an earlier spectral type than secondaries with the same mass but without magnetic activity. In these cases the empirical mass-spectral type relation by (Rebassa-Mansergas et al.

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Figure 2.15: Left: distances obtained for the WDMS that contain DA white dwarfs in our sample, based on spectral fits to the white dwarf $d_{\mathrm{wd}}$, and on the spectral fit to the secondary star $d_{\text {sec }}$. As noted earlier in Rebassa-Mansergas et al. (2007); Schreiber et al. (2008); Rebassa-Mansergas et al. (2008) about 30\% of the $d_{2}$ distances appear to be too large when compared to $d_{\mathrm{wd}}$. This is probably caused by magnetic activity in late type M-dwarfs. For systems at larger distances we here observe another effect, i.e. $d_{\mathrm{wd}}$ appears to be larger than $d_{\text {sec }}$ at distance exceeding $\sim 500 \mathrm{pc}$. This is only partially caused by reddening which makes especially distant white dwarfs appearing more distant than they actually are. Correcting for this reddening effect results in slightly shorter distances as displayed by the blue arrows. Right: The distribution of distances for systems with errors smaller than $25 \%$. Apparently, the agreement between the two distances is much better. More specifically, there is no longer a discrepancy at larger distances while the effect of having $d_{\mathrm{sec}}>d_{\mathrm{wd}}$ for about $30 \%$ of the systems at shorter distances remains.
2007) leads to systematically overestimating the secondary mass and consequently also to distance estimates that are systematically too large (see Fig.2.15).

In Nebot Gómez-Morán et al. (2009) we have developed and applied a possible way out of this problem based on information provided in the 2MASS data base. We find entries in the 2MASS catalog (Cutri et al. 2003) with photometric quality flags set to 'AAA' for 105 systems with DA primary star. We derive the masses of the secondary stars using the empirical mass $K$ luminosity relation from Delfosse et al. (2000), assuming $d_{\mathrm{wd}}$ as the distance to the system and subtracting the contribution of the white dwarf to the luminosity in the infrared (see chapter 6 for a detailed description of the method). The derived masses from 2MASS are compared with the masses obtained from the empirical spectral type-mass relation from Rebassa-Mansergas et al. (2007) in Fig.2.16, in the left panel we show all the systems while in the right panel we plot only those with relative errors lower than $25 \%$ in the white dwarfs parameters. The Sp2-mass relation seems to be overestimating the masses of the secondary stars for masses lower than $0.35 \mathrm{M}_{\odot}$, consistent with the 'activity hyphothesis', while the opposite trend is seen for masses


Figure 2.16: Comparison of the obtained secondary star masses from K-luminosity relation and the empirical spectral-type mass relation Rebassa-Mansergas et al. (2007). For low values $M_{2}(2 M A S S) \lesssim 0.35 \mathrm{M}_{\odot}$ the masses obtained from the spectral type-mass relation are systematically larger while the opposite is true for $M_{2}(2 M A S S) \geq 0.35 \mathrm{M}_{\odot}$. The discrepancy at low masses could be explained by activity in late type stars and we therefor consider the $M_{2}(2 M A S S)$ values to be more reliable in this mass range.
larger than 0.35 . This is probably related to the fact that more massive secondary stars are found at larger distances where the parameters for the white dwarf derived from spectral fitting become uncertain. From this study it becomes obvious the necessity of a better estimate of the masses in low mass stars. Eclipsing systems are very important in this context since we can contrain the radii and masses of the secondary stars accurately (see chapter 6).

### 2.6 Completeness

As described in Sect.2.2.3 our color selection has been designed to detect WDMS containing cold white dwarfs ( $\sim 10000-20000 \mathrm{~K}$ ) and these become hardly detectable in color-space for secondary stars earlier than $\sim M 3-M 2$ (see also Sect.2.5.3). As a consequence our sample is biased towards old systems containing late type secondary stars. The bias towards old systems has been a goal of the survey and the bias towards late type secondary stars is at least smaller than in previous samples. In this section we analyse how this bias relates to distances.

Our limiting $g$ magnitues, $15 \leq g \leq 20$ imply distance limits to detect a WDMS system for a given set of stellar parameters. These distance limits mainly depend on the white dwarf temperature and the secondary star spectral type. Following our approach in Sect. 2.2 we calculate for different white dwarf temperatures and secondary spectral types the distance at which
$g=20$ and $g=15$. The values obtained for the mass of the white dwarf and its effective temperature can be used to calculate the age of the WDMS binary by interpolating the cooling tracks by Wood (1995). Fig. 2.17 shows the lower and upper distance limits as a function of age for different secondary star spectral types. As mentioned above, our color selection citeria preferentially select old white dwarfs with late type secondary companions. Of such binaries (lower magenta and blue lines) only very nearby ( $d \leq 50 \mathrm{pc}$ ) systems are excluded by the lower distance limit (resulting from $g \geq 15$ ). The upper distance limits (upper lines) are significantly decreasing with increasing age of the WDMS binary (i.e. decreasing temperature of the WD) especially if little is contributed by the secondary in the g-band, i.e. if the secondary is a late spectral type. In other words, for old white dwarfs ( $\gtrsim 1 \mathrm{Gyr}$ ) with a M6 (M4) secondary star, the magnitude limit of $g \leq 20$ implies a distance limit of $d \lesssim 200 \mathrm{pc}(d \lesssim 500)$. This effect is displayed in Fig.2.18. With increasing distance earlier spectral type secondary stars are detected (top and middle panel). These systems contain systematically hotter white dwarfs than the nearby WDMS (bottom panel of Fig.2.18).

To summarize, the combination of our color selection criteria and the SDSS magnitude limits favours the detection of rather nearby ( $d \leqslant 500 \mathrm{pc}$ ) WDMS that contain cold white dwarfs and late type secondary stars. However, as WDMS systems containing cold white dwarfs should represent the vast majority of all WDMS binaries, we should be able to at least derive reasonable lower limits on the space density of WDMS.

### 2.7 The galactic WDMS population

In this section we base our analysis on the DR7 database. Please note that this excludes two WDMS systems (SDSSJ135643.56-085808.9 and SDSSJ135930.96-101029.7) that have been found on plate 2716 which is not included in DR7 (see http://www.sdss.org/dr7/start/aboutdr7.html).

### 2.7.1 Space density

To estimate the space density we performed a detailed analysis of our success rates for each plate-pair based on the CAS database DR7. Table 2.2 gives the most important numbers for each plate-pair that contained SEGUE-WDMS color-selection. $N_{\text {cand }}$ is the number of candidates, i.e. the number of systems with ugriz colors obeying our selection criteria and with clean photometry flags. $N_{\text {spec }}$ gives the number of candidates that have been observed spectroscopically. In some rare cases we find objects that got a spectrum although their flags indicate photometric problems. This is probably caused by changes in the photometry pipeline after the target selection process. In the very few cases were this happened, the missing system is added to the list of candidates. The total number of spectroscopically identified WDMS is given by $N_{\text {WDMs }}$. Please note that some early plates (plate numbers < 2377) have been accidently observed with a target selection algorithm based on reddening corrected colors. On these plates we therefore find some WDMS


Figure 2.17: The 193 DA WDMS of our sample in the distance-age plane. Using the approach described in Sect.2.2.3 we calculated distance limits corresponding to the magnitude limits $15 \leq g \leq 20$ for different secondary spectral types as a function of white dwarf age (i.e. decreasing white dwarf temperature). Apparently, systems older than 1 Gyr containing late type companions are only detected up to distances of $\sim 400-500 \mathrm{pc}$.
systems that are outside our color criteria. The number of these systems is given by $N_{\text {out }}$. The success rate of our target selection is hence given by $\left(N_{\text {WDMS }}-N_{\text {out }}\right) / N_{\text {spec }}$ and the intrinsic number of WDMS can be estimated by multiplying the success rate with the number of candidates for each plate. Dividing this number by the volume of the spherical sector finally gives the local space density. The volume of the spherical sector $V$, of course, depends on the distance that actually defines the survey volume. In the previous section we have shown that our selection criteria select mostly old systems with late type secondary stars and that this implies a selection effect even at rather short distances $d_{\sim}<100-200$ pc. Defining the survey volume is therefore not straight forward. If we use a very short distance, the involved selection effects decrease but our estimates are based on quite a few WDMS detections and the statistical error increases. If, on the other hand, a large distance is assumed (e.g. $d \sim 1000 p c$ ) the statistical error decreases but the selection effects begin to strongly influence our results leading to very much underestimating the space density. We performed a KS-test between the effective temperature distributions drawn for systems at larger distances than 500 pc and at closer distances to see whether they are similar


Figure 2.18: Relations between distance, secondary star spectral type and white dwarf temperature. With dashed lines are shown those systems with distance estimates exceeding 500 pc . As discussed in Sect. 2.6 the combination of our color selection and magnitude limits favours the detection of systems containing cold white dwarfs, that are nearby, and have late type secondary stars.
or not. We obtained a maximum distance in the cumulative function of 0.25 at a significance level of $0.4 \%$. We performed a KS test for the spectral type distributions as well and obtained a distance of 0.54 at a significance level of $\sim 4 \%$. From this analysis and inspecting Fig 2.17 and 2.18 we think that assuming $d=500 \mathrm{pc}$ is a reasonable compromise: we detect WDMS with secondary spectral types later than M3 and $63 \%$ of the identified WDMS are closer than $d=500 \mathrm{pc}$. The space density is then given by

$$
\begin{equation*}
\rho=\frac{\left(N_{\mathrm{WDMS}}-N_{\mathrm{out}}\right) N_{\text {cand }}}{V N_{\text {spec }}} . \tag{2.1}
\end{equation*}
$$

Estimates of the space density can be obtained for each plate by inserting the numbers for a given plate-pair. The space density of SEGUE-SDSS, shown in Fig. 2.19, varies from $\sim 2 \times 10^{-4}$ at low galactic latitudes to $\sim 2 \times 10^{-5}$ at higher galactic latitudes. The mean space density can be derived by averaging the space densities of all plates and we obtain $\rho=3.33 \times 10^{-5} \pm 6.6 \times 10^{-6} \mathrm{pc}^{-3}$. In Fig. 2.19 we show success rates and space densities for each plate pair as a function of galactic
latitude and $E(B-V)$.
The obtained space densities are smaller than the values predicted by Willems \& Kolb (2004) $\left(10^{-3}-10^{-4} \mathrm{pc}^{-3}\right)$. However, one should keep in mind that the predictions of Willems \& Kolb (2004) have been made for the entire WDMS population ranging from short orbital period post common envelope binaries to very wide systems and covering the whole range of possible secondary star masses. In contrast our SEGUE-WDMS sample is subject to serious biases and selection effects. First of all, based on ugriz colors it is impossible to detect white dwarf companions to secondary spectral types earlier than M0 but such systems certainly represent a significant fraction of the WDMS population simulated by Willems \& Kolb (2004, their Fig. 10). Second, a significant fraction of wide WDMS are resolved by SDSS imaging and are hence not in our sample. Willems \& Kolb (2004) give an upper limit of the PCEB fraction of $25 \%$ while Schreiber et al. (2008) obtain $35 \%$ from radial velocity studies of SDSS WDMS. This implies that only $\gtrsim 30 \%$ of the intrinsic WDMS population is resolved in the SDSS imaging data base. Taking into account the two effects just mentioned, our results are in agreement with those of binary population studies.

### 2.7.2 Spatial distribution

As WDMS binaries certainly form a relatively old stellar population they should be concentrated towards the Galactic plane and the space density $\rho$ of WDMS should exponentially decrease with the height above the Galactic plane $z$, i.e. $\rho \propto \exp (-z / h)$ where $h$ is the typical scale height of the population. Both plots on the right hand side of Fig. 2.19 show the expected steep decrease of the space density for increasing galactic latitude. In the lower right panel the error bars for low galactic latitudes are quite large as the obtained values depend on few WDMS ( $N_{\text {WDMS }}$ ) detections among large numbers of candidates ( $N_{\text {cand }}$ ). The dashed lines in the bottom right panel show calculated space densities as a function of galactic latitude assuming a limiting distance of $d=500 \mathrm{pc}$, and three different scale heights: 100,150 , and 200 pc . Keeping in mind the large uncertainties of the measured values of the space density close to the galactic plane we conclude that the SEGUE WDMS population agrees best with scale heights of $h=100-150 \mathrm{pc}$. This result appears to be reasonable as similar values have been obtained for cataclysmic variables (CVs) (Patterson 1984; Ak et al. 2008) and late type stars (Vallenari et al. 2006).

### 2.8 Summary

The SEGUE WDMS survey differs from SDSS I WDMS surveys in the applied color-selection algorithm. The SEGUE WDMS search has been especially designed to identify WDMS systems containing cold white dwarfs. In addition, SEGUE covered a much broader range of galactic latitudes. We here present 277 new white dwarf/main sequence binaries and 24 candidates identified with SEGUE. We characterized the sample using spectral decomposition techniques, discussed


Figure 2.19: Left: success rates as a function of galactic latitude and $E(B-V)$. The squares in the top panels and the lower left panel represent values derived for single plate-pairs as given in Table 2.2. The success rate is on average slightly better for low $E(B-V)$ and high galactic latitudes. Right: Space densities as a function of galactic latitude for each plate (top) and a binned distribution (bottom). In the top panel only values that differ from zero (i.e. those with at least one WDMS detection) are shown. The histogram in the bottom panel gives space densities averaged over a given range in $|b|$. As expected, the derived space densities increase towards the galactic plane. Also shown (dashed lines) are calculated space densities assuming an exponential distribution, a limiting distance of $d=500 \mathrm{pc}$, and scale height of $h=100,150$, and 200 pc .
the obtained distributions, and derived plausible values for the space density and the scale height. The main results of this analysis can be summarized as follows.

- As expected, our sample contains significantly more old systems than SDSS I. The combination of our color selection and the magnitude limits of SDSS causes our sample to be biased towards cold white dwarfs and late type secondary stars that are relatively nearby $d_{\approx} \leq 500 \mathrm{pc}$.
- The space density of WDMS inside our selection criteria is $\sim 2 \times 10^{-4} \mathrm{pc}^{-3}$ and decreases to $\sim 2 \times 10^{-5} \mathrm{pc}^{-3}$ at higher galactic latitudes.
- The space density of SDSS WDMS increases significantly towards the galactic plane in agreement with a scale height of the galactic population of WDMS binaries of $100-150 \mathrm{pc}$. This value is similar to values estimated previously for the population of cataclysmic variables and late type stars.


## Chapter 3

## Post common envelope binaries from SEGUE

White dwarf/main sequence binaries are perfect laboratory systems for testing current theories of angular momentum loss and constrain the efficiency of the common envelope phase. Using a sample of white dwarf/main sequence binaries We test the disrupted magnetic braking law that has been questioned in the last years. From a statistical analysis of the radial velocities measured from the SDSS sub-exposures of the 277 (plus one candidate) white dwarf/main sequence binaries with stellar parameters derived in chapter 2 we select those that have gone through a common envelope phase. We derive a lower limit of $\sim 13 \%$ to the post-common envelope fraction of white dwarf/main sequence binaries. The number of PCEBs decreases with increasing mass of the secondary star, and has a drop of $15 \%$ at the boundary where the secondary star becomes fully convective. This indicates that the angular momentum loss is less efficient at later spectral types, and according to predictions of binary population synthesis studies, in agreement with the disrupted magnetic braking law, firstly proposed to explain the orbital period gap between 2 and 3 hours in the orbital period distribution of cataclysmic variables.

### 3.1 Introduction

The orbital period distribution in cataclysmic variables (CVs) extends from $\sim 1$ hour to $\sim 10$ hours and presents a gap between 2-3 hours. To explain the observed orbital period distribution of CVs one needs to know which are the mechanisms involved in angular momentum loss. Above the orbital period gap the main mechanism leading to an angular momentum loss is magnetic braking (MB). The main idea of MB is that dynamo processes generate magnetic fields which are responsible of the spin-down of stars with age. Ionized material is coupled to the large scale magnetic field lines. Small amounts of mass are carried away in the magnetized stellar wind to large distances, carrying with it more angular momentum than it had at the surface, and slowing down the star (Verbunt \& Zwaan 1981). Below the period gap (2 hours) gravitational radiation is
responsible for bringing the systems closer $\left(\dot{J}_{G R} \propto \omega^{(7 / 3)}\right)$. To explain the period gap (only $10 \%$ of all the CVs are inside this region) it has been proposed that, since the dynamo changes once the star becomes fully convective (around spectral type M3), for later spectral types, which have no tachocline ${ }^{1}$ magnetic braking would be inefficient ( $\dot{J}_{D M B} \propto \omega^{3}$ for $M>M_{\text {conv }}, \dot{J}_{D M B}=0$ for $M<M_{\text {conv }}$ ), the so called disrupted magnetic braking (DMB) model (Rappaport et al. 1983).

Observations from field stars and open clusters seem to disagree with the DMB model. Delfosse et al. (1998) studied a sample of field M dwarfs and showed that only late spectral types have a measurable rotation, $v \sin i>2-3 \mathrm{~km} / \mathrm{s}$, and that young disk stars rotate faster than old disk stars. For interpreting this effect they suggested that the spin-down depends on the mass, low mass stars would need more time for decreasing their rotation, varying from few Gyr for M3-M4 to 10 Gyr for M6. They also observed that all fast rotating stars are active, and that the flux from the $\mathrm{H} \alpha$ emission increases with rotation until it saturates at a certain $v \sin i$, remaining constant for higher values. In other words, the flux in $\mathrm{H} \alpha$ is independent of the rotation for fast rotators. They see no clear change in the rotation nor the activity of the stars at the limit when they are fully convective.

Sills et al. (2000) studied a sample of 4 open clusters in the age range $30-600 \mathrm{Myrs}$ and find the DMB overestimates the angular momentum loss as given by Rappaport et al. (1983) at high rotation rates. They give an empirical AML law that fits the data better in the form $\dot{J} \propto \omega^{3}$, when the rotation is lower than $\omega_{\text {crit }}$ and $\dot{J} \propto \omega$ for faster rotations, the lower the value the longer a fast rotation can last. This model is known as the reduced magnetic braking (RMB). They find that $\omega_{\text {crit }}$ increases for increasing mass: low mass stars can have fast rotations for a longer time, in agreement with the idea of Delfosse et al. (1998). Since no sharp break in the angular momentum loss rate when the star becomes fully convective is seen, they claim that the DMB model can not be the cause of the period gap, but give no alternative explanation.

Politano \& Weiler (2006) proposed a new test for magnetic braking. They calculate the present day population of post common envelope binaries (PCEB) as a function of the secondary star mass assuming different mechanisms of angular momentum loss. Would magnetic braking get disrupted the number of PCEB be different by almost 2 orders of magnitude when the secondary becomes completely convective, around $0.3 \mathrm{M}_{\odot}$. They observe a decrease of $38 \%$ in the number of PCEBs at the boundary where the secondary star becomes fully convective, since magnetic braking would be more efficient for stars with a radiative core, the remaining systems would be already CVs. The influence of different efficiencies for the CE phase, the $\alpha_{C E} \mathrm{pa}$ rameter, which can be dependent or not on the mass of the secondary star is investigated by Politano \& Weiler (2007), finding that the total number of PCEBs is affected by the choice of $\alpha_{C E}$, but the drop at the fully convection boundary is always present.

The current observed population of PCEBs is very small. The pre-SDSS sample has been analyzed in detail by Schreiber \& Gänsicke (2003). They could discuss only 30 systems with determined orbital period and white dwarf temperature (today we know $\sim 50$, Morales-Rueda et al.

[^12](2005), and also see table 1.2.2). In the past, PCEBs have been discovered as white dwarfs in the first place, with some evidence for a faint red companion found later. Schreiber \& Gänsicke (2003) showed that the current sample of PCEBs is therefore not only small but also heavily biased towards hot white dwarfs and late type secondary star spectral types.

White dwarf/main sequence binaries (WDMS) represent the most numerous compact binaries in the universe. The population of WDMS binaries consists of two types of systems which differ due to their evolutionary history. According to recent binary population synthesis calculations more than $75 \%$ are wide binaries in which the stellar components evolve like single stars (Willems \& Kolb 2004). Virtually all of the remaining $\lesssim 25 \%$ suffered from common envelope evolution when the more massive star left the main sequence. This population of PCEBs represents the largest population of close compact binaries.

Fortunately, a large population of WDMS has been identified since the launch of the SDSS: based on SDSS imaging and some DR 1 spectra Smolčić et al. (2004) identified a new stellar locus in color-color diagrams, i.e. the WDMS binary bridge. Later, the SDSS turned out to be also very efficient in spectroscopically identifying new unresolved WDMS binaries, e.g. Silvestri et al. (2006) published a list of $\sim 747$ new WDMS binary systems found in SDSS/DR4 and Silvestri et al. (2007) published a list of more than 1200 systems using SDSS/DR5. These WDMS are biased towards hot white dwarfs and as pointed by Politano \& Weiler (2006) their sample is neither well-defined photometrically nor statistically complete and should not be considered as representative of the secondary mass function in PCEBs.

Recently Rebassa-Mansergas et al. (2009) published the most complete sample of WDMS binaries, with around 1600 WDMS. We have already measured the orbital period of a dozen of those systems (see Rebassa-Mansergas et al. (2008); Schreiber et al. (2008); Pyrzas et al. (2009); Nebot Gómez-Morán et al. (2009)).

In Schreiber et al. (2007) and in chapter 2 we describe a complementary survey, i.e. a dedicated search for old WDMS binaries performed with SEGUE. Using this sample of WDMS binaries we want to test the magnetic braking as suggested by Politano \& Weiler (2006). We identified the PCEBs using radial velocities and calculated the fraction of PCEBs among the WDMS sample.

### 3.2 The data: SDSS subspectra

Since the DR6 of the SDSS (Adelman-McCarthy et al. 2008) access is given to the sub-spectra of which every spectrum is composed. Sub-exposures of up to 25 minutes are taken and coadded to achieve sufficient signal to noise in a single spectrum. We have retrieved the individual subexposures of the 277 WDMS systems from chapter 2. In total we have 2048 spectra, that is 7 spectra per object in mean. In Fig. 3.6 we show in the upper panel the frequency of the number of sub-spectra per object. Most of the systems got 5-7 sub-exposures, with a minimum of 2 and up to a maximum of 19 sub-exposures. In the bottom panel we show the time elapsed between
the first and the last exposures for each system as a function of the number of sub-exposures. Some systems are observed only during one night, while others are reobserved months later. In general, systems with more sub-exposures are spread over a wider range in time, but there can be up to 8 sub-exposures in one night.

### 3.3 Post common envelope binary identification

As shown by Rebassa-Mansergas et al. (2007) it is possible to identify PCEBs among WDMS binaries from multiple SDSS spectroscopy, and as shown by Schwope et al. (2009) when the signal to noise in the individual sub-exposures that make a SDSS spectrum is high enough, radial velocities can be measured with sufficient accuracy.

We measured radial velocities by fitting a double Gaussian of fixed separation to the laboratory value of the Na absorption doublet ( $8183 / 8194 \AA$ ) originating from the atmosphere of the secondary star, plus a polynomial to the normalized continuum. We also measured the radial velocity from the $\mathrm{H} \alpha$ by fitting a polynomial, representing the underlying continuum, plus a Gaussian for the emission line.

We calculated the $\chi^{2}$ of the $n$ radial velocities with respect to the mean value:

$$
\begin{equation*}
\chi^{2}=\sum_{k=1}^{n}\left[\frac{\mathrm{RV}_{k}-\overline{\mathrm{RV}}}{\sigma_{\mathrm{RV}_{k}}}\right]^{2} \tag{3.1}
\end{equation*}
$$

and the probability for a $\chi^{2}$ value with $N=n-1$ degrees of freedom, to exceed the calculated $\chi^{2}$ value, which is given by

$$
\begin{equation*}
P(\chi ; N)=\int_{\chi^{2}}^{\infty} \frac{2^{-N / 2}}{\Gamma(N / 2)} \chi^{\prime N-2} e^{-\chi^{\prime 2} / 2} d \chi^{\prime 2} \tag{3.2}
\end{equation*}
$$

where $\Gamma(x)$ is the gamma function. We consider strong PCEB candidates those systems showing a probability at a significance level $\geq 99.73 \%$. In Fig. 3.2 we plot the radial velocities for a subsample of systems, with PCEBs highlighted in pink ${ }^{2}$ and the name of the particular system written above.

1. PCEB identification from SDSS-sub-exposures Among the 277 WDMS from chapter 2, 29 systems were identified as PCEB from the Na doublet (see Fig. A.1) and 28 systems from the $\mathrm{H} \alpha$ emission (see Fig. A.2). We considered all the systems satisfying the criterium aabove explained as PCEB, independent on the spectral line which was used for measuring the radial velocities. We identified a total of 33 PCEBs alone from the SDSS-sub-exposures. Some systems had only two-three sub-exposures and for many systems

[^13]

Figure 3.1: Example of a single spectral exposure ( 30 min ) and radial velocities fits for the $\mathrm{H} \alpha$, emission line and the Na absorption doublet shown in the boxes.
the time span between sub-exposures was very short, around 4 hours, therefore no significant radial velocity variation could be measured, perhaps faking a wide system (only short orbital period systems can be detected in such a short time span). In Fig. 3.1 we show an example of one of the sub-exposures of SDSS1055 +4729 , where the fits to the $\mathrm{H} \alpha$ emission line and to the Na doublet are shown in the left and the right boxes respectively.
2. PCEB identification from spectroscopic follow-up From own observations we have identified 19 PCEBs (see chapter 4), three of them where not classified as such when using the sub-spectra: SDSS1429+5759, SDSS1436+5741 and SDSS1437+5737.
3. PCEB identification combining SDSS with own spectroscopic follow-up Finally if we combine the data from own observations with the sub-exposures from the SDSS database we were able to identify one further PCEB candidate: SDSS2258+0710.

SDSS1436+5741 was classified as a candidate (dM plus a blue excess) in chapter 2, and it's binary nature is clear from the radial velocity shifts. We include this system in our study, which brings the total number of WDMS to 278 and among those we have identified 37 secure PCEBs. On the other hand 45 systems do not show any radial variation which means that either they have a low inclination or that they are wide systems (see Sect. 3.4.2). We list the radial velocities of the 37 PCEBs in table 3.2. In the following sections we will refer as 'wide' systems to all those


Figure 3.2: Radial velocities of the Na absorption doublet for a subsample of WDMS binaries taken around R.A. 03. PCEB candidates are plotted in pink.

Table 3.2: Radial velocities of the WDMS measured from the SDSS subexposures. Extract of the table, for a complete table see the appendix.

| Name |  |  | Name |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| HJD | $\mathrm{RV}(\mathrm{Na})$ | $\mathrm{RV}(\mathrm{H} \alpha)$ | HJD | $\mathrm{RV}(\mathrm{Na})$ | $\mathrm{RV}(\mathrm{H} \alpha)$ |
| SDSS0142-0835 |  |  | SDSS114+0924 |  |  |
| 54469.5887 | $4.1 \pm 13.5-17.3 \pm 11.954169 .7317-103.2 \pm 17.6$ |  |  |  |  |
| 54469.6080 | - $5.8 \pm 14.6-13.8 \pm 13.154169 .7494$ |  |  | $-45.4 \pm 21.5$ |  |
| 54491.5776 | $6-18.3 \pm 13.2-23.7 \pm 12.554169 .7691$ |  |  | $53.2 \pm 24.5$ |  |
| 54491.6026 | -9.9 $\pm 14.2-29.3 \pm 13.854169 .7883$ |  |  | $105.4 \pm 22.2$ | $113.0 \pm 17.4$ |
| 54495.5732 | $28.4 \pm 12.6$ | $6.2 \pm 15.754169 .8095$ |  |  | $130.6 \pm 18.4$ |
| 54495.5928 | 23.4 $\pm 15.0 \quad 17.5 \pm 14.2$ |  |  | SDSS1123-1155 |  |
| 54497.5811 | $-37.4 \pm 13.9-47.5 \pm 13.954565 .6238$ |  |  | $-124.7 \pm 11$ | $-132.1 \pm 10.5$ |
| 54497.6022 | $-27.8 \pm 14.3-54.5 \pm 15.7$ |  | 54565.6397 | $-120.9 \pm 11.4$ | $-124.0 \pm 10.6$ |
| 54498.5811 | $-0.3 \pm 15.5$ | $2.1 \pm 12.1$ | 54565.6553 | $-111.8 \pm 12.0$ | $-124.3 \pm 10.6$ |
| 54498.6039 | $11.1 \pm 16.6$ | $8.2 \pm 12.6$ | 54568.6426 | $-122.9 \pm 12.7$ | $-147.2 \pm 10.8$ |
| 54499.5716 | $-3.5 \pm 12.7$ | $1.2 \pm 15.5$ | 54569.6279 | $15.1 \pm 11.8$ | $3.0 \pm 10.9$ |
| 54499.5945 | $5 \quad 8.3 \pm 14.6$ | $-26.9 \pm 16.5$ | 54569.6534 | $43.5 \pm 11.9$ | $35.6 \pm 11.3$ |

systems that are not PCEB candidates but we make the reader note that this might contain a small fraction of close binaries.

Table 3.3: Stellar parameters derived from the SDSS spectrum for the 37 PCEB detected through radial velocity variations measured from the Na doublet or/and the $\mathrm{H} \alpha$ emission line. Maximum orbital period are calculated and shown in the last column.

| System (SDSS) | type | $T_{\text {eff }}(\mathrm{K}) \quad \log g$ | $M_{\text {wd }}\left(\mathrm{M}_{\odot}\right)$ | $d_{\text {wd }}(\mathrm{pc}) \mathrm{Sp} M_{\text {sec }}\left(\mathrm{M}_{\odot}\right)$ |  |  | $d_{\text {sec }}(\mathrm{pc})$ | $\mathrm{P}_{\text {arb }}^{\max (d)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0142-0835 | DA/dM | $9187 \pm 1488.77 \pm 0.18$ | $1.08 \pm 0.10$ | $113 \pm 17$ | 3 | 0.380 | $428 \pm 84$ | $121{ }^{4}$ |
| $0239+2736$ | DA/dM | $12681 \pm 11457.91 \pm 0.38$ | $0.56 \pm 0.23$ | $468 \pm 107$ | 4 | 0.319 | $774 \pm 228$ | 0.784 |
| $0301+0502$ | DA/dM | $11565 \pm 6808.46 \pm 0.23$ | $0.90 \pm 0.14$ | $209 \pm 36$ | 4 | 0.319 | $380 \pm 112$ | $0.982^{1}$ |
| $0307+3848$ | DA:/dM |  |  |  | 3 | 0.380 | $373 \pm 73$ |  |
| $0420+0649$ | WD/dM |  |  |  | 5 | 0.255 | $173 \pm 89$ |  |
| $0722+3859$ | DA:/dM |  |  |  | 4 | 0.319 | $264 \pm 78$ |  |
| $0730+4054$ | WD/dM |  |  |  | 3 | 0.380 | $295 \pm 58$ |  |
| $0734+4105$ | DA/dM | $19868 \pm 3538.01 \pm 0.07$ | $0.63 \pm 0.04$ | $299 \pm 14$ | 3 | 0.380 | $354 \pm 70$ | 13.742 |
| $0753+1754$ | DA/dM 1 | $18756 \pm 14158.36 \pm 0.30$ | $0.84 \pm 0.18$ | $553 \pm 121$ | 4 | 0.319 | $545 \pm 161$ | 3.730 |
| $0853+0720$ | DC/dM |  |  |  | 3 | 0.380 | $573 \pm 113$ |  |
| $1021+1744$ | DA/dM 3 | $32972 \pm 20388.65 \pm 0.36$ | $1.03 \pm 0.18$ | $720 \pm 207$ | 4 | 0.319 | $435 \pm 128$ | 0.571 |
| $1024+1624$ | DA/dM 1 | $15422 \pm 10498.31 \pm 0.21$ | $0.81 \pm 0.13$ | $385 \pm 59$ | 3 | 0.380 | $403 \pm 79$ | 19.400 |
| $1028+0931$ | DA/dM | $18756 \pm 3138.29 \pm 0.06$ | $0.80 \pm 0.04$ | $144 \pm 7$ | 3 | 0.380 | $125 \pm 25$ | 0.891 |
| $1047+4835$ | DA/dM 1 | $12681 \pm 13947.84 \pm 0.45$ | $0.52 \pm 0.27$ | $610 \pm 161$ | 3 | 0.380 | $1048 \pm 206$ | 31.886 |
| $1055+4729$ | DA/dM | $10073 \pm 5799.50 \pm 0.08$ | $1.37 \pm 0.02$ | $73 \pm 7$ | 3 | 0.380 | $269 \pm 53$ | $24.830^{2}$ |
| $1105+3851$ | DA/dM | $10548 \pm 1428.18 \pm 0.13$ | $0.71 \pm 0.09$ | $205 \pm 19$ | 3 | 0.380 | $462 \pm 91$ | $1.499^{1}$ |
| $1114+0924$ | DA/dM | $10427 \pm 2118.28 \pm 0.23$ | $0.78 \pm 0.15$ | $236 \pm 38$ | 5 | 0.255 | $465 \pm 238$ | 3.762 |
| 1123-1155 | DA/dM | $10073 \pm 2159.12 \pm 0.25$ | $1.25 \pm 0.08$ | $64 \pm 14$ | 5 | 0.255 | $117 \pm 6$ | 13.974 |
| $1135+0103$ | DA/dM 3 | $30071 \pm 30766.41 \pm 0.66$ | 0.18 | $23 \pm 1174$ |  | 0.319 | $550 \pm 16$ | 0.269 |
| $1300+1908$ | DA/dM | $8673 \pm 2598.81 \pm 0.41$ | $1.10 \pm 0.18$ | $123 \pm 39$ | 4 | 0.319 | 378 | $21.461^{1}$ |
| 1316-0037 | DC/dM |  |  |  | 3 | 0.380 | $394 \pm 78$ |  |
| $1320+6612$ | DA/dM | $28389 \pm 14078.05 \pm 0.27$ | $0.67 \pm 0.16$ | $719 \pm 131$ | 1 | 0.464 | $976 \pm$ | $11.454^{4}$ |
| $1348+1834$ | DA/dM | $15071 \pm 3557.96 \pm 0.07$ | $0.59 \pm 0.04$ | $180 \pm 8$ | 4 | 0.319 | $236 \pm 69$ | $0.346^{1}$ |
| $1429+5759$ | DA/dM 1 | $16336 \pm 17818.69 \pm 0.35$ | $1.04 \pm 0.17$ | $378 \pm 104$ | 3 | 0.380 | $632 \pm 124$ | 1,3 |
| $1436+5741$ | cand |  |  |  | 3 | 0.380 | $511 \pm 101$ | 1,3 |
| $1437+5737$ | DA/dM | $17912 \pm 8468.12 \pm 0.19$ | $0.69 \pm 0.120$ | $392 \pm 50$ | 4 | 0.319 | $323 \pm 95$ | ${ }^{3}$ |
| $1524+5040$ | DA/dM | $19640 \pm 5878.14 \pm 0.12$ | $0.71 \pm 0.07$ | $221 \pm 18$ | 3 | 0.380 | $336 \pm 66$ | $1.082^{1}$ |
| $1558+2642$ | DA/dM 1 | $14560 \pm 40698.74 \pm 0.64$ | $1.07 \pm 0.26$ | $281 \pm 129$ | 4 | 0.319 | $320 \pm 94$ | $2.328^{1}$ |
| $1623+6306$ | DA/dM | $9731 \pm 2898.63 \pm 0.35$ | $1.00 \pm 0.19$ | $180 \pm 48$ | 4 | 0.319 | $335 \pm 99$ | $21.483^{1}$ |
| $1625+6400$ | DA/dM | $8773 \pm 1698.31 \pm 0.27$ | $0.79 \pm 0.17$ | $155 \pm 30$ | 6 | 0.196 | $212 \pm 98$ | $3.270^{1}$ |
| $1635+6201$ | DA/dM | $17505 \pm 5827.81 \pm 0.13$ | $0.52 \pm 0.07$ | $378 \pm 31$ | 3 | 0.380 | $514 \pm 101$ | 10.907 |
| $1724+0733$ | DA/dM | $13588 \pm 9898.02 \pm 0.24$ | $0.62 \pm 0.15$ | $384 \pm 59$ | 4 | 0.319 | $324 \pm 95$ | $113.591^{4}$ |
| $1844+4120$ | DA/dM | $7554 \pm 287.45 \pm 0.12$ | $0.33 \pm 0.05$ | $75 \pm 5$ | 6 | 0.196 | $58 \pm 27$ | $6.320^{1}$ |
| $1919+6214$ | WD/dM |  |  |  | 3 | 0.380 | $583 \pm 115$ |  |
| $2243+3122$ | DC/dM |  |  |  | 5 | 0.255 | $171 \pm 87$ | 1 |
| $2258+0710$ | DA/dM | $8475 \pm 2728.07 \pm 0.57$ | $0.64 \pm 0.37$ | $248 \pm 87$ | 5 | 0.255 | $351 \pm 180$ |  |
| $2311+2202$ | DA/dM | $10189 \pm 4608.92 \pm 0.40$ | $1.16 \pm 0.15$ | $163 \pm 52$ | 3 | 0.380 | $536 \pm 105$ | $3.806^{1}$ |

${ }^{1}$ The orbital period was measured and is given in table 4.3. ${ }^{2}$ The stellar parameters are uncertain due to poor signal to noise in the SDSS spectrum. ${ }^{3}$ Only two subspectra were available, therefore the system was not classified as PCEB from the SDSS alone, but further spectra showed strong radial velocity variation. ${ }^{4}$ The systems was classified as a PCEB only through variation in the $\mathrm{H} \alpha$ emission line.

### 3.4 Results

### 3.4.1 The PCEB fraction

The fraction of PCEBs among WDMS binaries and the corresponding distributions of their stellar parameter represents an important tool to constrain current theories of close binary formation and evolution. We estimate that the fraction of PCEB among WDMS is $>13 \%$, lower than the predicted value of $25 \%$ by Willems \& Kolb (2004). Nevertheless our estimated value is just a lower limit to the total number of PCEBs. Many of the subexposures were taken in one day a most of them in a time span of less than 10 days so our result is strongly biased towards fast rotating system, i.e. short orbital periods, being therefore just a lower limit of the entire population of PCEB. Also a number of systems with low orbital inclination will not be detected as PCEBs. Based on 101 WDMS binaries with multiple SDSS spectra, Rebassa-Mansergas et al. (2007) estimated a fraction of PCEBs to WDMS of $\sim 15 \%$. Later on Schreiber et al. (2008) based on a subsample of these 101 WDMS and taking higher S/N spectra found a value of $35 \pm 12 \%$. This result suggests that our observed fraction is a lower limit and underlines the relevance of taking further spectra with higher $\mathrm{S} / \mathrm{N}$.

## The secondary spectral type distribution in the SEGUE PCEB sample

The fraction of PCEBs in the SEGUE subsample is presented in the bottom left panel Fig. 3.4 as a function of the secondary spectral type with Poissonian errors. For completeness the spectral type distribution is included in the upper panel, where WDMS are plotted with solid line and PCEBs with dashed lines. The PCEB fraction is strongly correlated with the spectral type of the secondary star, increasing towards later spectral types. The fraction of PCEB in the SEGUE subsample presents a drop of $17 \%$ around M3. This subsample has been combined with SDSSWDMS to create a dataset representative of the entire population of WDMS binaries, which is better populated at earlier and later spectral types. In the right panels of Fig. 3.4 we show the spectral type distribution of the entire sample composed of 589 WDMS binaries (solid line), among which 193 are PCEBs (plotted with dashed line). The fraction of PCEBs, shown in the bottom panel, is around $20 \%$ for early spectral types, M0 - M3, increasing towards later spectral types until it reaches $\sim 50 \%$ at M5, where it seems to be flat until it drops again to $20 \%$ at M8. The decrease in the fraction of PCEBs around the spectral type where the secondary stars are fully convective, M3 is of the order of $80 \%$. Politano \& Weiler (2006) predict a pronounced drop in the relative number of PCEBs around this range in spectral type, $38-73 \%$ for disrupted magnetic braking, where the relative fraction depends on the efficiency of the CE phase. When assuming any other prescription for AML, only GR, GR plus IMB or GR plus RMB this feature would not be present (see Fig. 3.3). We have therefore confirmed DMB (Schreiber et al.submitted).


Figure 3.3: Fraction of PCEBs as a function of the secondary spectral mass when assuming different prescriptions for the angular momentum loss: only GR, GR $+\mathrm{DMB}, \mathrm{GR}+\mathrm{IMB}$ and $\mathrm{GR}+\mathrm{RMB}$. Figure was taken from Politano \& Weiler (2006).

## The white dwarf mass distributions

The $M_{\text {wd }}$ distribution of the WDMS containing a DA as primary star and with $T_{\text {eff }}>12000 \mathrm{~K}$ and with relative errors lower than $25 \%$, so that it's spectroscopic mass is reliable (Kepler et al. 2007), is shown in Fig. 3.5. This distribution is explained in chapter 2, so we just mention here that it resambles the distribution of single white dwarfs, peaking around $0.6 \mathrm{M}_{\odot}$ and decreasing towards higher masses. With dashed lines the distribution of PCEB is overplotted. After the strong filtering of having a relative error lower than $25 \%$ and an $T_{\text {eff }}>12000 \mathrm{~K}$ we end up with only 11 PCEB, which is not enough to draw any significant result. Nevertheless we comment that the $M_{\mathrm{wd}}$ distribution in the PCEB SEGUE subsample spreads from 0.5 to $0.9 \mathrm{M}_{\odot}$ and that it is wider, with a mean value of $M_{\mathrm{wd}}=0.607 \mathrm{M}_{\odot}$, differing from that one of single white dwarfs. All WDMS which have a primary star with lower mass than $\sim 0.48 \mathrm{M}_{\odot}$, that is He core WDs, are thought to be PCEBs (Liebert et al. 2005) (see chapter 1). We have 6 WDMS with $M_{\text {wd }}<0.48$ which show no significant radial velocity variation, even though their spectra are spread over several days. In Chapter 4 we discuss in detail the $M_{\text {wd }}$ distribution of PCEBs.

### 3.4.2 Upper limits on the orbital period

Among the 37 PCEBs, 24 contain a white dwarf of type DA as a primary star, for which we were able to derive the mass (see 2). Using these and assuming the maximum radial velocity



Figure 3.4: The distribution of the secondary spectral type for all the WDMS is shown in the upper panels, PCEB are overplotted with dashed lines. In the panels bellow we show the fraction of PCEB as a function of the secondary mass, with Poissonian errors. In the left panels we show the distribution and fractions from the SEGUE subsample, wich forms part of the larger sample from SDSS shown in the right panels.
difference to be equal to the radial velocity semi-amplitude and assuming an inclination of $90^{\circ}$ we have derived upper limits on the orbital period using Kepler's third law:

$$
\begin{equation*}
P_{\text {orb }}=2 \pi G \frac{\left(M_{\mathrm{wd}} \sin i\right)^{3}}{\left(M_{\mathrm{wd}}+M_{\mathrm{sec}}\right)^{2}} \frac{1}{K_{\mathrm{sec}}^{3}} \simeq 2 \pi G \frac{M_{\mathrm{wd}}{ }^{3}}{\left(M_{\mathrm{wd}}+M_{\mathrm{sec}}\right)^{2}} \frac{1}{\Delta V^{3}} \tag{3.3}
\end{equation*}
$$

We include the estimated upper orbital period in Table 3.3.

### 3.5 Discussion

To understand our detection biases we have to investigate how the spectra are spread in time. In Fig. 3.6 we show the frequency in the number of sub-spectra per object (upper panel), where we can see that most of the systems have around 5-7 sub-exposures. The maximum time elapsed between the exposures ranges from $\sim 1$ hour to several hundreds of days (lower panel). Systems


Figure 3.5: White dwarf mass distribution of all the WDMS containing a DA as a primary and with $T_{\text {eff }}>12000 \mathrm{~K}$ and a relative error lower than $25 \%$, with overplotted values for the PCEB with dashed line.
with more spectra cover in general a broader range in time. On the one hand where the sampling covers just few hours we are only sensible to shorter orbital period systems ( $P_{\text {orb }}<1$ day). On the other hand many spectra were taken covering several days and we should then be able to detect the long orbital periods as well. We separate PCEBs from wide systems, with open circles we show those systems where no high radial velocity variation was found, while we show those systems above the $3-\sigma$ detection with crosses.

Apparently there is no preference in the diagram for one or another type. There are 114 systems for which the sub-spectra were taken during the same night, among these, only 9 were detected as being PCEB candidates. That represents less than $8 \%$ of the systems. This low fraction of PCEBs indicates that, for systems with such a sampling, we are biased towards detection of short orbital periods, missing all the long orbital periods in this area. Among these systems we have measured the orbital period of 4 systems and all of them have periods shorter than $\sim 10$ hours. At this point, it is worth mentioning that the three systems which are confirmed as PCEBs from own spectroscopic observations (SDSS1429+5759, SDSSS1436+5741 and SDSS1437+5737) had only 2 sub-exposures spread in less than 1 hour, and could therefore not be detected as PCEBs alone from the SDSS-sub-spectra. We have measured the orbital period for two of those systems and they do have a period longer than 12 hours in agreement with the statement made before.

We find 24 PCEB candidates among systems with a sampling spread over more than a day, representing a fraction of $\sim 15 \%$. Among these 24 PCEB candidates we have measured the orbital period of 9 systems, and just 1 has an orbital period longer than a day. For these systems,
in principle we are not biased towards short orbital periods due to the sampling. But we might still be biased because long orbital periods have lower radial velocity amplitude and that might cause the system to fall outside our criteria although it is a PCEB. We now investigate this possible bias.


Figure 3.6: Frequency of number of sub-spectra per system (upper panel). Maximum difference in time versus number of sub-spectra per system. Confirmed PCEBs are plotted with crosses while the rest of the systems are plotted with open circles.

Using the mass function we have derived the possible radial velocity amplitudes for the secondary star as a function of the inclination, the mass of the white dwarf, the mass of the secondary and the orbital period. In Fig. 3.7 we plot $\mathrm{K}_{\text {sec }}$ for $M_{\mathrm{wd}}=0.3,0.6,0.9 \mathrm{M}_{\odot}$ plotted with solid, dotted and dashed lines respectively, for inclinations of $30^{\circ}$ (black), $60^{\circ}$ (red) and $90^{\circ}$ (blue) and for a typical spectral type M3, $M_{\text {sec }} \sim 0.35 \mathrm{M}_{\odot}$.

From the SDSS-sub-exposures we have a typical error of $15 \mathrm{~km} / \mathrm{s}$ in the radial velocity, with this relatively large error the minimum $\Delta R V$ that we have been able to detect is around $45 \mathrm{~km} / \mathrm{s}$.


Figure 3.7: Radial velocity amplitude of the secondary star as a function of the orbital period. $K_{2}$ is calculated for different primary masses, $M_{\mathrm{wd}}=0.3,0.6,0.9 \mathrm{M}_{\odot}$ from left to right, and for orbital inclinations 30,60 and 90 degrees. A detection limit of $45 \mathrm{~km} / \mathrm{s}$ is over-plotted with a dotted-dashed line.

This limit defines the minimum orbital inclination at a given orbital period that a system can have to be detectable with out sensitivity and is presented in Fig. 3.8. In other words, at a certain orbital period we should be able to detect all systems above this critical inclination. As we can see, for a given secondary star, which in this example was fixed to a spectral type M3 ( $M_{\text {sec }} \sim 0.35$ $\mathrm{M}_{\odot}$ ), the higher the primary's mass the longer the orbital period we will be able to detect, since lower masses will have smaller values of $\mathrm{K}_{\text {sec }}$. Now we may ask ourselves how many systems have a higher inclination and how many systems will have a lower inclination and will therefore be outside of our detection limit. The probability of an orbit to have a inclination, $i$, larger than a certain value is given by $\cos (i)$. In Fig. 3.9 we show the detection probability, assuming there is no preference for a certain inclination, of a system having an orbit with an inclination higher than the critical inclination as a function of the orbital period.


Figure 3.8: Minimum orbital inclination that can be detected as a function of orbital period for the same masses as in the Fig. 3.7.


Figure 3.10: Cumulative sampling distribution.


Figure 3.9: Probability of detecting a larger inclination than the critical detection inclination as a function of the orbital period, again for the same masses as for the plot above.


Figure 3.11: Probability of detection as a function of the orbital period, where the sampling has been taken into account.

But we would like to include our sampling into the detection probability. In Fig. 3.10 we show the cumulative sampling distribution, using the maximum difference in time between the sub-
exposures as the sampling time. Under the conservative assumption that in order to detect variability for a system with a given period we need to cover at least half of an orbit ( $\Delta \mathrm{HJD} \simeq \frac{1}{2} P_{\text {orb }}$ ) we have calculated the detection probability by multiplying the previously calculated detection probability (see Fig. 3.9) with the inverse of the CDF (Fig. 3.10), see Fig. 3.11.

For a typical white dwarf mass of $0.6 \mathrm{M}_{\odot}$ and a typical M3 ( $\sim 0.35 \mathrm{M}_{\odot}$ ), represented with dotted lines in Fig. 3.7,3.8,3.9 and 3.11, this implies that it is possible to detect higher inclination systems than e. g. 40 degrees up to orbital periods of 6 days, which translates into a probability detection of $\sim 50 \%$.

From this analysis we learn two important things: on the one hand we will always be able to detect short orbital periods ( $<1$ day) since the minimum inclination that we are able to detect is lower and the detection probability at higher inclinations than the critical inclination is very high ( $>80 \%$ ); and on the other hand we should be able to detect long orbital periods up to several days even for the less favored case, corresponding to low $M_{\mathrm{wd}}$.

### 3.6 Summary

Using the SDSS sub-exposures that are coadded to create a single SDSS spectrum, based on a statistical approach we have discovered 33 new PCEBs. Combining with own spectroscopic follow-up we have increased that number to 37. The PCEB fraction is $\sim 13 \%$, number below the theoretical value predicted by Willems \& Kolb (2004). Nevertheless our result is just a lower limit to the total number of PCEB in the sample, in order to have the complete number further spectroscopy is required. The fraction of PCEBs increases towards later spectral type secondary stars, presenting an increase between M2-M3, where the secondary becomes fully convective, which according to Politano \& Weiler (2006) indicates that magnetic braking gets disrupted once the secondary becomes fully convective (at around $0.35 \mathrm{M}_{\odot}$ ). We have studied our detection probability finding that even though we are biased towards systems with short orbital periods ( $<1$ day) we should be able to detect as well longer orbital periods. Given our sampling rate and radial velocity accuracy we reach a $50 \%$ detection probability at an orbital period of 2 days, and we are completely insensitive for objects with periods longer than $\sim 10$ days. To test the exintance of longer orbital period systems we need a better sampling and better spectral resolution.

## Chapter 4

## Orbital period distribution of PCEBs

The number of PCEB with orbital period known and well determined stellar parameters was only $\sim 30$ in 2003. From spectroscopic and photometric follow-up observations we measured the orbital period of 15 new systems, in the range $2.8 h<P_{\text {orb }}<2 d$. This sample provides the largest sample of post common envelope binaries until the date to be used to proof the CE efficiency. We analyze the orbital period and the white dwarf mass distributions. We analyze the remaining PCEBs in detail and constrain their orbital period limit, finding 7 long orbital period candidates and 15 short orbital period candidates.

### 4.1 Observations and reduction

### 4.1.1 Spectroscopic follow-up observations

We made spectroscopic follow-up observations of 65 WDMS binaries at different telescopes. The SEGUE WDMS project is part of a large multinational campaign, where several observers have been involved. We describe in detail the spectroscopic observations and reduction that took place in Calar Alto, where the writer was the responsible and list in Table 4.1 the telescopes, period, number of nights, observed time, and name of the observers during that period.

## TWIN at the 3.5m Telescope

Observations at the 3.5 meter telescope in Calar Alto (Spain) were carried out during 19-24 July 2007, 09-13 and 26-30 June, 23-27 July, 17-21 October 2008, between the 30 April and 4 May 2009, and between the 09-13 and the 23-27 September 2009. Observations were carried out for a total of 31 nights, $3 \%$ of the time was lost due to technical problems and $40 \%$ due to bad weather conditions, leaving $57 \%$ of the time for observations. A total of 430 spectra were taken during

Table 4.1: Observations carried out at the 3.5 m telescope in Calar Alto with the period over which the obervations took place, the name of the observers, the number of nights and the observed time.

| Telescope Period | Observers | $\mathrm{N}^{\circ}$ Nights Observed (\%) |  |
| :---: | :---: | :---: | :---: |
| CAHA3.5 2007 | Ada Nebot | 6 | 83 |
| 2008A1 | Ada Nebot, Alberto Rebassa-Mansergas | 5 | 60 |
| 2008A2 Ada Nebot, Stelios Pyrzas, Matthias Müller | 5 | 100 |  |
| 2008B1 | Ada Nebot, Stelios Pyrzas | 5 | 80 |
| 2008B2 | Robert Schwarz, Matthias Müller | 5 | 22 |
| 2009A1 | Ada Nebot, Daniele Faccino | 5 | 0 |
| 2009A2 | Ada Nebot, Justus Vogel | 5 | 65 |
| 2009B1 | Ada Nebot, Robert Schwarz | 5 | 55 |
| 2009B2 | Ada Nebot, Andreas Rabitz | 5 | 37 |

that time, and among these spectra, 309 were for SEGUE systems and are thus presented in the present work.

The TWIN spectrograph was equipped with the grating T05 in the blue arm and T06 in the red ( 1200 lines $/ \mathrm{mm}$ ) and all observations were done through a $1.5^{\prime \prime}$ width slit, giving a reciprocal dispersion of $0.54 \AA$ per pixel. The coverage was $\sim 4500-5500$ in the blue, covering $H \beta$, and $\sim 7500-8500 \AA$ in the red, to cover the Na doublet coming from the secondary star. The mean resolution estimated from the FWHM of sky emission lines in the spectra was approximately $1.6 \AA$ around $8200 \AA$. All exposures were done in synchronous mode and the exposure time was selected to optimize the signal in the red arm. Images were reduced using MIDAS and the spectra were extracted using the optimal algorithm (Horne 1986). We observed the standard stars BD332642, BD+254655 and Feige66 for flux calibration. HeAr arc lamps were used to calibrate in wavelength and to optimize the observations we cross-correlated the telluric lines to correct for wavelength shifts due to telescope flexures. We corrected the spectra from sky lines, for creating a sky spectrum template we used the standard stars.

## IMACS/Baade-Magellan, LDSS3/Clay-Magellan, EMMI/NTT, FORS/VLT, ISIS/WHT

Long slit spectroscopy was also carried out at the Baade and the Clay Magellan telescopes in Las Campanas, using LDSS3 and IMACS respectively; at the NTT in La Silla using EMMI. FORS2/VLT observations were carried out in service mode. Reduction and calibration were carried out in the same way as described in Rebassa-Mansergas et al. (2008). Since the observations were carried out in the same periods as the observations by Schreiber et al. (2008) and Rebassa-Mansergas et al. (2008) we refer the reader to those papers to see details. A total of 163 spectra were obtained for the SEGUE subsample.

A complete log of the observations is presented in Table 4.2, listing the 65 objects that were observed spectroscopically, the date of observation, the telescopes, the instrument and setup, the
integration time, the number of spectra taken and finally there is a column that indicates whether the system is a clear PCEB or not (see Chapter 3).

### 4.1.2 Photometric follow-up observations

## DuPont and IAC80 telescopes

Observations were carried out during 18-21 May 2007 at the DuPont telescope at Las Campanas (Chile). The telescope was equipped with the CCD camera, with a resolution of $0.259^{\prime \prime}$ per pixel over a field of 8.85 arcmin square. 337 frames were taken for SDSS0853+0720 in filter r and with a 40 seconds exposure time. Observations were carried out with the CCD camera CAMELOT installed at the IAC80 telescope in Observatorio del Teide (Spain) for SDSS2243+3122 in the sloan $i$ filter between the 15th and the 19th of August 2009. A total of 397 frames were taken with exposure time of 240 seconds. A binning of 2 was applied in both spatial directions and only a small window was read in order to decrease the readout time. The area covered by each frame was around $3^{\prime}$ at a resolution of $\sim 0.6^{\prime \prime} /$ pixel. Reduction was performed using standard packages in IRAF ${ }^{1}$. An observation log including all observations and details about exposure times, number of frames, filters and setup is given in Table 4.2.

### 4.2 Results

### 4.2.1 Orbital periods from spectroscopic observations

From the spectroscopic observations described in Sect. 4.1 we measured the RV velocities from the Na doublet for the 65 WDMS binaries and applied the same analysis described in Chapter 3 to identify the PCEBs. We identified 19 clear PCEBs and the rest did not show any high radial velocity variation. In Table 4.2 we include a column with this information. When only one spectrum was available from own observations we have combined the RVs with those from the SDSS-sub-spectra from Chapter 3 to discern whether the system is a PCEB or not.

A period search was performed by computing periodograms using the Multi-harmonic Fourier spectrum by orthogonal projections as implemented in MIDAS (Schwarzenberg-Czerny 1996). Trial periods were selected from the highest peaks and sine curves of the form:

$$
\begin{equation*}
v_{r}=\gamma_{\mathrm{sec}}+K_{\mathrm{sec}} \sin \left[\frac{2 \pi\left(t-t_{0}\right)}{P_{i}}\right], \tag{4.1}
\end{equation*}
$$

[^14]Table 4.2: Log of observations. Object name, date, telescope, instrument, and number of frames taken for each system. A last column indicating whether the system is a PCEB candidate is included.

| $\begin{aligned} & \hline \hline \text { Name } \\ & \text { (SDSS) } \end{aligned}$ | Date | TeI | Inst | $N_{\text {frames }}$ | PCEB? | $\begin{aligned} & \hline \hline \text { Name } \\ & \text { (SDSS) } \end{aligned}$ | Date | TeI | Inst | $N_{\text {frames }}$ | PCEB? |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0005+2434 | 27/07/08-22/10/08 | CAHA3.5 | TWIN | 3 | no | 1429+5759 | 20/07/07-01/07/08 | CAHA3.5 | TWIN | 16 | yes |
| $0006+2846$ | 09/09/09 | САНА3.5 | TWIN | 1 | no |  | 06/07/08-11/08/08 | WHT | ISIS | 5 |  |
| $0009+2432$ | 26/07/08-16/10/08 | CAHA3.5 | TWIN | 9 | no | 1436+5719 | 26/07/08-27/07/08 | WHT | ISIS | 2 | no |
| $0038+0834$ | 03/09/06 | VLT (sm) | FORS2 | 2 | no | $1436+5741$ | 19/07/07-01/07/08 | CAHA3.5 | TWIN | 19 | yes |
| 0103+0031 | 04/11/08-19/11/08 | VLT (sm) | FORS2 | 2 | no |  | 07/07/08-10/07/08 | WHT | ISIS | 4 |  |
| 0111+0009 | 25/08/06-05/09/06 | VLT (sm) | FORS2 | 3 | no | 1437+5737 | 19/07/07-23/07/07 | CAHA3.5 | TWIN | 4 | no |
|  | 05/10/07 | NTT | EMMI | 1 |  | $1439+5739$ | 20/07/07-22/07/07 | CAHA3.5 | TWIN | 2 | yes |
|  | 05/09/07 | WHT | ISIS | 1 |  | $1439+5741$ | 20/07/07-22/07/07 | CAHA3.5 | TWIN | 4 | no |
| 0249+3350 | 11/09/09 | CAHA3.5 | TWIN | 1 | no | 1504+3214 | 28/07/08-29/07/08 | WHT | ISIS | 2 | no |
| $0253+3352$ | 11/09/09 | CAHA3.5 | TWIN | 1 | no | 1524+5047 | 24/07/08-25/07/08 | CAHA3.5 | TWIN | 6 | \% |
| $0255+3528$ | 09/09/09 | CAHA3.5 | TWIN | 1 | no | $1558+2642$ | 11/06/08-01/07/08 | CAHA3.5 | TWIN | 29 | yes |
| 0301+0502 | 19/09/06-22/10/06 | VLT (sm) | FORS2 | 3 | yes | $1623+6306$ | 20/07/07-01/07/08 | CAHA3.5 | TWIN | 25 | yes |
|  | 05/10/07-08/10/07 | NTT | EMMI | 18 |  |  | 08/07/08-10/07/08 | WHT | ISIS | 4 |  |
| $0302+3721$ | 24/09/09-25/09/09 | CAHA3.5 | TWIN | 3 | no | 1625+6400 | 21/07/07-22/07/07 | CAHA3.5 | TWIN | 2 | yes |
| $0307+3848$ | 13/09/09-25/09/09 | CAHA3.5 | TWIN | 24 | yes |  | 07/07/08-10/07/08 | WHT | ISIS | 10 |  |
| $0309+4110$ | 10/09/09 | CAHA3.5 | TWIN | 1 | no | 1635+6201 | 20/07/07-24/07/07 | CAHA3.5 | TWIN | 6 | yes |
| $0318+4230$ | 10/09/09 | CAHA3.5 | TWIN | 1 | no | 1654+1310 | 24/07/08-25/07/08 | CAHA3.5 | TWIN | 4 | 崖 |
| 0320+0442 | 22/10/06-24/10/06 | VLT (sm) | FORS2 | 2 | no | $1725+6329$ | 12/09/09 | CAHA3.5 | TWIN | 1 | no |
| 0420+0649 | 19/10/08-22/10/08 | CAHA3.5 | TWIN | 17 | yes | 1731+0703 | 24/07/08-25/07/08 | CAHA3.5 | TWIN | 6 | no |
| 0830-0536 | 03/12/08-04/12/08 | M-Clay | LDSS3 | 5 | no | $1833+6431$ | 25/07/08-26/07/08 | CAHA3.5 | TWIN | 4 | no |
|  | 06/12/08-07/12/08 | M-Baade | IMACS | 5 |  | $1834+4137$ | 09/09/09 | CAHA3.5 | TWIN | 1 | no |
| 0848+0501 | 24/10/07-26/10/07 | VLT (sm) | FORS2 | 2 | no | 1844+4108 | 09/09/09-12/09/09 | CAHA3.5 | TWIN | 3 | no |
| $0852+1154$ | 03/12/08 | M-Clay | LDSS3 | 1 | no | 1844+4120 | 14/06/08-01/07/08 | CAHA3. 5 | TWIN | 14 | yes |
| 0852+0713 | 12/11/07-13/11/07 | VLT (sm) | FORS2 | 2 | no |  | 06/07/08-10/07/08 | WHT | ISIS | 7 |  |
| 0853+0720 | 12/11/07-13/11/07 | VLT (sm) | FORS2 | 2 | yes | 1919+3703 | 24/07/08-25/07/08 | CAHA3.5 | TWIN | 4 | no |
|  | 03/12/08-04/12/08 | M-Clay | LDSS3 | 8 |  | $1923+6203$ | 10/09/09 | CAHA3.5 | TWIN | 1 | no |
|  | 06/12/08 | M-Baade | IMACS | 4 |  | 2012+6017 | 09/09/09 | CAHA3.5 | TWIN | 1 | no |
| 1055+4729 | 01/05/09-05/05/09 | CAHA3.5 | TWIN | 6 | yes | 2046+0218 | 27/07/08 | CAHA3.5 | TWIN | 3 | no |
| $1105+2824$ | 23/03/09-25/03/09 | NTT | EMMI | 2 | no | $2213+0722$ | 09/09/09 | CAHA3.5 | TWIN | 1 | no |
| $1105+3851$ | 02/05/09-05/05/09 | CAHA3.5 | TWIN | 16 | yes | $2228+3912$ | 25/07/08-27/07/08 | CAHA3.5 | TWIN | 7 | о |
| 1114+0838 | 25/12/07-26/12/07 | VLT (sm) | FORS2 | 2 | no | $2243+3122$ | 22/10/08 | CAHA3.5 | TWIN | 3 | yes |
| 1114+0924 | 15/04/07-17/04/07 | VLT (sm) | FORS2 | 2 | yes |  | 09/09/09/10/09/09 | CAHA3.5 | TWIN | 12 |  |
|  | 25/12/07-26/12/07 | VLT (sm) | FORS2 | 2 |  | 2257+0745 | 21/07/07-23/07/07 | CAHA3.5 | TWIN |  | no |
| 1138-0011 | 15/04/07-17/04/07 | VLT (sm) | FORS2 | 2 | no |  | 14/10/07-17/10/07 | VLT (sm) | FORS2 | 2 |  |
|  | 17/05/07-19/05/07 | M-Clay | LDSS3 | 6 |  |  | 09/08/08-10/08/08 | GEMINI-S | GMOS | 2 |  |
|  | 19/06/07 | WHT | ISIS | 1 |  | $2258+0710$ | 21/07/07-23/07/07 | CAHA3.5 | TWIN | 4 | yes |
| 1239+0055 | 08/04/07-10/04/07 | VLT (sm) | FORS2 | 2 | no |  | 17/10/07-18/10/07 | VLT (sm) | FORS2 | 2 |  |
| 1242-0853 | 06/01/08-08/01/08 | VLT (sm) | FORS2 | 2 | no |  | 09/08/08-06/11/08 | GEMINI-S | GMOS | 2 |  |
| 1243-0647 | 06/01/08-09/01/08 | VLT (sm) | FORS2 | 2 | no | $2308+2240$ | 20/07/07-23/07/07 | CAHA3.5 | TWIN | 3 | no |
| 1300+1908 | 01/05/09-05/05/09 | CAHA3.5 | TWIN | 16 | yes | $2311+2202$ | 21/07/07-28/07/08 | CAHA3.5 | TWIN | 29 | yes |
| 1347+2707 | 18/03/09-19/03/09 | NTT | EMMI | 2 | no | $2338+0744$ | 09/09/09 | CAHA3.5 | TWIN | 1 | no |
| 1348+1834 | 12/06/08-30/06/08 | CAHA3.5 | TWIN | 24 | yes | $2339+0744$ | 13/09/09 | CAHA3.5 | TWIN | 1 | no |
| Photometry Name (SDSS) | Date | Tel | Filter | $t_{\text {int }}$ | $N_{\text {frames }}$ | $\begin{aligned} & \text { Name } \\ & \text { (SDSS) } \end{aligned}$ | Date | Tel | Filter | $t_{\text {int }}$ | $N_{\text {frames }}$ |
| 0853+0720 | 18/05/07-21/05/07 | DuPont | r | 40 | 337 | $2243+3122$ | 15/08/09-19/08/09 | IAC80 | 1 | 240 | 397 |

were fitted to the phase folded radial velocity curves. Where $\gamma_{\mathrm{sec}}$ is the systemic velocity of the secondary star, $t_{0}$ corresponds to the zero point defined by the inferior conjunction of the secondary star and with $v_{r}=\gamma_{\text {sec }}, K_{\text {sec }}$ the radial velocity amplitude of the secondary star and $P_{i}$ $(i=1,2, \ldots)$ are the trial periods picked from the periodogram. In Fig. 4.4 we show two examples of the periodograms with the highest peak marked and with the associated sine fits to the RVs. We accept the orbital period from the best fit solution, corresponding to a minimum chi-square value, which was always coinciding with the highest peak in the periodogram. Radial velocity curves are presented in Fig. 4.2. We derived the orbital period of 15 PCEBs, their spectra are shown in Fig. 4.2.1 and their stellar parameters given in Table 3.3. The orbital periods were always below the upper limits estimated in Chapter 3. The orbital periods of the 15 systems

Table 4.3: Orbital period, amplitude of the secondary's radial velocity, systemic velocity with errors included in parenthesis, estimated primary's radial velocity amplitude, limits for the orbital inclination, orbital separation and minimum filling factor of the secondary star $\left(f_{\min }\right)$. For those systems where no mass of the white dwarf is known we assumed an $0.6 \mathrm{M}_{\odot}$ white dwarf.

| Name | $P_{\text {orb }}$ <br> $($ days $)$ | $K_{\text {sec }}$ <br> $(\mathrm{km} / \mathrm{s})$ | $\gamma_{\text {sec }}$ <br> $(\mathrm{km} / \mathrm{s})$ | $K_{\text {WD }}$ <br> $(\mathrm{km} / \mathrm{s})$ | i <br> $(\mathrm{deg})$ | a <br> $\left(\mathrm{R}_{\odot}\right)$ | $f_{\text {min }}$ <br> $\left(\frac{R_{\text {sec }}}{R_{\text {lob }}}\right)$ |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| SDSS0301+0502 | $0.540(9)$ | $175(3)$ | $13(2)$ | 62 | $52-68$ | $3.0 \pm 0.2$ | 0.32 |
| SDSS0307+3848 | $0.430(8)$ | $147(2)$ | $-9(1)$ | 93 | $51-74$ | $2.4 \pm 0.2$ | 0.36 |
| SDSS0420+0649 | $0.203(1)$ | $156(3)$ | $47(2)$ | 66 | $36-46$ | $1.4 \pm 0.1$ | 0.45 |
| SDSS0853+0720 | $0.150(1)$ | $221(7)$ | $-8(6)$ | 139 | $56-90$ | $1.2 \pm 0.1$ | 0.70 |
| SDSS1105+3851 | $0.344(4)$ | $152(2)$ | $-9(2)$ | 81 | $44-54$ | $2.1 \pm 0.1$ | 0.46 |
| SDSS1300+1908 | $0.308(3)$ | $142(3)$ | $-14(2)$ | 41 | $28-35$ | $2.2 \pm 0.2$ | 0.50 |
| SDSS1348+1834 | $0.2483(4)$ | $222(3)$ | $-21(2)$ | 120 | $\sim 90$ | $1.6 \pm 0.1$ | 0.50 |
| SDSS1429+5759 | $0.545(1)$ | $147(8)$ | $-12(5)$ | 53 | $39-49$ | $3.2 \pm 0.2$ | 0.38 |
| SDSS1436+5741 | $0.864(3)$ | $119(2)$ | $-16(2)$ | 75 | $53-78$ | $3.8 \pm 0.3$ | 0.23 |
| SDSS1558+2642 | $0.661(2)$ | $145(3)$ | $-10(2)$ | 43 | $38-53$ | $3.6 \pm 0.3$ | 0.27 |
| SDSS1623+6306 | $2.23(3)$ | $70(4)$ | $-9(3)$ | 22 | $28-36$ | $7.9 \pm 0.6$ | 0.13 |
| SDSS1625+6400 | $0.218(2)$ | $106(5)$ | $-10(4)$ | 26 | $20-25$ | $1.5 \pm 0.2$ | 0.36 |
| SDSS1844+4120 | $0.2255(3)$ | $148(4)$ | $-80(3)$ | 87 | $50-68$ | $1.3 \pm 0.2$ | 0.27 |
| SDSS2243+3122 | $0.11954(3)$ | $183(4)$ | $-21(3)$ | 77 | $35-45$ | $1.0 \pm 0.1$ | 0.65 |
| SDSS2311+2202 | $0.580(2)$ | $116(3)$ | $-1(2)$ | 38 | $29-35$ | $3.4 \pm 0.2$ | 0.39 |

range from 2.86 to 53.52 hours, values are given in Table 4.3 together with $K_{\text {sec }}$ and $\gamma_{\text {sec }}$. Their orbital period distribution is discussed in Sect. 4.3.1. The number of spectra needed to determine the orbital period varied from 15 to 36 , and in general the longer the orbital period the more spectra are required.

## Orbital inclinations

From the masses of the white dwarfs, including their errors we calculated the range of possible orbital inclinations, combining the mass function and Kepler's third law:

$$
\begin{equation*}
\sin i=\left(M_{\mathrm{wd}}+M_{\mathrm{sec}}\right)^{2 / 3} \frac{K_{\mathrm{sec}}}{M_{\mathrm{wd}}}\left(\frac{P_{\mathrm{orb}}}{2 \pi G}\right)^{1 / 3} \tag{4.2}
\end{equation*}
$$

For those systems for which we do not have the mass of the primary star we assumed a white dwarf of mass of $0.6 \mathrm{M}_{\odot}$. We give these values in Table 4.3 together with the radial velocity amplitude of the secondary stars and the systemic velocities. Note that system SDSS1348+1834 is a strong candidate for being an eclipsing binary and photometry should be done to confirm.


Figure 4.1: SDSS spectra of the 15 systems with orbital period measurement.


Figure 4.2: Phase folded radial velocities curves and sine fits to the data (dotted lines).


Figure 4.3: Radial velocity curve for SDSS0420+0649 as measured from the $\mathrm{H} \alpha$ emission line (squares) and from the Na absorption doublet in the SDSS-subspectra.

## Estimates of orbital separation, $K_{\mathrm{WD}}$ and $R_{\mathrm{lob}}$

Using Eggleton's equation (Eggleton 1983) for the radius of the Roche lobe, given in equation 4.3 we derived the minimum filling factors of the secondary star for those systems. We estimated the radius of the secondary star using the empirical radius-spectral type relation given by Rebassa-Mansergas et al. (2007). An error of spectral type of one subclass would imply in mean an error on the radius of $\sim 0.05 R_{\odot}$, so we assumed an error of $0.05 R_{\odot}$ for estimating the minimum filling factor.

$$
\begin{equation*}
R_{\mathrm{lob}}=\frac{a \cdot 0.49 \cdot q^{2 / 3}}{0.6 \cdot q^{2 / 3}+\log \left(1+q^{1 / 3}\right)} \tag{4.3}
\end{equation*}
$$

Using Kepler's third law we derived the orbital separation and, finally we estimated the amplitude of the radial velocity for the primary star using: $K_{\mathrm{WD}}=K_{\mathrm{sec}} \frac{M_{\text {sec }}}{M_{\mathrm{wd}}}$. For those cases where we have no estimate of the mass of the white dwarf we used the standard value of $0.6 \mathrm{M}_{\odot}$. We give these values in Table 4.3.

## On the nature of SDSSO420+0649

For SDSSO420+0649 we could measure the RVs from the Na doublet and of the $\mathrm{H} \alpha$ emission line. In Fig. 4.3 we show the measured RVs from the SDSS-sub-spectra, where we plot RV(Na) with circles and $\mathrm{RV}(\mathrm{H} \alpha)$ with squares. SDSS0420+0649 has on one hand the velocity coming from the $\mathrm{H} \alpha$ line anti-correlated with the one from the Na doublet. The anti-correlation is not perfect, but has a shift of round 0.1 in orbital phase. The amplitude of the $\mathrm{RV}(\mathrm{Na})$ curve is 156 $\mathrm{km} / \mathrm{s}$, while for $\mathrm{RV}(\mathrm{H} \alpha)$ it is $33 \mathrm{~km} / \mathrm{s}$. On the other hand the $\mathrm{H} \alpha \mathrm{EW}>20 \AA$ suggesting a CV nature of the system. If the binary has a disk this behavior would be explained (Thorstensen et al. 2009).


Figure 4.4: Calculated periodogram from using the spectroscopic data, radial velocity and photometric light curves for SDSS0853+0720 phase folded with the orbital period corresponding to the highest peak in the periodogram, $P_{\text {orb }}=0.1503$ days.


Figure 4.5: Periodogram calculated using the photometric data, radial velocity and photometric light curves for SDSS2243+3122 phase folded with the orbital period corresponding to the highest peak in the periodogram, $P_{\text {orb }}=0.11954$ days.

### 4.2.2 Orbital periods from photometric observations

SDSS0853+0720 was observed with the Du Pont telescope for three consecutive nights (see details in Sec. 4.1) in the $r$ band. We estimated the orbital period computing a periodogram (see section ). A phase folded light curve using the photometric period, $P_{\text {orb }}=3.6$ hours, is presented in Fig. 4.4, together with the ort periodogram (upper panel) and the radial velocity curve phase folded over the same orbital period (middle panel). The light curve shows two uneven maxima at phases 0.25 and 0.75 , being the first maximum, $\phi=0.25$, brighter than the second one, and equal minima at phases 0 and 0.5 . The maximum variation is almost 0.2 magnitudes in the $r$ band. Ellipsoidal modulation might be the cause of such a variability, although one would expect to have equal maxima, spots in one of the hemispheres of the secondary star could explain the uneven maxima (O’Connell effect, see Liu \& Yang 2003). We explored the activity on the secondary star by measuring the equivalent width of the $\mathrm{H} \alpha$ line. The obtained value, $\mathrm{EW}=1.3$ $\AA$, is at the lower end of the activity scale, which might contradict the hypothesis just mentioned.

Photometry in the $i$ band was obtained for SDSS2243+3122 for four nights. We estimated the orbital period, by computing a periodogram, to be $P_{\text {orb }}=2.86$ hours (upper panel of Fig. 4.5). The


Figure 4.6: Differential photometry in the $i$ band obtained for SDSS2243+2122 the 15th August 2009. A flare of $\sim 25$ minutes length with a relative enhancement of $\sim 0.4$ magnitudes was observed.
radial velocity curve phase folded with the photometric orbital period is shown in the upper panel of Fig. 4.5. Using the photometric period we could put the spectroscopic observations in phase obtained 25 days ( 208 binary cycles) later without cycle count ambiguity. We combined the epochs of the spectrocopic phase zero and the photometric minimum to obtain a final estimate of the orbital period of $P_{\text {orb }}=0.11954 \pm 0.00003$ days. In the bottom panel we show the light curve. As for SDSS0853+0720 uneven consecutive maxima and two equal minima are observed, but in this case the brightest maximum is observed at $\phi=0.75$ (see Fig. 4.5). The variability in the light curve presents a maximum difference of 0.2 mag in the $i$ band and it's nature might be due to ellipsoidal modulation. The night of the 15th of August 2009 a flare with $\sim 25$ minutes length in the decay, and rising $\Delta r$ by 0.35 mag., was observed (see Fig. 4.6), which would strengthen the argument of magnetic activity being the cause of the disparity in the maxima. Although, the origin of the O'Connell effect might be a mix of different phenomena, such as spots and capture of circumstellar material (Liu \& Yang 2003). With its $P_{\text {orb }}=2.86$ hours the system in located in the CV orbital period gap. The probability of this system to be a detached CV, that has relaxed to it's equilibrium, instead of being a detached system in which the secondary star has never filled it's Roche lobe is between $4-13$ to 1 according to Davis et al. (2008), where the assumed prescription for MB is as given by Hurley et al. (2002) and the efficiency of the CE phase is taken from the numerical calculations from Iben \& Livio (1993), $\alpha_{C E}=0.13-0.6$. There are just two other systems with similar properties, HS2237+8154 (Gänsicke et al. 2004) and SDSS0052-0053 (Rebassa-Mansergas et al. 2008), but this is the only one in which a flare has been detected so far.

The minimum filling factors calculated in Sect. 4.2 .2 are 0.6 and 0.49 for SDSS0853+0720 and SDSS2243+3122 respectively. It is worth mentioning that both systems have the largest minimum filling factors among the 15 systems.


Figure 4.7: Orbital period distribution in days (the upper panel is in logarithmic scale to highlight the absence of systems with longer orbital periods than one day. The plot includes all the known PCEBs listed in Ritter \& Kolb (2003) (version v7.12 from 2009) that containing a white dwarf plus a main sequence and the 15 new systems ( 69 PCEBs in total) for which we give the orbital period in this study marked in the plots and over-plotted in black.

### 4.3 Discussion

### 4.3.1 The PCEB orbital period distribution

In Fig. 4.7 we show the orbital period distribution of all the known PCEB from (Ritter \& Kolb 2003) containing a white dwarf plus a main sequence and include the 15 new systems ( 69 PCEBs in total). We show the distribution on a linear and a logarithmic scale. The former to show the continously decreasing number of systems towards longer periods and the latter to be able to
compare with past representations. The upper panel shows that the orbital period distribution is flat, dropping dramatically around 1 day. A long tail towards longer orbital periods which extends up to 100 days is predicted by Willems \& Kolb (2004), which might indicate that the amount of angular momentum extracted from the orbit during the CE phase is higher than predicted, bringing the systems closer. Nevertheless care must be taken with possible biases. This orbital period distribution contains all the systems known until the date and investigating the biases on the detection of these becomes an almost impossible task. In Chapter 3 we investigated the limits of our criterium to detect systems at long orbital periods and we saw that we should be able to detect longer orbital periods than a day (see discussion in the previous chapter). But, one thing is being able to detect a system and another is to measure it's orbital period. As can be seen in the lower panel of Fig. 4.7, the number of systems decreases with the orbital period in a continuous way, reflecting on one hand the fact that it is easier to measure short orbital periods since they are less time demanding and on the other hand also an accumulation of systems at short orbital periods due to their high $K_{\text {sec }}$. The positions of the orbital period of our 15 systems is marked in the figure and plotted in black, we see there that among them only 1 system has a period longer than 1 day. We now investigate the remaining PCEBs presented in Chapter 3 for which we haven't measured the orbital periods to see whether there are long orbital period systems.

### 4.3.2 Long orbital period candidates

In Chapter 3 we identified 37 systems as PCEB. We measured the orbital period of 15 of these systems. Among the remaining 22 systems without $P_{\text {orb }}$ measured we calculated upper limits for 16 of them (Chapter 3, Sect. 3.4.2). We found that 5 have $P_{\text {orb }}<1$ day: SDSS0239+2736, SDSS1021 +1744 , SDSS1028 +0931 , SDSS1135 +0103 and SDSS15245040. We investigated the long orbital period candidates as well as those for which we did not give upper limits on the $P_{\text {orb }}$ in more detail since they are of most interest for our purpose. We inspected in a case by case the radial velocity variations for these systems (see Fig. 4.8).

- SDSS0734+4105 varies ~ $110 \mathrm{~km} / \mathrm{s}$, SDSS0753+1754 varies $\sim 190 \mathrm{~km} / \mathrm{s}$ and SDSS1114+0924 varies $\sim 220 \mathrm{~km} / \mathrm{s}$, in less than 2 hours, SDSS1047+4835 varies $\sim 80 \mathrm{~km} / \mathrm{s}$, in less than 30 minutes, implying that these systems must have an orbital period shorter than 1 day.
- SDSS1024+1624 was observed two consecutive nights. The first day the maxima of the radial velocity was covered, and the second day, $\sim 25$ hours later, almost the same phase was re-observed, implying a maximum of two cycles per day.
- SDSS1055+4729 was observed two consecutive nights, covering the minima in the first night and somewhere close to the maxima in the second night, making the system a good candidate for having a longer orbital period than a day, close to 2 days.
- SDSS1123-1155 was observed three different nights. The first night it almost did not vary, but the time span between the first spectrum and the last in night 1 was 45 minutes,
and it looks like being around the minimum, where variations in the radial velocity are slower. The second night, three days later, one spectrum was taken and the same phase was covered, so the maxima of the orbital period is 3 days. Nevertheless two more spectra were taken a day later and they vary around $30 \mathrm{~km} / \mathrm{s}$ in less than 30 minutes, so it could be that the period is rather short.
- SDSS1635+6201 was observed 6 nights. There are 11 spectra and they all show rather small velocity, so it is a candidate for having a long orbital period.

There are 3 systems for which we derived upper limits on the orbital period based on the RV from the $\mathrm{H} \alpha$ emission line. We look into their RV with more detail, and show the RVs in Fig. 4.8.

- SDSS0142-0835 was observed 7 different nights, spread over 34 days. Radial velocities variation are rather small, making it a good candidate for having long $P_{\text {orb }}$.
- SDSS1320+6612 varied $\sim 100 \mathrm{~km} / \mathrm{s}$ in less than 1 hour during the second night that it was observed, so once more this system might have a short orbital period.
- SDSS1724+0733 observed 2 different nights, varied only $\sim 40 \mathrm{~km} / \mathrm{s}$ in $\sim 1.5$ hours. It is difficult to draw any strong conclusion on this specific system.

We finally inspect the radial velocities of the remaining 6 systems, for which we have no mass estimate of the primary star.

- SDSS0722 +3859 was observed in 2 consecutive nights. We could measure the radial velocities only from the $\mathrm{H} \alpha$ emission line and it varies $\sim 250 \mathrm{~km} / \mathrm{s}$, covering what could be the minimum and the maximum, over $\sim 4.5$ hours in the first night, so it has a short orbital period.
- SDSS0730+4054 and SDSS1919+6214 vary both $\sim 160 \mathrm{~km} / \mathrm{s}$ in $\sim 2$ and $\sim 3$ hours respectively, so they must have a rather short orbital period. RVs of SDSS0730+4054 show a clearly sinusoidal trend, of what could be, if the systemic velocity of the secondary star is close to $0 \mathrm{~km} / \mathrm{s}$, a fourth of a cycle, implying a $P_{\text {orb }}$ close to 9 hours.
- SDSS1316-0037 was observed three consecutive nights, the first and the third night approximately the same radial velocity was observed, hence the system has $P_{\text {orb }}<2$ day. During 1 hour it varied $100 \mathrm{~km} / \mathrm{s}$ so it has rather short orbital period.
- For SDSS1437+5737 there are two spectra taken during the same night and spread over less than 30 minutes, so we cannot learn much from the sub-exposures of the SDSS. We confirmed its PCEB nature from own observations and they point that it might be long orbital period systems. SDSS2258+0710 was also identified from own observations as a PCEB, and since the time spread between them is very long it is difficult to learn more than saying that it might be a long orbital period as well. We don't show the RVs from the sub-spectra for these two systems.


Figure 4.8: From left to right and from top to bottom: 1) Radial velocities from the SDSS sub-spectra for 8 long orbital period candidates. Inspecting their radial velocity variation in time we see that only 3 systems, SDSS $1055+4729$, SDSS $1123-1155$ and SDSS1635+6201 can have $P_{\text {orb }}>1$ day; 2) Radial velocities from the $\mathrm{H} \alpha$ emission line of the SDSS sub-spectra for 4 systems, among which only SDSS 1724+0733 can have a long orbital period; 3) Radial velocities from the SDSS sub-spectra for 3 systems for which we have no estimate of the mass of the primary star and no maximum $P_{\text {orb }}$ was given. Their RV variation indicates they have short orbital period.

Table 4.4: Maximum orbital period.

| System (SDSS) | $P_{\text {orb }}{ }^{\max }$ (days) | System (SDSS) | $P_{\text {orb }}{ }^{\max }$ (days) |
| :---: | ---: | :---: | ---: |
| SDSS0142-0835 | 121 | SDSS1114+0924 | 1 |
| SDSS0239+2736 | 0.784 | SDSS1123-1155 | 3 |
| SDSS0722+3859 | 1 | SDSS1135+0103 | 0.269 |
| SDSS0730+4054 | 1 | SDSS1316-0037 | 1 |
| SDSS0734+4105 | 1 | SDSS1320+6612 | 1 |
| SDSS0753+1754 | 1 | SDSS1437+5737 | $P_{\text {orb }}>1$ |
| SDSS1021+1744 | 0.571 | SDSS1524+5040 | 1.082 |
| SDSS1024+1624 | 1 | SDSS1635+6201 | 11 |
| SDSS1028+0931 | 0.891 | SDSS1724+0733 | 114 |
| SDSS1047+4835 | 1 | SDSS1919+6214 | 1 |
| SDSS1055+4729 | 2 | SDSS2258+0710 | $P_{\text {orb }}>1$ |

To sum up, we have that among 37 PCEBs, 29 systems have $P_{\text {orb }}<1$ day, and 8 systems could have $P_{\text {orb }}>1$ day (only 1 confirmed). We list the maximum periods of the 22 systems without $P_{\text {orb }}$ measure in Table 4.4. To constrain the CE efficiency it is necessary to observe these systems and measure their true orbital period. If the CE phase is very efficient (small values of $\alpha_{C E}$ ) extracting energy and angular momentum from the orbit then we would expect less systems at short orbital periods (Politano \& Weiler 2007). The orbital period distribution of WDMS binaries predicted from Willems \& Kolb (2004) consists of two different kind of populations: a large fraction of the systems, $\sim 75 \%$, which have very long orbital periods and have never gone through a CE phase; and a smaller fraction, $\sim 25 \%$, of systems which have gone through a CE phase. The later distribute peaking around 1 day and with a long tail towards up to 100 days.

Davis et al. (2009) calculated the present day population of PCEBs for different values of the CE efficiency parameter $\alpha_{C E}$ and compared their orbital period distribution with that one of known PCEBs until 2009 for a range of secondary masses (see Fig. 4.9). They find that the best solution that fits the data has a distribution with an initial mass ratio on the form $n\left(q_{i}\right)=q_{i}^{-0.99}$. They predict a smooth decline of systems towards longer orbital periods (red lines) in contrast with the sharp observed cut at 1 day (gray histograms). Systems with later spectral types secondaries have shorter orbital periods. Since the discovery of WDMS binaries has been biased towards systems with late spectral types secondaries this implies that the orbital period distribution is biased towards short orbital periods. Davis et al. (2009) corrected for the detection biases (green lines), and even though the observed and the predicted distributions are in a better agreement, a KS test over the CDF gives a better result, 0.35 versus 0.11 (see right panels of the same figure), the predicted tail towards long orbital periods is still present. We contribute with new 15 PCEBs spread from M3 to M6 in the secondary spectral type, corresponding to a mass range of $0.196-0.380 \mathrm{M}_{\odot}$ according to the spectral type-mass relation from Rebassa-Mansergas et al. (2007). All but one have shorter orbital period than a day, so that we can not reconcile observations and predictions yet. This highlights the relevance of measuring the $P_{\text {orb }}$ of the 7 new long orbital period candidates.


Figure 4.9: Orbital period distribution of PCEBs from Davis et al. (2009). The gray histograms show the known PCEBs until 2009, for 3 different ranges in the secondary mass. The red line shows the calculated distribution of the intrinsic population $\left(n\left(q_{i}\right)=q_{i}^{-0.99}\right.$, model A where $\left.\alpha_{C E}=1.0\right)$ and the green is the same but taking into account the detection probability. The right panels show the CDF with the KS significance level ( $\sigma_{K S}$ ) indicated. Figure was taken from Davis et al. (2009).

### 4.3.3 The white dwarf mass distribution of PCEBs

In order to investigate the white dwarf masses of PCEBs we select systems which have $T_{\text {eff }}>$ 12000 K and relative error lower than $25 \%$, so that its spectroscopic masses are reliable Kepler et al. (2007). After this strong filtering we end up with only 11 PCEBs from our initial sample of 37. We investigated the white dwarf masses of other systems and include 45 systems given in the cataloge from Ritter \& Kolb (2003) (see Table 1.2.2).

The $M_{\mathrm{wd}}$ distribution (see Fig. 4.10) has a mean mass of $0.617 \pm 0.165$, and presents two peaks. Although the number of PCEB is very small in order to contrain their positions with enough accuracy one is located around $0.58 \mathrm{M}_{\odot}$ and the second at $0.85 \mathrm{M}_{\odot}$. Both peaks are
present in field WDs being the later weaker in single WDs (Liebert et al. 2005). The distribution has a more pronounced tail towards lower masses than the found for our wide WDMS sample. It is thought that all WDs with $M_{\mathrm{wd}}<0.47 \mathrm{M}_{\odot}$ are product of binary evolution Marsh et al. (1995) (see Chapter 1). Single stars would need more time than the age of the Galaxy to achieve this stage, while if being member of a close binary, a common envelope phase achieved during the red giant branch would allow the star to loose it's envelope, becoming a white dwarf with He in it's core. We have 6 systems with $M_{w d}<0.47 \mathrm{M}_{\odot}$ which did not show any significant radial velocity in our analysis, SDSS0111+0009, SDSS0852+1154, SDSS0944+6143, SDSS1235+0030, SDSS1239+0055 and SDSS1241+6007, but as shown in Fig. 3.9 the lower the mass of the primary star the less sensitive we are with our detection criterium, so it could be that they are indeed close binaries and these systems should be reobserved.


Figure 4.10: Distribution of white dwarf's mass for all the known PCEB binaries that contain a DA as primary from Ritter \& Kolb (2003) and the PCEBs from this work.

### 4.4 Summary

We have determined the orbital periods of 15 sytems, and only one of them has an orbital period longer than one day. The orbital period distribution of all the known PCEBs apparently presents a sharp cut at around one day. This seems to contradict the distribution predicted by Willems \& Kolb (2004) and Davis et al. (2009), which contains an extended tail of systems with orbital period up to 100 days. This could imply that the CE phase might extract more energy and angular momentum than previously thought. But one must notice that the actual period distribution is biased towards short orbital periods, since their measurement is less time demanding than
for those with longer orbital periods and since the secondaries are also biased towards late spectral types. Investigating in more detail the remaining 22 PCEBs that were identified in Chapter 3 for which we don't have a measurement of the orbital period we have identified 7 long orbital period ( $>1$ day) candidates and 15 short orbital period ( $<1$ day) candidates. To learn about the efficiency of the CE phase it is very important to measure their true orbital period. The white dwarf mass distibution of PCEBs is similar to that of field white dwards, presenting two peaks, one around $0.58 \mathrm{M}_{\odot}$ and the other around $0.84 \mathrm{M}_{\odot}$. It has an extended tail towards low masses, in agreement with the idea of all He core white dwarfs ( $M_{\mathrm{wd}}<0.47 \mathrm{M}_{\odot}$ ) being product of a common envelope phase. We have 6 WDMS with lower mass than this limit, making them good candidates for being close binary systems, this systems should be reobserved to proof their close binary nature.

## Chapter 5

## Activity binarity relation


#### Abstract

We study the influence of binarity in the stellar activity of the secondary stars, measuring the equivalent width of the $\mathrm{H} \alpha$ emission line originating from the chromosphere of the red dwarf. We would like to know if the fast rotating secondaries in PCEBs harbor stronger magnetic fields than their slow-rotating counterparts and if so, whether we can make use of magnetic activity to single out the PCEBs among a sample of WDMS binaries. We find that the fraction of active stars increases with the spectral type, a result found for single field red dwarfs as well, though we find a higher fraction at earlier spectral types. This result can be explained by the age of the systems. We find that the majority of the PCEBs contain active secondaries, and at a given spectral type the $\mathrm{EW}(\mathrm{H} \alpha)$ is higher than for wide WDMS binaries. We also investigate the relation between the estimated distances, $d_{\mathrm{sec}}$ and $d_{\mathrm{wd}}$, and the activity as a possible cause for the previously found mismatch.


### 5.1 Introduction

Chromospheric magnetic activity, can be measured from CaII H and K for spectral types G and K. Since $M$ stars have very little flux in the blue, their spectral energy distribution dominates at longer wavelengths than $6500 \AA$, it becomes more difficult to analyze activity from these lines. In active G stars there is a correlation between the fluxes from CaII H and K lines and the emission which fills in the $\mathrm{H} \alpha$ absorption line (Stauffer \& Hartmann 1986), making $\mathrm{H} \alpha$ a better activity indicator for later spectral types. Early models of M stars have shown that the photospheric $\mathrm{H} \alpha$ absorption line is very weak due to their low temperatures, but the chromosphere can produce a prominent $\mathrm{H} \alpha$ line, which can be in absorption or in emission (Cram \& Mullan 1979, 1985). Stauffer \& Hartmann (1986) studied a sample of M stars, they measured H $\alpha$ EW and used broad band photometry to separate between different activity levels. They find that redder objects have higher EW and claim that the stronger the absorption the weaker the activity. Recently, Walkowicz \& Hawley (2009) studied a sample of 81 close dM3 stars. They took intermediate and high resolution spectra covering simultaneously the CaII H and K lines and the $\mathrm{H} \alpha$ line to
allow comparison of both elements at the same time. They restricted their sample to M3 stars to remove a dependence with the spectral type and choose M3 since it is at the boundary of being total convective ( $\sim 0.35 \mathrm{M}_{\odot}$ ). From spectra of intermediate resolution ( $\mathrm{R} \sim 2000$ ) they found that for weak and intermediate activity ( $\mathrm{EW}(\mathrm{CaII} \mathrm{K})<2 \AA$ ), there is no correlation between CaII K line (CaII H is normally not used since it is blended with $\mathrm{H} \epsilon$ ) and the emission of $\mathrm{H} \alpha$ while for stars with strong activity one observes a positive correlation, a monotonic increase with the CaII K EW. They find that weak active stars can have $\mathrm{H} \alpha$ in absorption and that to distinguish between inactive and weak active stars high resolution spectroscopy is needed. When using $\mathrm{H} \alpha$ emission as an activity indicator one has to be cautious and keep in mind that it will only give a lower limit to the total number of dM active stars.

The fraction of field M stars with $\mathrm{H} \alpha$ in emission increases with the spectral type (Hawley et al. 1996). Based on a study on 7840 single $M$ stars, West et al. (2004) found that the fraction of active stars is very small for early stars, has a steep increase in the range M3-M5 and, reaches a maximum around M7. They also find a correlation between activity and distance to the Galactic plane: stars closer to the plane would be younger and therefore they would be active. From a later study, based on a very large sample of dM spectra from the SDSS-DR5, West et al. (2008) found similar results, but with a more pronounced enhancement at $\mathrm{Sp} 2=\mathrm{M} 5$, where $\sim 60 \%$ of the systems are active. As before they find that for a given spectral type the activity fraction decreases with the distance to the Galactic plane and by comparison with 1D dynamical models conclude that this effect can be explained with a dynamically heated disk and a dependence of the activity lifetime with the spectral type. They conclude that the activity lifetime is longer for later spectral types, varying from 1.8 Gyr for M0 to 8.0 Gyr for M7 and with a very steep increase at the boundary where stars become completely convective, between M3-M5, which they interpret as a different physical mechanism responsible for the magnetic field.

Activity is expected to be enhanced in stars when being members of a close binary system. Due to tidal forces, they would be forced to rotate faster than single stars of the same age, enhancing activity. Several studies have been carried out in this direction. Basri (1987) found that the activity does not change when a star is a member of a binary system. Strassmeier et al. (1990) found that while activity in main sequence binary stars show higher levels of activity than single stars (rotation is faster due to tidal forces), evolved systems show no obvious difference. The components of wide binary systems have never interacted, therefore the secondary stars should be comparable with single stars. We investigate the activity and compare the results between wide binaries and PCEBs.

### 5.2 Analysis

We have studied the activity in our WDMS binaries by measuring the EW of the $\mathrm{H} \alpha$ line. To get a true continuum for the red dwarf we subtracted the contribution of the white dwarf from the SDSS spectrum. We used the white dwarf that best fitted the SDSS WDMS spectrum (see chapter 2). We measured the equivalent width of $\mathrm{H} \alpha$ selecting interactively the emission region. For systems


Figure 5.1: The spectrum of SDSSJ030138.24+050218.9 (black) with the best fitted white dwarf (blue) and the residual rew dwarf (red). A zoom into the $\mathrm{H} \alpha$ emission line is plotted in the right panel, with the selected region for measuring the EW plotted with vertical lines, and the underlying continuum is also shown.
with no obvious emission we chose the range 6556-6570 $\AA$. We assumed a continuum level of constant slope defined by the median flux in two neighboring regions around $\mathrm{H} \alpha$ of $11 \AA$ in size (see Fig. 5.1). We consider active those stars with EW > $1 \AA$ for comparison with previous studies.

### 5.3 Fraction of active stars

The fraction of active stars for wide and for close binaries is shown in the two upper panels in Fig. 5.2. We find that among 278 WDMS ( $277 \mathrm{wdms}+1$ candidate), 144 are active. The fraction of active stars in PCEBs is $\sim 90 \%$, significantly higher than the fraction of active stars in wide binaries, which is $\sim 45 \%$.

In the upper left panel of Fig. 5.2 we plot the fraction of active stars for the wide WDMS, and plot the values obtained for field stars from West et al. (2008) with squares. The fraction of active stars is higher at earlier spectral types. For wide systems we find that the fraction of active stars is smaller at early spectral types, increases with the spectral type and reaches a maximum at M5 and M6. Although the general trend is consistent with results in field M stars (West et al. 2008), the fraction of dMe in the range $\mathrm{M} 0-\mathrm{M} 3$ is much higher, $40 \%$ versus $10 \%$. Our wide systems can be contaminated with PCEB by up to $\sim 12 \%$ (Willems \& Kolb 2004). Assuming this $12 \%$ of PCEB are distributed in spectral type according to our previous result (see 3.4.1), we don't expect to see more than $\sim 50 \%$ of them in that spectral type range. We have 185 wide WDMS with spectral type between M0-M3, so we would have less than 13 PCEB in our sample, being

WIDE



PCEB



Figure 5.2: Upper panels: fraction of active stars as a function of the secondary spectral type for WIDE (left) and for PCEB (right). On the upper left panels the fraction of active stars from field M stars from West et al. (2008) is plotted with squares for comparison. Lower left panel: mean $\mathrm{H} \alpha \mathrm{EW}$ as a function of spectral type ( Sp 2 ) for wide systems (dashed-dotted line) and for PCEBs (solid line). Right panel: Strength of magnetic activity (diamonds) for all the WDMS compared with dMe field stars from West et al. (2008).
the majority M3. To match the fraction of active stars with the one given by West et al. (2008), we would need a PCEB fraction of $\sim 57 \%$. In other words the "missing" PCEBs are not enough to explain the higher fraction of dMe. In Sect. 5.5 we investigated the age as a possible reason of such enhancement, finding that dMe in this spectral type range, are young systems, younger than the activity lifetime. Silvestri et al. (2005) studied the activity in a sample of wide WD+dM binaries. They found that $\sim 16 \%$ of the systems where active. The fraction, although higher

Table 5.1: Mean $\mathrm{EW}(\mathrm{H} \alpha)$ for wide and close dMe , with the number of stars in each spectral type bin given in parenthesys.

| $S p 2$ | $\mathrm{EW}_{\text {WIDE }}$ | $\mathrm{EW}_{\text {PCEB }}$ |
| :--- | :--- | :--- |
| M0 | $1.50(5)$ | - |
| M1 | $0.97(36)$ | $4.41(1)$ |
| M2 | $0.83(60)$ | - |
| M3 | $1.01(84)$ | $3.57(17)$ |
| M4 | $1.72(43)$ | $5.10(13)$ |
| M5 | $2.41(11)$ | $10.13(3)$ |
| M6 | $4.81(2)$ | $4.45(2)$ |

than for field M stars is still lower than our result. This discrepancy could be due to two reasons. They measure the equivalent width for the M stars without subtracting the white dwarf, deriving lower values since the continuum of the red dwarfs would be enhanced by the white dwarf's and in some cases the $\mathrm{H} \alpha$ could be even masked. On the other hand a large fraction of the systems they studied are older than 4 Gyr , and less active systems are expected.

In the left bottom panel of Fig. 5.2 we plot the mean EW as a function of spectral type for wide (dashed-dotted line) systems and for PCEBs (continuous line) (SDSS0420+0649 has been excluded since it might be a CV, see Sect. 4.2 .1 for details). We see that in both cases it increases towards later spectral type. That is due to decreasing photospheric luminosity with spectral type and not to an increase in the chromospheric activity (Stauffer \& Hartmann 1986). The lower the temperature the redder the object and the lower the contribution of the photosphere around $\mathrm{H} \alpha$ therefore, the higher the contrast with an emission in $\mathrm{H} \alpha$, which means an increase of the EW. At each spectral type there is a scatter in the EW which seems to increase with the spectral type. This spread can reflect different rotation levels at each spectral type, which can be an age effect (young objects rotate faster) or be associated with the orbital period of the PCEBs. In Sect. 5.5 we study the ages and their relation with the activity in detail.

We give the mean $\mathrm{EW}(\mathrm{H} \alpha)$ for PCEBs and wide systems in table 5.1. We include the number of systems used to compute the mean at each spectral bin in parenthesis. Although the number of objects is small in order to draw any strong conclusion, the mean $\mathrm{EW}(\mathrm{H} \alpha)$ is higher for PCEBs than for wide binaries at every spectral type in agreement with the idea exposed at the beginning of the section.

### 5.4 Activity strength

The strength of magnetic activity can be quantified using the ratio between the luminosity in $\mathrm{H} \alpha$ and the bolometric luminosity, $\chi_{\mathrm{H} \alpha}=\mathrm{L}_{\mathrm{H} \alpha} / \mathrm{L}_{\text {bol }}$. This value can be inferred by multiplying the EW of $\mathrm{H} \alpha$ by the ratio of the flux in the continuum around $\mathrm{H} \alpha$ to the bolometric flux,


Figure 5.3: Age of the systems as a function of the spectral type of the secondary star. Active systems are plotted with filled diamonds, while inactive systems are plotted with open triangles. The line indicates the activity lifetime given by West et al. (2008).


Figure 5.4: $\mathrm{H} \alpha$ EW and age of the systems for different spectral types of the secondary star. All systems above the dotted line $(\mathrm{EW}>1 \AA)$ are active.
$\chi=f_{\mathrm{H} \alpha} / f_{\text {bol }}$ (Walkowicz et al. 2004; West et al. 2004, 2008). Based on a sample of M stars covering the spectral range M0-L0, Walkowicz et al. (2004) tabulated $\chi$ as a function of spectral type and we make use of their values. In the bottom right panel of Fig. 5.2 we plot the calculated $\chi_{\mathrm{H} \alpha}$ as a function of the spectral type (diamonds) together with values from the fit given by West et al. (2008) for field dM stars (squares). The strength of magnetic activity is more or less constant for earlier spectral types than M4 and a decrease towards later spectral types. Although the results are similar to those from field stars, there is a systematic trend to higher values, effect which is related to higher EW for the PCEBs.

### 5.5 Binary age

For wide binaries the age of the system can be estimated from the age of the white dwarf, which is the sum of the cooling age of the white dwarf (time passed since the planetary nebulae phase, $t_{\text {cool }}$ ) and the time it took to evolve a star from the main sequence to a white dwarf of mass $M_{\mathrm{wd}}$ $\left(t_{\text {evol }}\right)$, that is $t=t_{\text {cool }}+t_{\text {evol }}$. For all the systems with reliable stellar parameters we calculated the cooling age of the white dwarfs by interpolating the cooling tracks provided by Wood et al. (1995) for CO white dwarfs and Althaus \& Benvenuto (1996) for He core white dwarfs, i.e. for

WDs with masses below $0.47 \mathrm{M}_{\odot}$. We asumed the initial to final mass empirical relation from Catalán et al. (2008) given by:

$$
\begin{equation*}
M_{f}=(0.096 \pm 0.005) M_{i}+(0.429 \pm 0.015) \tag{5.1}
\end{equation*}
$$

for $M_{i}<2.7 \mathrm{M}_{\odot}$ and:

$$
\begin{equation*}
M_{f}=(0.137 \pm 0.007) M_{i}+(0.318 \pm 0.018), \tag{5.2}
\end{equation*}
$$

for larger masses. We calculated the nuclear time scale for the progenitor mass, $t_{\text {evol }}$, using the relation from Iben \& Laughlin (1989):

$$
\begin{equation*}
\log t_{\text {nucl }}=9.921-3.6648 \log M+1.9697(\log M)^{2}-0.9369(\log M)^{3}, \tag{5.3}
\end{equation*}
$$

We added the calculated nuclear time to the cooling ages. Please note that the total age derived in this way represents a reliable estimate for wide WDMS only, i.e. for systems that did not interact in the past. The total age of PCEBs has to be calculated by reconstructing common envelope evolution and significantly depends on the common envelope efficiency (Nelemans \& Tout 2005) (Zorotovic et al. 2009, in prep.). As there are probably some PCEBs even among those systems that did not show radial velocity variations, the given total ages can be significantly wrong for individual systems. However, the majority of the WDMS without radial velocity variations are wide WDMS and the derived ages can therefore be used for describing the typical age of wide WDMS binaries.

In Fig. 5.3 we plot the age of the system as a function of spectral type, active systems are plotted with filled diamonds and inactive with black triangles, the line indicates the mean activity lifetime given by West et al. (2008). Most of the active systems are younger than the activity lifetime explaining the higher fraction of active stars with respect to field stars obtained in Sect. 5.3. For comparison of our results with the results from Silvestri et al. (2005) we plot the EW versus the age for different spectral types as in their Fig. 4 and show it in Fig. 5.4. Our systems are in general younger than the sample from Silvestri et al. (2005) which can then explain why we obtain a higher fraction of active systems at each spectral type (see Sect. 5.3).

### 5.6 Activity and distance

We estimated the distances to our subsample of 193 WDMS binaries with DAs as primary stars in chapter 2. We have two estimates, one coming from the fit to the WD, $d_{\mathrm{wd}}$, and another coming from the fit to the secondary spectral type, $d_{\text {sec }}$. We obtained a disagreement of more than $1.5 \sigma$ for about $30 \%$ of the systems. Rebassa-Mansergas et al. (2007) suggested that activity could be the cause of such discrepancy. Active M stars show larger radii (López-Morales \& Shaw 2007) and lower effective temperatures at constant luminosities (Morales et al. 2008) than their inactive counterparts, resembling earlier spectral types and leading to a larger distance estimate. We have distinguished between active and inactive systems so we investigate this possibility in detail.


Figure 5.5: Distances estimated to the WDMS with DA as primary in chapter 2. In the upper panels all the systems are included, independent on their errors, while in the bottom panels only those with relative error smaller than $25 \%$ are included. In the left panels we plot systems differing in more than $1-\sigma$ with blue filled circles. In the middle panels we plot systems with active secondaries with red filled circles. In the left panels we show only systems that differ more than $1-\sigma$ and plot systems with active secondaries with red filled circles.

In the left panels of Fig. 5.5 we plot the two estimated distances, $d_{\text {sec }}$ against $d_{\text {wd }}$, for all the systems (upper panel) and for those that have stellar parameters of the DA with relative errors smaller than $25 \%$ (bottom panel), plotting in blue the systems for which the difference between $d_{\text {sec }}$ and $d_{\text {wd }}$ is larger than $1.5 \sigma$. Among the $193 \mathrm{DA} / \mathrm{dM}$ binaries, 98 contain active secondary stars (middle panels, red filled circles). In the right panels we plot only those systems for which we obtained a difference between the two estimated distances larger than $1.5 \sigma$, with systems with active secondaries plotted in red. While around $50 \%$ of all the DA/dM contain active secondaries, if we only select the systems for which we obtained a difference between the two estimated distances larger than $1.5-\sigma$, more than $60 \%$ of them contain active secondaries (plotted in red in the right panel). We expected to have the active systems located at the left side of the right panels, but as we can see they are distributed over $d_{\mathrm{wd}}>d_{\mathrm{sec}}$ too. In fact, we found the opposite: the majority of the systems with longer $d_{\mathrm{wd}}$ are active. We can only conclude that for around $50 \%$ of the systems activity might be the cause of the discrepancy between the distances
derived from the dM and the WD , but this is still work in progress.

### 5.7 Summary

We have measured the activity of the secondary stars, finding that wide binaries have a similar trend as field stars, that is an increase in the number of active stars with spectral type. Although, at earlier spectral types than M4 the fraction of active stars is higher than for field stars, and also higher than found before in WDMS wide systems by Silvestri et al. (2005). To explain such effect we investigated the possibility of PCEB contamination at this spectral types and also calculated the age of the systems. We conclude that since the systems with secondaries in this spectral type range are younger than the activity lifetime it reflects an age effect. At least $90 \%$ of the PCEB are active, since we have just used the $\mathrm{H} \alpha$ emission as an activity indicator, this value is just a lower limit, and it might well be that all the PCEB are active, pointing to an enhancement of activity due to the fact of having a companion star. The EW of the $\mathrm{H} \alpha$ line is higher for close systems at each spectral type, but on the one hand the number of close binaries at earlier spectral types is rather small. And on the other hand as we have seen in chapter 4 most of the close binary stars have a rather short orbital period, which when having a hot white dwarf as a primary would cause the secondary's surface to be heated, enhancing the $\mathrm{H} \alpha$ emission line. We investigated whether the difference in the two estimated distances from chapter 2 could be explained by the activity of the secondary star, finding a positive result for $\sim 50 \%$ of the systems. A more detail analysis based on a larger database is in progress and will give more light into the activity-binarity relation.

## Chapter 6

## The eclipsing system SDSS1212-0123

From optical photometry we show that SDSSJ121258.25-012310.1 is a new eclipsing, post common-envelope binary with an orbital period of 8.06 hours and an eclipse length of 23 min utes. We observed the object over 11 nights in different bands and determined the ephemeris of the eclipse to $\mathrm{HJD}_{\text {mid }}=2454104.7086(2)+0.3358706(5) \times \mathrm{E}$, where numbers in parenthesis indicate the uncertainties in the last digit. The depth of the eclipse is $2.85 \pm 0.17 \mathrm{mag}$ in the $V$ band, $1.82 \pm 0.08 \mathrm{mag}$ in the $R$ band and $0.52 \pm 0.02 \mathrm{mag}$ in the $I$ band. From spectroscopic observations we measured the semi-amplitude of the radial velocity $K_{2}=181 \pm 3 \mathrm{~km} / \mathrm{s}$ for the secondary star. The stellar and binary parameters of the system were constrained from a) fitting the SDSS composite spectrum of the binary, b) using a $K$-band luminosity-mass relation for the secondary star, and c) from detailed analyses of the eclipse light curve. The white dwarf has an effective temperature of $17700 \pm 300 \mathrm{~K}$, and its surface gravity is $\log g=7.53 \pm 0.2$. We estimate that the spectral type of the red dwarf is $\mathrm{M} 4 \pm 1$ and the distance to the system is $230 \pm 20$ parsec. The mass of the secondary star is estimated to be in the range $M_{\mathrm{sec}}=0.26-0.29 \mathrm{M}_{\odot}$, while the mass of the white dwarf is most likely $M_{\mathrm{wd}}=0.46-0.48 \mathrm{M}_{\odot}$. From an empirical mass-radius relation we estimate the radius of the red dwarf to be in the range $0.28-0.31 \mathrm{R}_{\odot}$, whereas we get $R_{\mathrm{wd}}=0.016-0.018 \mathrm{R}_{\odot}$ from a theoretical mass-radius relation. Finally we discuss the spectral energy distribution and the likely evolutionary state of SDSS1212-0123.

### 6.1 Introduction

In this chapter we report the discovery of a new eclipsing PCEB. In our ongoing search for PCEBs among white-dwarf/main-sequence binaries (Schreiber et al. 2008; Rebassa-Mansergas et al. 2007, 2008, 2009), SDSSJ121258.25-012310.1 (Adelman-McCarthy et al. 2008) (henceforth SDSS1212-0123) was included in our target list for photometric monitoring of candidate objects. The serendipitous discovery of a binary eclipse from time-resolved differential photometry triggered a photometric and spectroscopic follow-up. Only seven eclipsing binaries containing a white dwarf and a low mass main sequence star were known until 2007. Since then another three
eclipsing systems have been published (Steinfadt et al. 2008; Drake et al. 2009), and a further three systems have been discovered by us (Pyrzas et al. 2009). Eclipsing binaries are of great interest since they offer the possibility of deriving fundamental properties of stars with a high accuracy. SDSS1212-0123 was firstly listed as a quasar candidate by Richards et al. (2004) and later classified as a DA + dMe by Silvestri et al. (2006). It contains a relatively hot white dwarf (from now on primary) and an active mid-type dM star (from now on secondary).

We summarize our current knowledge about this source from own observations and archival work. It is organized as follows. In Sect. 6.2 we describe the observations and reductions. In Sect. 6.3 we present the results, we study the evolution of the system in Sect. 6.4 and conclude in Sect. 6.6.

### 6.2 Observations and reductions

### 6.2.1 IAC80 and AIP70 photometry

Optical photometric observations were obtained using two different telescopes over 11 nights. The 80 cm telescope IAC80 in Observatorio del Teide, Spain, was equipped with the standard CCD camera and the 70 cm telescope of the Astrophysical Institute Potsdam at Babelsberg was used with a cryogenically cooled 1 x 1 k TEK-CCD. A $\log$ of observations is presented in Table 6.1. A field of $\sim 3$ arc minutes was read with the IAC80 CCD camera, and we used a binning factor of 2 in both spatial directions (scale of $0.6^{\prime \prime}$ ), while we used a binning factor of 3 for the 70 cm telescope (scale of 1.41 "), in order to decrease the readout time and improve the signal to noise. Reduction was performed using standard packages in IRAF ${ }^{1}$ and MIDAS. Differential magnitudes were obtained with respect to the comparison star SDSS J121302.39-012343.5 (see Fig.6.1), with magnitudes ugriz=17.40, 16.00, 15.51, 15.36, 15.30. SDSS magnitudes were transformed into Johnson's using equations taken from the Sloan pages ${ }^{2}$. Neglecting the color term, we calculated absolute magnitudes of SDSS1212-0123. The estimated error of the absolute calibration is 0.05 mag .

### 6.2.2 Spectroscopy

Spectroscopic follow up observations were obtained during the period 16-19 May 2007 with the LDSS3 imaging spectrophotograph at the Magellan Clay telescope. Ten spectra were taken for SDSS1212-0123. Exposure times varied from 300 to 600 seconds. Seeing and transparency were highly variable. The VPH_Red grism and an OG590 blocking filter were used. The detector

[^15]

Figure 6.1: SDSS image of SDSS1212-0123 (in the cross-hair) and the comparison star $(R A=$ 12:13:02.39, $D E C=-01: 23: 43.5)$.

Table 6.1: Log of photometric observations for SDSS1212-0123.

| Date | Tel | Filter | $t_{\text {int }}$ | $N_{\text {obs }}$ | $\phi_{\text {ini }}$ | $\phi_{\text {fin }}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 04 Jan 2007 | IAC80 | $I$ | 180 | 74 | 0.805 | 1.278 |
| 26 Jan 2007 | AIP70 | $V$ | 180 | 19 | 0.041 | 0.156 |
| 13 Feb 2007 | IAC80 | $V$ | 70 | 191 | 0.607 | 1.202 |
| 14 Feb 2007 | IAC80 | $V$ | 70 | 221 | 0.525 | 1.292 |
| 12 Mar 2007 | AIP70 | $I$ | 120 | 181 | 0.031 | 0.946 |
| 13 Mar 2007 | AIP70 | $I$ | 120 | 153 | 0.377 | 1.343 |
| 14 Mar 2007 | AIP70 | $I$ | 120 | 49 | 0.786 | 1.040 |
| 15 Mar 2007 | AIP70 | $R$ | 120 | 73 | 0.683 | 1.023 |
| 26 Mar 2007 | AIP70 | $I$ | 120 | 45 | 0.994 | 1.179 |
| 21 May 2007 | AIP70 | $I$ | 90 | 59 | 0.907 | 1.097 |
| 06 May 2008 | IAC80 | $R$ | 120 | 32 | 0.913 | 1.049 |

was a STA $4 \mathrm{k} \times 4 \mathrm{k}$ pixel CCD with two read out amplifiers. We used a slit width of 0.75 arcsec, that together with the spectral resolution $R=1810$, gave a coverage of $5800-9980 \AA$ at a reciprocal dispersion of $1.2 \AA \AA_{\mathrm{pix}^{-1}}$. Four of the spectra taken at quadrature were obtained through a narrow slit of $0.5 \operatorname{arcsec}$ resulting in a FWHM spectral resolution of $4.8 \AA$, with the purpose
of measuring the radial velocity amplitude with a higher accuracy. Flat-field images were taken at the position of the target to allow effective fringe removal in the red part of the spectra. The spectral images were reduced using STARLINK packages FIGARO and KAPPA, and the spectra were optimally extracted (Horne 1986) using the PAMELA package (Marsh 1989). Wavelength calibration was done using sky lines. Wavelengths of good sky lines were obtained from the atlas of Osterbrock et al. $(1996,1997)$. A fifth-order polynomial was fitted to 36 sky lines. Spectra were flux calibrated and corrected for telluric lines using spectra of the standard star LTT3218 taken during the same observing run.

### 6.3 Results

### 6.3.1 The light curve

The optical light curve of SDSS1212-0123 displays a total eclipse of the primary with length of approximately 23 minutes. The depth of the eclipse is $0.52 \pm 0.02 \mathrm{mag}$ in the $I$ band, $1.82 \pm 0.08$ mag in the $R$ band and $2.85 \pm 0.17 \mathrm{mag}$ in the $V$ band (see Fig. 6.2). Eclipse magnitudes are $m_{I}=16.56 \pm 0.02, m_{R}=18.58 \pm 0.08$ and $m_{V}=19.68 \pm 0^{\mathrm{m}} 17$. The much deeper eclipse in the $V$ band is due to the fact that the primary emits most of the light in the blue, while the secondary dominates in the $I$ band. Photometric variability outside of the eclipse, e.g. from an irradiated secondary or from ellipsoidal modulation of the secondary, was found to be less than 0.01 .

At the given time resolution of our photometry, the WD ingress and egress phases are not resolved. Five eclipses were completely covered and the eclipse length was determined in these light curves measuring their full width at half maximum of the flux level. The weighted mean of those five measurements gives an eclipse length of $23 \pm 1 \mathrm{~min}$.

### 6.3.2 Ephemeris

In addition to the five eclipses which were covered completely one further eclipse was covered partially. Using the measured eclipse length from the previous section we thus determined six eclipse epochs (Table 6.2). The eclipses of March 12, 14 and 26, respectively, were not covered due to bad weather conditions. Using a phase-dispersion minimization technique a tentative period was determined, $P_{\text {orb }}=0.3359 \pm 0.0006$ hours, which was sufficiently accurate to connect all follow-up observations without a cycle count alias.

We then used the six mid eclipse epochs to calculate a linear ephemeris by fitting a line to the cycle number and eclipse epoch:

$$
\begin{equation*}
\mathrm{HJD}_{\text {mid }}=2454104.7086(2)+0.3358706(5) \times \mathrm{E}, \tag{6.1}
\end{equation*}
$$

where numbers in parenthesis indicate the $1 \sigma$ uncertainty in the last digits. The observed minus calculated values are tabulated in Table 6.2.


Figure 6.2: Optical photometry from the IAC80 telescope in the $V, R$ and $I$ band (from bottom to top) phase folded over the orbital period, $P_{\text {orb }}=8.06$ hours. The eclipse has $\sim 23$ minutes length. Note the different scales for each panel.

Table 6.2: Date, times of mid eclipses, cycle number obtained from the photometric observations and residuals from the linear ephemeris.

| Date | HJD (Mid-eclipse) | Cycle | $O-C(\mathrm{~s})$ |
| ---: | ---: | ---: | ---: |
| 04 Jan 2007 $^{c}$ | $2454104.7085(21)$ | 0 | -9.9 |
| 13 Feb 2007 $^{c}$ | $2454145.6847(8)$ | 122 | -11.0 |
| 14 Feb 2007 $^{p}$ | $2454146.6922(8)$ | 125 | -19.0 |
| 13 Mar 2007 $^{c}$ | $2454173.5621(10)$ | 205 | -0.3 |
| 21 May 2007 $^{c}$ | $2454242.4163(21)$ | 410 | 66.9 |
| 06 May 2008 | 2454593.4000(14) | 1455 | -25.9 |
| ${ }^{c}$ Eclipse completely covered. |  |  |  |
| Eclipse partially covered. |  |  |  |

### 6.3.3 Stellar parameters

## Decomposition of the SDSS spectrum

We determined the stellar parameters of SDSS1212-0123 from the SDSS spectrum following the procedure described in Rebassa-Mansergas et al. (2007).

In a first step the best match of the SDSS composite spectrum is determined with an optimization strategy on a grid of observed white dwarf and M-dwarf template spectra created from the SDSS DR6 database. The main result of this first step is the determination of the spectral type of the secondary. Using the spectral type-radius relation from Rebassa-Mansergas et al. (2007) and the apparent magnitude of the scaled template results in a first distance estimate $d_{\text {sec }}$. After subtracting the best-fitting M-star template, white-dwarf parameters are determined via $\chi^{2}$ minimization in a $\log g-T_{\text {eff }}$ grid of model atmospheres (Koester et al. 2005). Since this analysis step is performed on spectra normalized to a continuum intensity, the results are bi-valued yielding a 'hot' and a 'cold' solution (see Fig. 6.4). The degeneracy can typically be broken by an additional fit to the overall spectrum (continuum plus lines in the wavelength range 3850 $7150 \AA$ ). In the present case of SDSS1212-0123 the GALEX detection (see below) provides an additional constraint excluding the 'cold' solution. The results of the spectral decomposition and the white dwarf fit for SDSS1212-0123 are shown in Fig. 6.4.

Mass and radius of the white dwarf are calculated with the best-fitting $\log g-T_{\text {eff }}$ combination using updated versions of the tables by Bergeron et al. (1995). The flux scaling factor together with the derived radius of the white dwarf results in a second distance estimate of the binary, $d_{\mathrm{wd}}$.

The spectral type of the secondary was determined to be M4 $\pm 1$ implying a distance $d_{\text {sec }}=$ $320 \pm 95 \mathrm{pc}$, mass range of the secondary $M_{\text {sec }}=0.255-0.380 \mathrm{M}_{\odot}$ and radius range $R_{\text {sec }}=0.258$ $-0.391 \mathrm{R}_{\odot}$, using Rebassa-Mansergas et al. (2007) spectral type-mass and spectral type-radius empirical relations respectively. The derived temperature and $\log g$ of the primary were found to be only weakly dependent on the chosen spectral type and spectral template of the secondary, because we use $\mathrm{H} \beta-\mathrm{H} \epsilon$ for the white dwarf line fit, where the secondary star contribution is small. It is also weakly dependent on the accuracy of the spectral flux calibration and also the small radial velocity line displacements. The best fit was found for $T_{\text {eff }}=17700 \pm 300$ K and $\log g=7.53 \pm 0.05$ (implying a white dwarf mass $M_{\mathrm{wd}}=0.39 \pm 0.02 \mathrm{M}_{\odot}$, and $R_{\mathrm{wd}}=$ $0.018 \pm 0.001 \mathrm{R}_{\odot}$ ). The obtained values are in agreement with those published by Silvestri et al. (2006). However, one should be aware of the fact that all the quoted errors are purely statistical. The true uncertainty of the white dwarf spectral parameters is clearly higher than suggested by the derived numbers. We estimate the systematic uncertainty of our $\log g$ determination to be on the order of 0.2 dex, which results in rather wide ranges of possible values for the mass and the radius of the primary, i.e. $M_{\mathrm{wd}}=0.33-0.48 \mathrm{M}_{\odot}$ and $R_{\mathrm{wd}}=0.015-0.021 \mathrm{R}_{\odot}$.

The derived distance to the white dwarf is $d_{\mathrm{wd}}=226 \pm 8 \mathrm{pc}$ (assuming the statistical error only). The two distance estimates differ, $d_{\text {sec }}$ being longer than $d_{\mathrm{wd}}$, but in agreement within the errors. A similar trend was found by Rebassa-Mansergas et al. (2007) for 101 WDMS binaries in


Figure 6.3: Two component fit to SDSS1212-0123. The top panel shows the WDMS spectrum (black line) and the white dwarf and the M4 M-dwarf templates (dotted lines), while the lower panel shows the residuals to the fit.
their study. They argue that such difference could be due to stellar activity of the secondary star, and that the spectral type determined from the optical SDSS spectrum is too early for the mass of the secondary star, which would lead to a larger radius and consequently a larger distance to the system. Since the secondary in SDSS1212-0123 was found to be active too, we regard the distance estimate for the white dwarf being more reliable. Taking into account systematic errors we obtain $d_{\mathrm{wd}}=230 \pm 20 \mathrm{pc}$ as the distance to the system.

## Constraining the secondary mass using 2MASS

In the previous section we derived the mass and the radius of the secondary star using empirical relations from Rebassa-Mansergas et al. (2007) and obtained $M_{\mathrm{sec}}=0.255-0.380 \mathrm{M}_{\odot}$ and $R_{\mathrm{sec}}=$ $0.258-0.391 \mathrm{R}_{\odot}$, respectively. However, as clearly shown in Fig. 7 of Rebassa-Mansergas et al. (2007), the masses and radii derived from observations largely scatter around the empirical relations. In addition, according to Rebassa-Mansergas et al. (2007) increased activity of the rapidly rotating secondary stars in close binaries can cause the stars to appear as earlier spectral types when compared to non-active stars of the same mass. To sum up, the secondary masses derived from empirical relations can obviously only considered to reasonable but rough estimates.

An alternative method to determine the mass of secondary star is to use luminosity-spectral type relations. To that end, we explored the Two Micron All Sky Survey Point Source Catalog (Cutri et al. 2003), finding magnitudes $J=14.90 \pm 0.03, H=14.39 \pm 0.05$ and $K_{\mathrm{s}}=13.96 \pm 0.05$ for SDSS1212-0123. Subtracting the extrapolated contribution of the primary star $(\log g=7.5$


Figure 6.4: Spectral model fit to the white dwarf component of SDSS1212-0123, obtained after subtracting the best-fit M-dwarf template from its SDSS spectra. Top left panel: best fit (black lines) to the normalized $\mathrm{H} \beta$ to $\mathrm{H} \epsilon$ line profiles (gray lines, top to bottom). Top right panel: 1,2 and $3 \sigma \chi^{2}$ contour plots in the $T_{\text {eff }}-\operatorname{logg}$ plane. The black contours refer to the best line profile fit, the red contours to the fit of the whole spectrum. The dashed line indicates where the maxima of the $\mathrm{H} \beta$ equivalent width occurs in the $T_{\text {eff }}-\log g$ plane, dividing it into two different solutions, a cold and a hot one. The best-fit parameters of the hot and the cold normalized line profile solutions and of the fit to the $3850-7150 \AA$ range are indicated by the black and the red dots, respectively. Bottom panel: the white dwarf spectrum and associated flux errors (gray lines) along with the best-fit white dwarf model (black lines) to the 3850 $-7150 \AA$ wavelength range (top) and the residuals of the fit (gray line, bottom).
and $\left.d_{\mathrm{wd}}=230 \mathrm{pc}\right)$ yields infra-red colors of $J-H=0.51 \pm 0.06, H-K_{s}=0.43 \pm 0.07$, respectively. Using the empirical mass-luminosity relation from Delfosse et al. (2000), we derive the mass of the secondary star to be $0.26 \pm 0.03$. Using again the mass-radius relation from Rebassa-Mansergas et al. (2007) this implies a spectral type M5, i.e. later by one spectral type than estimated from the deconvolution of the SDSS spectrum. This supports the idea of activity significantly affecting the determination the secondary star spectral types and the corresponding distances.

## Radial velocity

In each of our observed spectra we measured the radial velocities of the NaI absorption doublet ( $8183.27 \AA, 8194.81 \AA$ ), which originates from the secondary star. A double Gaussian with a fixed separation of $11.54 \AA$ was fitted to the line profiles using the FIT/TABLE command provided by ESO/MIDAS.
$\mathrm{H} \alpha$ was deconvolved into an absorption and an emission line component using two Gaussians. While the emission line showed pronounced wavelength shifts, the centroids of the absorption lines thus measured did not constrain the curve of the white dwarf significantly.

Assuming a circular orbit a sine-function was fitted to the measured radial velocity curves to obtain the radial velocity semi-amplitude $K_{2}$ of the secondary star:

$$
\begin{equation*}
v_{r}=\gamma_{2}+K_{2} \sin \left[\frac{2 \pi\left(t-t_{0}\right)}{P}\right], \tag{6.2}
\end{equation*}
$$

The orbital period $P$ and the epoch of mid eclipse $t_{0}$ were determined photometrically and were kept fixed for the radial velocity fit. For the NaI doublet we find the systemic velocity $\gamma_{2}=$ $17 \pm 3 \mathrm{~km} \mathrm{~s}^{-1}$ and $K_{2}=181 \pm 3 \mathrm{~km} \mathrm{~s}^{-1}$, while we find for the $\mathrm{H} \alpha$ line $\gamma_{2}=21 \pm 2 \mathrm{~km} \mathrm{~s}^{-1}$ and $K_{2}=161 \pm 3 \mathrm{~km} \mathrm{~s}^{-1}$. The fit to the NaI lines is shown if Fig. 6.5 together with the residuals.

The semi-amplitudes of the two radial velocity curves are different and these differences seem to be significant. The semi-amplitude derived from $\mathrm{H} \alpha$ is lower, indicating that its emission is displaced towards the inner hemisphere of the secondary star with respect to the NaI doublet. As neither of the two line features shows significant photometric variability, which would indicate a biased origin of one of the line species (e.g. towards the non-irradiated side of the secondary), we exclude irradiation as the explanation for the observed difference in $K_{2}$. A detailed comparison of radial velocities derived from the NaI doublet and $\mathrm{H} \alpha$ lines has been performed by Rebassa-Mansergas et al. (2007). They find that both velocities often significantly differ but that there seems to be no systematic shift of $\mathrm{H} \alpha$ radial velocities towards smaller values. As discussed in detail in Rebassa-Mansergas et al. (2008), this is probably explained by the $\mathrm{H} \alpha$ emission being related to activity and not uniformly distributed over the surface of the secondary. Kafka et al. (2005) studied in detail the origin of different line species, however SDSS1212-0123 shows no evidence of accretion nor irradiation. We therefore assume that in SDSS1212-0123 the NaI doublet much better traces the center of mass of the secondary and we use its semi-amplitude for the mass estimate.

We write the mass function of the binary assuming a circular orbit in the form

$$
\begin{equation*}
M_{\mathrm{sec}}=\left(\sqrt{\frac{2 \pi G \sin ^{3} i}{P K_{2}^{3}} M_{\mathrm{wd}}}-1\right) M_{\mathrm{wd}}, \tag{6.3}
\end{equation*}
$$

and derive an upper limit for $M_{\text {sec }}$ for a given white-dwarf mass $M_{\mathrm{wd}}$ assuming $i=90^{\circ}$ (see bottom panel of Fig. 6.6).


Figure 6.5: Radial velocities measured from the NaI doublet $8183,8194 \AA$ originating from the secondary star of SDSS1212-0123 folded over the orbital period obtained from the photometry. Sine fit and residuals (lower panel) are shown.

Using the empirical mass-radius relation for main sequence stars derived by Bayless \& Orosz (2006) we estimate the radius of the secondary (middle panel of Fig. 6.6). The top panel of the same figure illustrates the maximum possible eclipse length ( $i=90^{\circ}$, black line) for the given stellar radius, the orbital period $P$ and the orbital separation $a$ according to

$$
\begin{equation*}
t_{\mathrm{ecl}}=\frac{R_{\mathrm{sec}} P}{\pi a} \tag{6.4}
\end{equation*}
$$

The measured values of the eclipse length and the range of the white-dwarf mass from Sec.6.3.3 are shown in the figure with horizontal and vertical lines, respectively, their intersection is shaded in grey in the top panel. It is also plotted the solution for $i=75^{\circ}$ for comparison. From the eclipse length the range of possible values for the mass of the WD is $M_{\mathrm{wd}}=0.46-0.52$, and for the $\mathrm{dM} M_{\text {sec }}=0.21-0.32 \mathrm{M}_{\odot}$, and $R_{\text {sec }}=0.23-0.34 \mathrm{R}_{\odot}$.

## Light curve modeling

A determination of most of the physical parameters of an eclipsing system can be achieved by fitting model light curves to the actual data. We made use of a newly developed light curve fitting code, written by T.R. Marsh, for the general case of binaries containing a white dwarf. The code is described in detail in Pyrzas et al. (2009). Briefly, a model light curve is computed based on user-supplied initial system parameters. These are the two radii, scaled by the binary separation, $R_{\mathrm{wd}} / a$ and $R_{\text {sec }} / a$, the orbital inclination, $i$, the un-irradiated stellar temperatures of the white dwarf and the secondary star $T_{\text {eff,WD }}$ and $T_{\text {eff,sec }}$ respectively, the mass ratio $q=M_{\text {sec }} / M_{\mathrm{wd}}$ and $t_{0}$ the time of mid-eclipse of the white dwarf.

Starting from this parameter set, the model light curve is then fitted to the data using LevenbergMarquardt minimization. Every parameter can either be allowed to vary or remain fixed, during


Figure 6.6: Solution of the mass function for $K_{2}=181 \pm 3 \mathrm{~km} / \mathrm{s}$ as a function of $M_{\mathrm{wd}}$ (bottom panel); radius from the mass-radius empirical relation from Bayless \& Orosz (2006) (mid panel); eclipse duration (top panel), assuming circular orbit and an inclination angle of $90^{\circ}$. Vertical lines indicate the mass of the primary star, $M_{\mathrm{wd}}=(0.33-0.48) \mathrm{M}_{\odot}$, as determined from the deconvolution of the SDSS spectrum. The eclipse length, $t_{\text {ecl }}=23 \pm 1$ min, is marked with horizontal lines, and the intersection in shaded in grey. The errors in $K_{2}$ are shown with the small dashed lines in the three panels. In the top panel the solution for an inclination of $75^{\circ}$ is plotted with a blue line to show it's influence. See text for a more detailed description.
the fitting process.
Our approach for modeling the $I$ band photometry of SDSS1212-0123 was the following. A large and dense grid of points in the $M_{\mathrm{wd}}-M_{\text {sec }}$ plane was first calculated, generously bracketing the estimates for the mass of the two components (see Sec.6.3.3). Each point defines a mass ratio $q$, and through $P_{\text {orb }}$, a binary separation $a$. Furthermore, from the mass function equation (Eq. 6.3), using the value of $K_{2}$ (derived in Sec. 6.3.3) and $P_{\text {orb }}$, one can calculate the inclination angle $i$. Points for which (formally) $\sin i>1$ were discarded from the grid, for all other points the corresponding light curve model was computed, leading to the computation of some 9000 models.

As an initial estimate for the radii of the binary components, we adopted values from the theoretical M - R relations of Bergeron et al (1995) for the white dwarf, and Baraffe et al. (1998) - the 5 Gyr model - for the secondary. Regarding the two temperatures, $T_{\text {eff,WD }}$ and $T_{\text {eff,sec }}$, the value from our spectral decomposition (Sec.6.3.3) was used for the white dwarf, while the $\operatorname{Sp}(2)$ - T relation from Rebassa-Mansergas et al. (2007), together with our result for the spectral type of the secondary, were used to obtain an initial value for $T_{\text {eff,sec }}$.

For the fitting process $q, i, R_{\mathrm{wd}}$ and $T_{\text {eff }, \mathrm{WD}}$ were fixed, leaving only $R_{\text {sec }}, T_{\text {eff,sec }}$ and $t_{0}$ free
to vary. $R_{\mathrm{wd}}$ was fixed mainly because of the poor temporal resolution of our data set, which does not resolve the white dwarf ingress and egress. Consequently, if allowed to vary, the white dwarf radius would only be loosely constrained and it would introduce large uncertainties in the determination of $R_{\text {sec }}$. $T_{\text {eff,WD }}$ was also fixed, because allowing both temperatures to vary simultaneously would lead to a degenerate situation, as they are strongly correlated. Our spectral decomposition results are sufficiently accurate, so as to allow us to fix $T_{\text {eff,WD }}$ without affecting the fitting result. The parameter $t_{0}$ on the other hand, was left free during the fitting, to account for the $O-C$ errors in the mid-eclipse times, which in some cases were significant (see Table 6.2 again).

The results of the light curve fitting process were analyzed as follows. We first applied a cut in the quality of the fits. This was done by selecting the minimum $\chi^{2}$ value of all fits and then culling all model fits at $>1 \sigma$ above the best fit. Afterwards, we selected from the remaining, equally good light curve fits, those which where physically plausible. We defined a $\delta R$ parameter, as $\delta R=\left(R_{\mathrm{fit}}-R_{\mathrm{th}}\right) / R_{\mathrm{th}}$, i.e. how much the fitted radius value deviates from the theoretical radius value, obtained from a M-R relation, for a given model. Thus, we selected only those models that had $\delta R \leq 0.15$, to allow for an oversized secondary.

The results are illustrated in Fig. 6.7. Black dots designate those light curve fits making the $1 \sigma$ cut, red dots those that satisfy both the $1 \sigma$ and $\delta R=15 \%$ cuts. The resulting ranges in white dwarf masses and secondary star masses (indicated with dashed, vertical, red lines) are $M_{\mathrm{wd}}=0.46-0.6 \mathrm{M}_{\odot}$ and $M_{\text {sec }}=0.23-0.4 \mathrm{M}_{\odot}$, respectively, corresponding to a white dwarf radius of $R_{\mathrm{wd}}=0.013-0.016 \mathrm{R}_{\odot}$ and a secondary radius of $R_{\mathrm{sec}}=0.27-0.41 \mathrm{R}_{\odot}$. The range for the inclination angle is $i=82^{\circ}-90^{\circ}$. Also indicated, with dotted, horizontal, gray lines are the radii of M-dwarfs with spectral types $\mathrm{Sp}(2)=\mathrm{M} 3-\mathrm{M} 5$ in steps of 0.5 , based on the spectral type-mass relation given by Rebassa-Mansergas et al. (2007).

Fig. 6.8 shows one example of the light curve fits within the components masses range for the model parameters: $M_{\mathrm{wd}}=0.49 \mathrm{M}_{\odot}, M_{\text {sec }}=0.26 \mathrm{M}_{\odot}$ and $i=89.2^{\circ}$. The detailed models do not predict any variation in the light curve caused by irradiation of the secondary star by the white dwarf. The predicted variations due to ellipsoidal modulation are expected to be quite small, i.e. $\sim 0.005 \mathrm{mag}$, consistent with our observational non-detection of any variability outside the eclipse.

## Spectral energy distribution

We cross-identified SDSS1212-0123 with the database from the Galaxy Evolution Explorer (GALEX (Martin et al. 2005; Morrissey et al. 2005)), and found a detection in the far and near ultraviolet (FUV and NUV). The magnitudes are $m_{\mathrm{FUV}}=16.79 \pm 0.03 \mathrm{mag}$ and $m_{\mathrm{NUV}}=16.81 \pm 0.02$ mag, exposure times were 150 sec . FUV and NUV fluxes can provide an estimate of the effective temperature of the white dwarf for a certain $\log g$, assuming that all the flux in the UV is emitted by the primary. White dwarf models for $\log g=7.5$ and $\log g=8.0$ and effective temperature in the range $6000-100000 \mathrm{~K}$, were folded over the FUV and NUV filters. The calculated



Figure 6.7: Light curve model fitting results for SDSS 1212-0123. Left panel: $M_{\text {wd }}$ and $M_{\text {sec }}$ values corresponding to fits with $\chi^{2}$ values within $1 \sigma$ of the minimum value (black points) and, simultaneously, with $\delta R \leq 0.05$ (red points). Right panel: the same, only in the $q-i$ plane. Also depicted in the left panel are curves corresponding to the mass function (solid black lines, $i=90^{\circ}$ and $75^{\circ}$ ) which (by definition) bracket the possible solutions, $\mathrm{Sp}(2)$ - M relations (dotted, horizontal, gray lines) and the range of possible ( $M_{\mathrm{wd}}, M_{\mathrm{sec}}$ ) values (dashed, horizontal and vertical, red lines)

Figure 6.8: Model fit to the $I$ band light curve of SDSS 1212-0123, for $M_{\mathrm{wd}}=0.49 \mathrm{M}_{\odot}$ and $M_{\text {sec }}=0.26 \mathrm{M}_{\odot}$. The model meets both the $\chi^{2}$ (within $1 \sigma$ ) and the $\delta R$ (within $15 \%$ ) cut-offs. The residuals from the fit are shown at the bottom of the panel. Inset panel: data points and model fit focused around the eclipse phase.
flux ratio FUV/NUV was compared with the observed for SDSS1212-0123 (see Fig. 6.9) . The GALEX flux ratio implies $T_{\text {eff }} \sim 13000 \mathrm{~K}$, significantly colder than what we obtain from the optical spectrum in Sec. 6.3.3. However, discrepant temperatures from GALEX UV and optical photometry were noticed earlier from an analysis for a large number of white dwarfs ( $\sim 250$ ) by Kawka \& Vennes (2007). We searched for standard stars with well determined temperatures and gravities that had been observed with GALEX and retrieved their fluxes. In table 6.3 we list their


Figure 6.9: Calculated FUV/NUV ratio for white dwarf models for $\log g=7.5$ and $\log g=8.0$ (solid and dashed lines) and effective temperature in the range $6000-100000 \mathrm{~K}$, observed FUV/NUV for 5 standard stars with well determined temperatures and gravities (indicated with their name) and for SDSS1212-0123 (horizontal line).

Table 6.3: Temperatures, gravities and GALEX fluxes for a number of standard stars in the same $\log$ grange as SDSS1212-0123.

| Name | $T_{\text {eff }}$ | $\log (g)$ | NUV | FUV |
| :--- | :--- | :--- | :--- | :--- |
| BPM16274 | $18745 \pm 564$ | $7.80 \pm 0.5$ | $6.16864 \mathrm{e}+15$ | $1.81443 \mathrm{e}+16$ |
| BPM3523 | $23614 \pm 78$ | $7.82 \pm 0.04$ | $1.09845 \mathrm{e}+16$ | $3.25284 \mathrm{e}+16$ |
| G93-48 | $17653 \pm 319$ | $7.99 \pm 0.06$ | $1.82277 \mathrm{e}+16$ | $4.35370 \mathrm{e}+16$ |
| BPM27891 | $16435 \pm 488$ | $7.93 \pm 0.36$ | $2.39285 \mathrm{e}+15$ | $6.82102 \mathrm{e}+15$ |
| HZ4 | $14100 \pm 350$ |  | $2.96225 \mathrm{e}-14$ | $7.19828 \mathrm{e}-14$ |

temperatures, gravities (Bragaglia et al. 1995) and GALEX fluxes and we show their FUV/NUV ratios in Fig. 6.9.

This shows that one cannot expect the same UV and optical temperatures in a case-by-case basis, but at best on a statistical average. For the time being we accept the temperature from our fit to the SDSS spectrum, which grossly reflects the UV to optical SED.

The spectral energy distribution is shown in Fig. 6.10, including ultraviolet, optical and infrared fluxes from 2MASS. A model spectrum for a white dwarf of pure Hydrogen (Koester et al.


Figure 6.10: Spectral energy distribution of SDSS1212-0123. GALEX near and far ultraviolet and 2MASS infrared fluxes (black circles), optical SDSS spectrum (black line). A white dwarf model of $T_{\text {eff }}=17500 \mathrm{~K}$ and $\log g=7.5$ (blue dashed line) and the spectrum of LHS1504 with spectral type M5 from Legget's library (red dots) are shown for comparison .
2005) with effective temperature of 17500 K and $\log g=7.5$ and a spectrum of the M5 star LHS1504 from Legget's library ${ }^{3}$ are shown for comparison (Leggett et al. 2000).

## Binary parameters summary

Fig. 6.11 shows the different ranges for the masses of the primary and the secondary from the spectral decomposition fit (Sect.6.3.3), the $K$-band luminosity-mass relation (Sect. 6.3.3), the radial velocity amplitude and eclipse length (Sect. 6.3.3) and the detailed light curve fitting (Sect.6.3.3). Of course, the different methods are not entirely independent, e.g. the constraints from the eclipse length/radial velocities studies and the detail light curve fitting basically use the same information with the only difference being that we could derive a clear lower limit from the latter. The dark shaded region in Fig. 6.11 represents the ranges of stellar masses in agreement with all the derived constraints i.e., $M_{\mathrm{wd}}=0.46-0.48 \mathrm{M}_{\odot}, M_{\mathrm{sec}}=0.26-0.29 \mathrm{M}_{\odot}$, implying a radius of the secondary star in the range $R_{\text {sec }}=0.28-0.31 \mathrm{R}_{\odot}$ using the empirical M-R relation from Bayless \& Orosz (2006) and $R_{\mathrm{wd}}=0.016-0.018 \mathrm{R}_{\odot}(\log g=7.5-7.7)$. We adopt these values as the most probable ones and all finally accepted stellar and binary parameters based on Sloan-data, other catalogues and our own follow-up observations are collected in Table 6.4.

[^16]

Figure 6.11: The ranges of masses of the white dwarf and the red dwarf coming from: the decomposition of the SDSS spectrum; the infrared brightness; the eclipse length for an inclination of $90^{\circ}$, and, the detailed light curve modeling. Each of the areas is labeled correspondingly, the intersection of the four different methods occurs for $M_{\mathrm{sec}}=0.26-0.29 \mathrm{M}_{\odot}$ and $M_{\mathrm{wd}}=0.44-0.46 \mathrm{M}_{\odot}$.

### 6.4 Evolutionary state

The post CE evolution of compact binaries is driven by angular momentum loss due to gravitational radiation and - perhaps much stronger - magnetic wind braking. Unfortunately, the latter mechanism is currently far from being well constrained, and predicting and reconstructing the post CE evolution sensitively depends on the assumed prescription for magnetic braking.

However, the disrupted magnetic braking scenario proposed by Rappaport et al. (1983) can still be considered the standard model for magnetic braking in close compact binaries. In this scenario it is assumed that magnetic braking ceases when the secondary star becomes fully convective at $M_{\text {sec }} \sim 0.3 \mathrm{M}_{\odot}$ (which corresponds to $P_{\text {orb }} \sim 3 \mathrm{hrs}$ ). Although observations of the spin down rates of single stars do drastically disagree with the predictions of disrupted magnetic braking (Sills et al. 2000), it remains the only consistent theory explaining the orbital period gap i.e. the observed deficit of CVs in the range of $P_{\text {orb }} \sim 2-3 \mathrm{hrs}$. Moreover, first results of our radial velocity survey of PCEBs seem to support the idea of disrupted magnetic braking

Table 6.4: Stellar and binary parameters of SDSS1212-0123.

| Parameter | Value | Parameter | Value |
| :--- | ---: | :--- | ---: |
| R.A. $(J 2000.0)$ | 121258.25 | $T_{\text {eff }}(\mathrm{K})$ | $17700 \pm 300$ |
| Dec. $(J 2000.0)$ | -012310.1 | $\log g(\mathrm{dex})$ | $7.5-7.7$ |
| $u$ | $17.045 \pm 0.020$ | $\mathrm{Sp}(2)$ | $\mathrm{M} 4 \pm 1$ |
| $g$ | $16.769 \pm 0.013$ | $R_{\mathrm{wd}}\left(\mathrm{R}_{\odot}\right)$ | $0.016-0.018$ |
| $r$ | $16.936 \pm 0.013$ | $R_{\text {sec }}\left(\mathrm{R}_{\odot}\right)$ | $0.28-0.31$ |
| $i$ | $16.627 \pm 0.015$ | $M_{\mathrm{wd}}\left(\mathrm{M}_{\odot}\right)$ | $0.46-0.48$ |
| $z$ | $16.136 \pm 0.018$ | $M_{\text {sec }}\left(\mathrm{M}_{\odot}\right)$ | $0.26-0.29$ |
| $J$ | $14.83 \pm 0.03$ | $P_{\text {orb }}(\mathrm{days})$ | $0.3358706(5)$ |
| $H$ | $14.35 \pm 0.05$ | $K_{2}\left(\mathrm{~km} \mathrm{~s}^{-1}\right)$ | $181 \pm 3$ |
| $K_{s}$ | $13.93 \pm 0.05$ | $\gamma_{2}\left(\mathrm{~km} \mathrm{~s}^{-1}\right)$ | $17 \pm 3$ |
| $m_{\mathrm{FUV}}$ | $16.79 \pm 0.03$ | $\mathrm{a}\left(\mathrm{R}_{\odot}\right)$ | $1.8 \pm 0.1$ |
| $m_{\mathrm{NUV}}$ | $16.81 \pm 0.02$ | $i_{\text {min }}$ | $82^{\circ}$ |
| $d(\mathrm{pc})$ | $230 \pm 20$ |  |  |

(Schreiber et al. 2008). To predict and reconstruct the post CE evolution of SDSS1212-0123 according to Schreiber \& Gänsicke (2003), we therefore assume disrupted magnetic braking.

First, we interpolate the cooling tracks of Wood et al. (1995) and estimate that the cooling age of SDSS1212-0123 is $6.8 \times 10^{7}$ yrs (see top panel of Fig.6.12). Second, according to the mass derived for the secondary star ( $M_{\text {sec }} \sim 0.27 \mathrm{M}_{\odot}$ ) we assume that, since SDSS1212-0123 left the CE phase, the only mechanism driving the evolution of SDSS1212-0123 towards shorter orbital periods is (and has been) gravitational radiation. As shown in Fig. 6.12 (bottom panel), SDSS1212-0123 left the CE phase with an orbital period of $P_{\text {CE }} \sim 8.07 \mathrm{hrs}$, very similar to the present value. Significant changes in the orbital period are predicted to occur on timescales longer than the current cooling age of the white dwarf. In $\sim 1.8 \times 10^{10}$ years SDSS1212-0123 will eventually become a CV within the orbital period gap, however, giving that it's calculated PCEB lifetime exceeds the age of the Galaxy it is not representative of the progenitors of todays CV population.

The mass of the primary star, makes SDSS1212-0123 more interesting since, as Shen et al. (2009) realized, it will become a CVs with a He core. Up to know there no CVs and only 8 WDMS with a He core.

### 6.5 Mass-radius relation for dM stars

Empirical mass-radius relations of low mass stars around $0.3 \mathrm{M}_{\odot}$, are up to $15 \%$ larger than predicted by models (López-Morales \& Shaw 2007). Observations of eclipsing systems are of utmost relevance, since we can get accurate parameters from them, for improving this relation.


Figure 6.12: Top panel: Interpolating the cooling tracks from Wood (1995) and according to the current temperature of the white dwarf ( $T_{\text {eff }}=17700 \mathrm{~K}$ ) we derive for SDSS1212-0123 a cooling age of $\sim 7 \times$ $10^{7}$ years. Bottom panel: Assuming gravitational radiation as the only angular momentum loss mechanism we reconstructed the post-CE evolution of SDSS1212-0123 and find that it left the CE phase with an orbital period of $P_{\mathrm{CE}} \sim 8.07 \mathrm{hrs}$. Apparently, SDSS1212-0123 has passed only a small fraction of its PCEB lifetime and it will take $\sim 1.8 \times 10^{10}$ years until SDSS1212-0123 will become a CV. At that moment the white dwarf temperature will be $T_{\text {eff }} \sim 4000 \mathrm{~K}$ and the system will be inside the period gap (grey bar).

Masses and radius of the secondary star for all close WDMS are given in table 1.2.2 and presented in Fig. 6.13. The empirical mass-radius relations from Rebassa-Mansergas et al. (2007) and Bayless \& Orosz (2006) are also shown. All the known eclipsing systems (Pyrzas et al. 2009) with a white dwarf as a primary and a low mass secondary star are plotted with squares and the position of SDSS1212-0123 is highlighted with a black filled square. We show the theoretical mass-radius relation from Baraffe et al. (1998) for $1 \mathrm{Gyr}, \mathrm{Z}=0.02$, and mixing length $\alpha=1$. We can see that models and observations are in agreement at the bottom of the massradius relation, but that as soon as we go to masses higher than $0.3 \mathrm{M}_{\odot}$ the differences increase. This behavior is seen in dM binaries as well and it has been suggested that this could be a result of stellar rotation linked to magnetic activity (López-Morales 2007). Nevertheless our systems with smaller mass than $0.3 \mathrm{M}_{\odot}$ have short orbital periods, that is they are fast rotators and they are in agreement with the theoretical values.


Figure 6.13: Masses and radius for all the close WDMS. Eclipsing systems are shown in squares, the position of SDSS1212-0123 is highlighted with a black filled square. The empirical mass-radius relations from Rebassa-Mansergas et al. (2007) and Bayless \& Orosz (2006) and the theoretical predicted values from Baraffe et al. (1998) are also shown.

### 6.6 Summary

From optical photometry we conclude SDSS1212-0123 is a eclipsing PCEB with an orbital period of 0.336 days and an eclipse length of 23 min . From spectroscopic follow-up observations we have derived a systemic velocity of $17 \pm 3 \mathrm{~km} / \mathrm{s}$ and a semi-amplitude of the radial velocity of $181 \pm 3 \mathrm{~km} / \mathrm{s}$. From the SDSS spectrum we derived $T_{\text {eff }}=17700 \pm 300 \mathrm{~K}, \log g=7.53 \pm 0.2$ implying a mass in the range $0.33-0.48 \mathrm{M}_{\odot}$ and a secondary spectral type $\mathrm{M} 4 \pm 1$, and a distance to the system of $230 \pm 20$ parsecs. From infrared photometry, using a mass-luminosity empirical relation we derived $M_{\text {sec }}=0.26 \pm 0.03 \mathrm{M}_{\odot}$. We have calculated the radius of the secondary star using an empirical mass-radius relation. The mass function, combined with the eclipse length, points towards the high end of the allowed mass range of the primary, i.e. $M_{\mathrm{wd}} \sim 0.46-0.48$, indicating it has a He core, one of the few know until the date. We have modeled the $I$ band light curve and find the inclination of the orbit to be $i>82^{\circ}$, and the masses to be consistent with previously determined values. The different methods applied are all consistent with $M_{\mathrm{wd}}=$ $0.46-0.48 \mathrm{M}_{\odot}$, implying $R_{\mathrm{wd}}=0.016-0.018 \mathrm{R}_{\odot}(\log g=7.5-7.7)$ for the primary and $M_{\text {sec }}=0.26-0.29 \mathrm{M}_{\odot}, R_{\text {sec }}=0.28-0.31 \mathrm{R}_{\odot}$ for the secondary. We have reconstructed and predicted the post CE evolution of SDSS1212-0123, finding that SDSS1212-0123 at the end of
the CE phase had a very similar orbital period. The only mechanism involved in shrinking the orbital period is and has been gravitational radiation. As the PCEB lifetime of SDSS1212-0123 exceeds the Hubble time we conclude that it is not representative of the progenitors of the current CV population. We collected data from other WDMS binaries with known masses and radii and see that for low masses the mass-radius relation is in agreement with the models, but for higher masses than $0.3 \mathrm{M}_{\odot}$ models and observations differ up to $15 \%$. The number of eclipsing systems, which give the most accurate parameters, is increasing, and with them we will be able to give a better empirical mass-radius relation.

## Chapter 7

## Conclusion and outlook

Before the era of the Sloan Digital Sky Survey only a few white dwarf/main sequence binaries were known. Due to the way these systems were discovered this sample was biased towards hot white dwarfs. Since then the number of WDMS binaries has been continuously increasing and has already reached more than 1600, where only a fraction of them have gone through a common envelope phase. Unfortunately these systems have also been biased towards systems containing hot white dwarfs. In this case the cause is that they were not one of the main targets of the SDSS but they were the byproduct of one of the main targets, quasars, and their colors resemble those of WDMS binaries with hot white dwarfs. As members of SEGUE, the Sloan Extension for Galactic Understanding and Exploration, a survey has been especially designed to identify WDMS binaries containing cold white dwarfs and covering a much broader range of galactic latitudes than SDSS I. In this work we present 277 new WDMS binaries and 24 candidates identified with SEGUE. We characterized the sample using spectral decomposition techniques, discussed the obtained distributions, and derived plausible values for the space density and the scale height. As expected, our sample contains significantly more cold systems than SDSS I. The combination of our color selection and the magnitude limits of SDSS causes our sample to be biased towards cold white dwarfs and late type secondary stars that are relatively nearby ( $d<500 \mathrm{pc}$ ). The space density of WDMS binaries inside our selection criteria is $\sim 2 \times 10^{-4} \mathrm{pc}^{-3}$ and decreases to $\sim 2 \times 10^{-5} \mathrm{pc}^{-3}$ at higher galactic latitudes. The space density of SDSS WDMS binaries increases significantly towards the galactic plane in agreement with a scale height of the galactic population of WDMS binaries of $100-150 \mathrm{pc}$, value that is similar to values estimated for the population of cataclysmic variables and late type stars.

Until 2003 only $\sim 30$ post common envelope binaries containing a white dwarf and a main sequence star with well determined parameters were known. Using the SDSS sub-exposures that are coadded to create a single SDSS spectrum, based on a statistical approach we discovered 33 new PCEBs. From own spectrocopic follow-up observations of 65 WDMS binaries we have independently confirmed 19 close binaries and combining with the mentioned SDSS sub-exposures we find a total number to 37 PCEBs. Willems \& Kolb (2004) predicted a fraction of PCEB to WDMS binaries of $\sim 25 \%$, while we found a value of $\sim 13 \%$. Nevertheless our result is just
a lower limit to the total number of PCEB in the sample which is not in contradiction with the theoretical predicted value. This becomes obvious when thinking that some systems will have a low orbital inclination so that no radial velocity variation can be measured within our detection limit.

One of the big questions of close binary evolution is whether a magnetized stellar wind is efficient extracting angular momentum for fully convective secondary stars, as it is for stars with a radiative core, or if this changes with the structure of the star. Politano \& Weiler (2006) proposed a test to answer this question. If magnetic braking gets disrupted the relative number of PCEBs should increase at the boundary where the star is fully convective, at around 0.35 $\mathrm{M}_{\odot}$, which corresponds to spectral type around M3, and towards later spectral types, i. e. lower masses. The SEGUE WMDS has been combined with a larger sample of WDMS-SDSS binaries to answer this question. We have found that the fraction of PCEBs to WDMS binaries is very low at early spectral type secondary stars, presents an steep increase to $\sim 50 \%$ at M3-M4, where the secondary becomes fully convective, and peaks at around M7, where $75 \%$ of the systems are PCEBs. This is the first test of magnetic braking and indicates that magnetic braking gets disrupted once the secondary star becomes fully convective.

The orbital period distribution of WDMS binaries predicted by Willems \& Kolb (2004) contains two groups. One formed by very long orbital period WDMS binaries where the components never interacted and evolved as single stars, and another, representing ~ $25 \%$ of the total WDMS binaries, formed by PCEBs. The latter extends from very short orbital periods up to 100 days, peaking at around 1 day. From own spectroscopic and photometric follow-up observations we have determined the orbital period of 15 systems among the 37 new PCEBs. Only one of them has an orbital period longer than 1 day. We studied our detection probability and found that even though we are biased towards systems with shorter orbital periods than 1 day we should be able to detect longer orbital periods as well. We made a compilation of all the known PCEBs until the date and realized that their orbital period distribution also presents a sharp cut at around 1 day. This seems to contradict the distribution predicted by Willems \& Kolb (2004) and Davis et al. (2009), which contains an extended tail of systems with orbital periods up to 100 days. This could imply that the CE phase might extract from the orbit more energy and angular momentum than previously thought. But one must not forget that the actual period distribution is biased towards short orbital periods, since their measurement is less time demanding than for those with longer orbital periods. Investigating in more detail the remaining 22 new SEGUE-PCEBs for which we don't have a measurement of the orbital period, we have identified 7 systems as long orbital period ( $>1$ day) candidates and 15 as short orbital period ( $<1$ day) candidates. To learn about the efficiency of the CE phase it is very important to measure their true orbital period.

All low mass white dwarf stars ( $M_{\mathrm{wd}}<0.47 \mathrm{M}_{\odot}$ ) are thought to be a product of close binary evolution (Marsh et al. 1995). In a single star wind mass loss wouldn't be strong enough so as to get rid of all the giant's envelope before the ignition of the He , while the existance of He -WDs can be explained with the ejection of the common envelope of a binary system. We investigated the white dwarf mass distribution of PCEBs and found that it is similar to that of single white dwarfs, presenting two peaks, one around $0.58 \mathrm{M}_{\odot}$ and the other around $0.84 \mathrm{M}_{\odot}$, but it has
an extended tail towards low masses. This is in agreement with the idea of all He core white dwarfs being product of a common envelope phase. Among the SEGUE sample there are 6 WDMS binaries for which the white dwarf mass is below the He-WD mass limit and that did not show any strong radial velocity variation. This seems to contradict the most likely evolutionary scenario for $\mathrm{He}-\mathrm{WD}$ stars.

The empirical mass-radius relation of low mass stars is in agreement with predicted values from models up to $0.3 \mathrm{M}_{\odot}$, but for higher masses models and observations seem to differ up to $15 \%$. Eclipsing systems give the most accurate parameters and can be used to give a better empirical mass-radius relation. We discovered 5 new eclipsing systems (Pyrzas et al. 2009; Nebot Gómez-Morán et al. 2009), and analyzed SDSS1212-0123 in detail. We estimated the masses and radii of the components with a 5\% accuracy. The estimated value of the white dwarf mass of SDSS1212-0123 suggests that it contains a He-core WD, which brings us back to the evolutionary scenario mentioned above. The number of eclipsing systems is still rather small and should be increased to improve the empirical radius-mass relation for low mass stars. Among the SEGUE sample we have found another new candidate for being eclipser and this should be observed photometrically to better constrain its stellar parameters and populate better the massradius diagram.

The activity-binarity relation is a field that has not been very much investigated among WDMS binaries. We have used our SEGUE-WDMS binaries, studying wide and close binaries separately in order to learn about possible connections. From the $\mathrm{H} \alpha$ emission line we have measured the stellar activity of the secondary stars. Wide binaries present an increase in the fraction of active secondary stars with spectral type, similar trend as found for field stars (West et al. 2008). At spectral types earlier than M4 the fraction of active stars is significantly higher than for field stars, and also higher than found before in WDMS wide binaries by Silvestri et al. (2005). To explain such effect we investigated the possibility of PCEB contamination in our wide binary sample at these spectral types and also calculated the age of the systems. We conclude that since most of the systems with secondaries in this spectral type range are younger than the activity lifetime it reflects an age effect. At least $90 \%$ of the PCEB are active pointing to an enhancement of activity due to the fact of having a companion star. The EW of the $\mathrm{H} \alpha$ line is higher for close systems at each spectral type for later spectral types than M2. But most of the close binary stars have a rather short orbital period, which when having a hot white dwarf as a primary could cause the secondary's surface to be heated, enhancing the $\mathrm{H} \alpha$ emission line. This needs to be investigated and a more detailed analysis based on a larger database is in progress and will give more light into the activity-binarity relation.

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## Appendix A

## Tables

Table A.1: Number of candidate, spectra taken according to our selection criteria, number of identified WDMS binaries, number of systems for which spectra were taken but are outside the selection criteria, success rate, galactic coordinates, space density, reddening and error on the density, for the 116 plate-pairs and 8 single plates with WDMS target selection that have been observed in SEGUE.

| Plate | $N_{\text {cand }}$ | $N_{\text {spec }}$ | $N_{\text {WDMS }}$ | $N_{\text {out }}$ | $\frac{\left(N_{\text {WDMS }}-N_{\text {out }}\right)}{N_{\text {spec }}}$ | $\frac{\left(N_{\text {WDMS }}-N_{\text {out }}\right)}{N_{\text {spec }}} * N_{\text {cand }}$ | 1 | \|b| | $\rho$ | $E(B-V)$ | $\sigma \rho$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2303/2318 | 31 | 3 | 0 | 0 | 0 | 0 | 21.999 | 31.00 | 0 | 0.113 | 0 |
| 2304/2319 | 3 | 1 | 1 | 0 | 1 | 3 | 41.947 | 206.64 | $2.13 \mathrm{e}-05$ | 0.038 | $2.13 \mathrm{e}-05$ |
| 2305/2320 | 9 | 1 | 0 | 0 | 0 | 0 | 36.654 | 44.84 | 0 | 0.227 | 0 |
| 2306/2321 | 1 | 1 | 1 | 0 | 1 | 1 | 50.928 | 156.16 | 7.10e-06 | 0.07 | 7.10e-06 |
| 2307/2322 | 2 | 2 | 1 | 0 | 0.5 | 1 | 44.606 | 171.39 | 7.10e-06 | 0.105 | 7.10e-06 |
| 2308/2323 | 6 | 2 | 1 | 1 | 0 | 0 | 38.777 | 67.76 | 0 | 0.101 | 0 |
| 2310/2325 | 2 | 1 | 2 | 2 | 0 | 0 | 46.371 | 80.43 | 0 | 0.07 | 0 |
| 2312/2327 | 2 | 1 | 1 | 0 | 1 | 2 | 55.193 | 116.28 | 1.42e-05 | 0.038 | 1.42e-05 |
| 2313/2328 | 4 | 4 | 2 | 1 | 0.25 | 1 | 62.582 | 131.95 | 7.10e-06 | 0.029 | 7.10e-06 |
| 2315/2330 | 3 | 1 | 2 | 1 | 1 | 3 | 31.957 | 199.78 | 2.13e-05 | 0.033 | 2.13e-05 |
| 2316/2331 | 3 | 3 | 4 | 1 | 1 | 3 | 37.195 | 164.26 | 2.13e-05 | 0.033 | $1.23 \mathrm{e}-05$ |
| 2317/2332 | 4 | 3 | 5 | 2 | 1 | 4 | 29.168 | 221.47 | 2.84e-05 | 0.055 | $1.64 \mathrm{e}-05$ |
| 2334/2339 | 4 | 4 | 1 | 0 | 0.25 | 1 | 40.799 | 177.71 | 7.10e-06 | 0.132 | 7.10e-06 |
| 2335/2340 | 3 | 1 | 0 | 0 | 0 | 0 | 42.745 | 174.65 | 0 | 0.201 | 0 |
| 2378/2398 | 9 | 5 | 3 | 0 | 0.6 | 5.4 | 22 | 150.00 | $3.84 \mathrm{e}-05$ | 0.118 | $2.21 \mathrm{e}-05$ |
| 2379/2399 | 2 | 2 | 1 | 1 | 0 | 0 | 32 | 150.00 | 0 | 0.114 | 0 |
| 2380/2400 | 4 | 3 | 2 | 0 | 0.66 | 2.66 | 40.307 | 185.88 | 1.89e-05 | 0.043 | 1.33e-05 |
| 2381/2401 | 7 | 4 | 4 | 0 | 1 | 7 | 43.491 | 195.57 | 4.97e-05 | 0.023 | $2.49 \mathrm{e}-05$ |
| 2382/2402 | 1 | 1 | 0 | 0 | 0 | 0 | 37.581 | 225.30 | 0 | 0.052 | 0 |
| 2383/2403 | 2 | 2 | 2 | 0 | 1 | 2 | 43.624 | 150.92 | 1.42e-05 | 0.029 | $1.00 \mathrm{e}-05$ |
| 2384/2404 | 3 | 3 | 3 | 0 | 1 | 3 | 46.196 | 163.48 | 2.13e-05 | 0.014 | $1.23 \mathrm{e}-05$ |
| 2386/2406 | 5 | 5 | 4 | 0 | 0.8 | 4 | 53.919 | 205.39 | 2.84e-05 | 0.029 | $1.42 \mathrm{e}-05$ |
| 2387/2407 | 4 | 4 | 3 | 0 | 0.75 | 3 | 54.796 | 189.36 | 2.13e-05 | 0.013 | $1.23 \mathrm{e}-05$ |
| 2389/2409 | 2 | 1 | 1 | 0 | 1 | 2 | 49.817 | 250.28 | 1.42e-05 | 0.039 | 1.42e-05 |
| 2390/2410 | 6 | 5 | 5 | 0 | 1 | 6 | 59.243 | 162.38 | 4.26e-05 | 0.016 | 1.91e-05 |
| 2393/2413 | 4 | 3 | 2 | 0 | 0.66 | 2.66 | 61.303 | 245.98 | $1.89 \mathrm{e}-05$ | 0.023 | $1.34 \mathrm{e}-05$ |
| 2394/2414 | 6 | 3 | 3 | 0 | 1 | 6 | 54.158 | 143.49 | 4.26e-05 | 0.009 | 2.46e-05 |
| 2397/2417 | 11 | 3 | 3 | 3 | 0 | 0 | 14.001 | 150.00 | 0 | 0.127 | 0 |
| 2441/2443 | 5 | 5 | 3 | 0 | 0.6 | 3 | 18 | 150.00 | 2.13e-05 | 0.119 | 1.23e-05 |
| 2442/2444 | 2 | 2 | 2 | 0 | 1 | 2 | 29 | 150.00 | 1.42e-05 | 0.136 | $1.00 \mathrm{e}-05$ |
| 2445/2460 | 3 | 3 | 4 | 1 | 1 | 3 | 50.16 | 116.77 | 2.13e-05 | 0.02 | $1.23 \mathrm{e}-05$ |
| 2446/2461 | 4 | 3 | 3 | 0 | 1 | 4 | 57.369 | 122.84 | 2.84e-05 | 0.012 | $1.64 \mathrm{e}-05$ |
| 2447/2462 | 2 | 2 | 2 | 0 | 1 | 2 | 56.812 | 100.68 | 1.42e-05 | 0.015 | $1.00 \mathrm{e}-05$ |

Table A.1: continued.

| plate | $N_{\text {cand }}$ | $N_{\text {spec }}$ | $N_{\text {WDMS }}$ | $N_{\text {out }}$ | $\frac{\left(N_{\text {WDMS }}-N_{\text {out }}\right)}{N_{\text {spec }}}$ | $\frac{\left(N_{\text {WDMS }}-N_{\text {out }}\right)}{N_{\text {spec }}} * N_{\text {cand }}$ | 1 | $\|b\|$ | $\rho$ | $E(B-V)$ | $\sigma \rho$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2449/2464 | 6 | 5 | 4 | 0 | 0.8 | 4.8 | 52.657 | 81.08 | $3.41 \mathrm{e}-05$ | 0.018 | $1.70 \mathrm{e}-05$ |
| 2452/2467 | 1 | 1 | 1 | 0 | 1 | 1 | 74.5 | 154.34 | $7.10 \mathrm{e}-06$ | 0.028 | $7.10 \mathrm{e}-06$ |
| 2457/2472 | 1 | 1 | 1 | 0 | 1 | 1 | 87.02 | 147.00 | 7.10e-06 | 0.016 | $7.10 \mathrm{e}-06$ |
| 2459/2474 | 4 | 4 | 2 | 0 | 0.5 | 2 | 49.491 | 42.88 | $1.42 \mathrm{e}-05$ | 0.041 | $1.00 \mathrm{e}-05$ |
| 2537/2545 | 366 | 1 | 0 | 0 | 0 | 0 | 10.5 | 110.00 | 0 | 0.478 | 0 |
| 2538/2546 | 429 | 21 | 0 | 0 | 0 | 0 | 16 | 110.00 | 0 | 0.525 | 0 |
| 2539/2547 | 9 | 8 | 6 | 0 | 0.75 | 6.75 | 54.362 | 100.60 | $4.79 \mathrm{e}-05$ | 0.012 | $1.96 \mathrm{e}-05$ |
| 2540/2548 | 6 | 5 | 3 | 0 | 0.6 | 3.6 | 25.711 | 130.00 | $2.56 \mathrm{e}-05$ | 0.056 | $1.48 \mathrm{e}-05$ |
| 2541/2549 | 8 | 5 | 4 | 0 | 0.8 | 6.4 | 29.71 | 130.00 | $4.55 \mathrm{e}-05$ | 0.031 | $2.27 \mathrm{e}-05$ |
| 2551/2561 | 5 | 4 | 3 | 0 | 0.75 | 3.75 | 33 | 94.00 | $2.66 \mathrm{e}-05$ | 0.025 | $1.54 \mathrm{e}-05$ |
| 2553/2563 | 6 | 4 | 2 | 0 | 0.5 | 3 | 20 | 94.00 | $2.13 \mathrm{e}-05$ | 0.045 | $1.51 \mathrm{e}-05$ |
| 2554/2564 | 17 | 1 | 1 | 0 | 1 | 17 | 14 | 94.00 | $1.21 \mathrm{e}-04$ | 0.219 | $1.20 \mathrm{e}-04$ |
| 2555/2565 | 914 | 16 | 0 | 0 | 0 | 0 | 8 | 94.00 | 0 | 0.927 | 0 |
| 2556/2566 | 272 | 3 | 0 | 0 | 0 | 0 | 8 | 94.00 | 0 | 0.297 | 0 |
| 2557/2567 | 4 | 3 | 2 | 0 | 0.66 | 2.66 | 57.629 | 171.74 | $1.89 \mathrm{e}-05$ | 0.017 | $1.34 \mathrm{e}-05$ |
| 2558/2568 | 4 | 4 | 1 | 0 | 0.25 | 1 | 62.082 | 288.15 | $7.10 \mathrm{e}-06$ | 0.029 | $7.10 \mathrm{e}-06$ |
| 2559/2569 | 2 | 1 | 0 | 0 | 0 | 0 | 49.817 | 250.28 | 0 | 0.039 | 0 |
| 2621/2627 | 4 | 4 | 3 | 0 | 0.75 | 3 | 25 | 94.00 | $2.13 \mathrm{e}-05$ | 0.053 | $1.23 \mathrm{e}-05$ |
| 2622/2628 | 6 | 4 | 3 | 0 | 0.75 | 4.5 | 50 | 94.00 | $3.20 \mathrm{e}-05$ | 0.131 | $1.85 \mathrm{e}-05$ |
| 2623/2629 | 3 | 3 | 2 | 0 | 0.66 | 2 | 35 | 94.00 | $1.42 \mathrm{e}-05$ | 0.171 | $1.00 \mathrm{e}-05$ |
| 2624/2630 | 4 | 4 | 4 | 0 | 1 | 4 | 65 | 94.00 | $2.84 \mathrm{e}-05$ | 0.034 | $1.42 \mathrm{e}-05$ |
| 2667/2671 | 7 | 4 | 1 | 0 | 0.25 | 1.75 | 31.529 | 216.61 | $1.24 \mathrm{e}-05$ | 0.045 | $1.24 \mathrm{e}-05$ |
| 2668/2672 | 15 | 1 | 0 | 0 | 0 | 0 | 12 | 187.00 | 0 | 0.46 | 0 |
| 2669/2673 | 29 | 4 | 0 | 0 | 0 | 0 | 22 | 187.00 | 0 | 0.379 | 0 |
| 2670/2674 | 2 | 1 | 1 | 0 | 1 | 2 | 32.64 | 183.37 | $1.42 \mathrm{e}-05$ | 0.04 | $1.42 \mathrm{e}-05$ |
| 2676/2694 | 21 | 3 | 0 | 0 | 0 | 0 | 12 | 187.00 | 0 | 0.093 | 0 |
| 2677/2695 | 9 | 3 | 2 | 0 | 0.66 | 6 | 20 | 187.00 | 4.26e-05 | 0.076 | $3.01 \mathrm{e}-05$ |
| 2678/2696 | 59 | 1 | 0 | 0 | 0 | 0 | 8 | 187.00 | 0 | 0.23 | 0 |
| 2680/2698 | 76 | 7 | 0 | 0 | 0 | 0 | 25 | 178.00 | 0 | 0.441 | 0 |
| 2681/2699 | 68 | 1 | 1 | 0 | 1 | 68 | 15.001 | 178.00 | 4.83e-04 | 0.495 | $4.83 \mathrm{e}-04$ |
| 2682/2700 | 21 | 4 | 2 | 0 | 0.5 | 10.5 | 15 | 178.00 | 7.46e-05 | 0.143 | $5.27 \mathrm{e}-05$ |
| 2683/2701 | 8 | 4 | 3 | 0 | 0.75 | 6 | 25 | 178.00 | $4.26 \mathrm{e}-05$ | 0.052 | $2.46 \mathrm{e}-05$ |
| 2689/2707 | 3 | 3 | 3 | 0 | 1 | 3 | 55 | 300 | $2.13 \mathrm{e}-05$ | 0.026 | $1.23 \mathrm{e}-05$ |
| 2690/2708 | 6 | 6 | 4 | 0 | 0.66 | 4 | 40 | 270.00 | $2.84 \mathrm{e}-05$ | 0.068 | $1.42 \mathrm{e}-05$ |
| 2714/2729 | 7 | 4 | 3 | 0 | 0.75 | 5.25 | 21.5 | 203.00 | $3.73 \mathrm{e}-05$ | 0.043 | $2.15 \mathrm{e}-05$ |
| 2724/2739 | 5 | 4 | 3 | 0 | 0.75 | 3.75 | 50.001 | 9.84 | $2.66 \mathrm{e}-05$ | 0.036 | $1.54 \mathrm{e}-05$ |
| 2797/2818 | 27 | 7 | 3 | 0 | 0.43 | 11.57 | 21.75 | 31.00 | $8.22 \mathrm{e}-05$ | 0.107 | $4.75 \mathrm{e}-05$ |
| 2798/2819 | 22 | 5 | 4 | 0 | 0.8 | 17.6 | 20 | 70.00 | $1.25 \mathrm{e}-04$ | 0.07 | $6.25 \mathrm{e}-05$ |
| 2800/2821 | 79 | 7 | 2 | 0 | 0.28 | 22.57 | 10.618 | 70.00 | $1.60 \mathrm{e}-04$ | 0.154 | $1.13 \mathrm{e}-04$ |
| 2801/2822 | 4 | 3 | 2 | 0 | 0.66 | 2.66 | 36.73 | 109.77 | $1.89 \mathrm{e}-05$ | 0.067 | $1.34 \mathrm{e}-05$ |
| 2803/2824 | 6 | 3 | 3 | 1 | 0.66 | 4 | 33.5 | 110.00 | $2.84 \mathrm{e}-05$ | 0.051 | $2.01 \mathrm{e}-05$ |
| 2805/2826 | 6 | 3 | 2 | 0 | 0.66 | 4 | 29.5 | 187.00 | $2.84 \mathrm{e}-05$ | 0.226 | $2.01 \mathrm{e}-05$ |
| 2806/2827 | 96 | 7 | 0 | 0 | 0 | 0 | 14 | 229.00 | 0 | 0.099 | 0 |
| 2807/2828 | 6 | 4 | 4 | 0 | 1 | 6 | 20 | 229.00 | 4.26e-05 | 0.038 | $2.13 \mathrm{e}-05$ |
| 2812/2833 | 2091 | 25 | 1 | 0 | 0.04 | 83.64 | 8 | 50.00 | 5.94e-04 | 0.391 | 5.94e-04 |
| 2849/2864 | 2 | 2 | 1 | 0 | 0.5 | 1 | 71.741 | 141.60 | 7.10e-06 | 0.042 | $7.10 \mathrm{e}-06$ |
| 2852/2867 | 4 | 2 | 2 | 0 | 1 | 4 | 40.721 | 239.10 | $2.84 \mathrm{e}-05$ | 0.035 | $2.01 \mathrm{e}-05$ |
| 2853/2868 | 6 | 5 | 4 | 0 | 0.8 | 4.8 | 55.272 | 220.87 | $3.41 \mathrm{e}-05$ | 0.026 | 1.70e-05 |
| 2854/2869 | 8 | 5 | 3 | 0 | 0.6 | 4.8 | 51.204 | 234.18 | $3.41 \mathrm{e}-05$ | 0.033 | $1.97 \mathrm{e}-05$ |
| 2855/2870 | 6 | 5 | 5 | 0 | 1 | 6 | 65.867 | 203.12 | $4.26 \mathrm{e}-05$ | 0.032 | $1.91 \mathrm{e}-05$ |
| 2856/2871 | 4 | 4 | 3 | 0 | 0.75 | 3 | 65.54 | 178.45 | $2.13 \mathrm{e}-05$ | 0.021 | $1.23 \mathrm{e}-05$ |
| 2857/2872 | 3 | 3 | 3 | 0 | 1 | 3 | 66.835 | 227.63 | $2.13 \mathrm{e}-05$ | 0.02 | $1.23 \mathrm{e}-05$ |
| 2858/2873 | 6 | 5 | 5 | 0 | 1 | 6 | 48.173 | 134.92 | $4.26 \mathrm{e}-05$ | 0.008 | $1.91 \mathrm{e}-05$ |
| 2859/2874 | 6 | 5 | 5 | 0 | 1 | 6 | 45 | 270.00 | $4.26 \mathrm{e}-05$ | 0.065 | $1.91 \mathrm{e}-05$ |
| 2861/2876 | 1 | 1 | 1 | 0 | 1 | 1 | 50 | 270.00 | $7.10 \mathrm{e}-06$ | 0.038 | $7.10 \mathrm{e}-06$ |
| 2862/2877 | 5 | 2 | 3 | 1 | 1 | 5 | 57.374 | 266.09 | 3.55e-05 | 0.024 | $2.51 \mathrm{e}-05$ |
| 2887/2912 | 4207 | 12 | 0 | 0 | 0 | 0 | 0.999 | 187.00 | 0 | 0.775 | 0 |
| 2888/2913 | 4 | 3 | 3 | 0 | 1 | 4 | 29.011 | 225.20 | $2.84 \mathrm{e}-05$ | 0.037 | $1.64 \mathrm{e}-05$ |

Table A.1: continued.

| plate | $N_{\text {cand }}$ | $N_{\text {spec }}$ | $N_{\text {WDMS }}$ | $N_{\text {out }}$ | $\frac{\left(N_{\text {WDMS }}-N_{\text {out }}\right)}{N_{\text {spec }}}$ | $\frac{\left(N_{\text {WDMS }}-N_{\text {out }}\right)}{N_{\text {spec }}} * N_{\text {cand }}$ | 1 | $\|b\|$ | $\rho$ | $E(B-V)$ | $\sigma \rho$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2889/2914 | 1 | 1 | 1 | 0 | 1 | 1 | 47.321 | 197.01 | $7.10 \mathrm{e}-06$ | 0.017 | $7.10 \mathrm{e}-06$ |
| 2890/2915 | 12 | 5 | 4 | 0 | 0.8 | 9.6 | 19.589 | 201.85 | 6.82e-05 | 0.032 | $3.41 \mathrm{e}-05$ |
| 2891/2916 | 4 | 4 | 3 | 0 | 0.75 | 3 | 23.159 | 197.73 | $2.13 \mathrm{e}-05$ | 0.067 | $1.23 \mathrm{e}-05$ |
| 2893/2918 | 3 | 2 | 2 | 0 | 1 | 3 | 77.606 | 245.85 | $2.13 \mathrm{e}-05$ | 0.027 | $1.51 \mathrm{e}-05$ |
| 2894/2919 | 4 | 3 | 2 | 0 | 0.66 | 2.66 | 65.671 | 140.22 | $1.89 \mathrm{e}-05$ | 0.025 | $1.34 \mathrm{e}-05$ |
| 2895/2920 | 2 | 2 | 2 | 0 | 1 | 2 | 62.619 | 294.52 | $1.42 \mathrm{e}-05$ | 0.019 | $1.00 \mathrm{e}-05$ |
| 2897/2922 | 3 | 1 | 1 | 0 | 1 | 3 | 60.318 | 299.18 | $2.13 \mathrm{e}-05$ | 0.032 | $2.13 \mathrm{e}-05$ |
| 2898/2923 | 5 | 5 | 2 | 0 | 0.4 | 2 | 67.387 | 123.12 | $1.42 \mathrm{e}-05$ | 0.013 | $1.00 \mathrm{e}-05$ |
| 2899/2924 | 3 | 3 | 2 | 0 | 0.66 | 2 | 82.452 | 315.26 | $1.42 \mathrm{e}-05$ | 0.022 | $1.00 \mathrm{e}-05$ |
| 2901/2926 | 6 | 4 | 4 | 0 | 1 | 6 | 62.426 | 314.09 | $4.26 \mathrm{e}-05$ | 0.037 | $2.13 \mathrm{e}-05$ |
| 2902/2927 | 5 | 4 | 1 | 0 | 0.25 | 1.25 | 50.001 | 9.84 | 8.88e-06 | 0.036 | $8.88 \mathrm{e}-06$ |
| 2903/2928 | 7 | 4 | 3 | 0 | 0.75 | 5.25 | 68.734 | 338.75 | $3.73 \mathrm{e}-05$ | 0.026 | $2.15 \mathrm{e}-05$ |
| 2904/2929 | 6 | 5 | 2 | 0 | 0.4 | 2.4 | 77.716 | 41.12 | $1.70 \mathrm{e}-05$ | 0.014 | $1.21 \mathrm{e}-05$ |
| 2905/2930 | 6 | 5 | 4 | 0 | 0.8 | 4.8 | 74.29 | 3.16 | $3.41 \mathrm{e}-05$ | 0.024 | $1.70 \mathrm{e}-05$ |
| 2906/2931 | 4 | 4 | 4 | 0 | 1 | 4 | 70.654 | 67.14 | $2.84 \mathrm{e}-05$ | 0.009 | $1.42 \mathrm{e}-05$ |
| 2907/2932 | 4 | 4 | 2 | 0 | 0.5 | 2 | 63.494 | 82.47 | $1.42 \mathrm{e}-05$ | 0.01 | $1.00 \mathrm{e}-05$ |
| 2908/2933 | 5 | 5 | 4 | 0 | 0.8 | 4 | 60.221 | 358.72 | $2.84 \mathrm{e}-05$ | 0.023 | $1.42 \mathrm{e}-05$ |
| 2909/2934 | 3 | 3 | 3 | 0 | 1 | 3 | 51.018 | 353.65 | $2.13 \mathrm{e}-05$ | 0.043 | $1.23 \mathrm{e}-05$ |
| 2910/2935 | 1 | 1 | 1 | 0 | 1 | 1 | 60.569 | 51.02 | 7.10e-06 | 0.022 | $7.10 \mathrm{e}-06$ |
| 2911/2936 | 3 | 2 | 1 | 0 | 0.5 | 1.5 | 55.839 | 63.98 | $1.06 \mathrm{e}-05$ | 0.023 | $1.07 \mathrm{e}-05$ |
| 2938/2943 | 10 | 3 | 3 | 0 | 1 | 10 | 19.999 | 178.00 | $7.10 \mathrm{e}-05$ | 0.066 | $4.10 \mathrm{e}-05$ |
| 2939/2944 | 2 | 2 | 2 | 0 | 1 | 2 | 30 | 150.00 | $1.42 \mathrm{e}-05$ | 0.04 | $1.00 \mathrm{e}-05$ |
| 2940/2945 | 8 | 3 | 1 | 0 | 0.33 | 2.66 | 18.619 | 211.61 | $1.89 \mathrm{e}-05$ | 0.019 | $1.89 \mathrm{e}-05$ |
| 2941/2946 | 4 | 4 | 4 | 1 | 0.75 | 3 | 22.441 | 180.89 | $2.13 \mathrm{e}-05$ | 0.052 | $1.23 \mathrm{e}-05$ |
| 2963/2965 | 3 | 3 | 2 | 1 | 0.33 | 1 | 72.77 | 303.81 | $7.10 \mathrm{e}-06$ | 0.023 | $7.10 \mathrm{e}-06$ |
| 2336 | 9 | 3 | 1 | 0 | 0.33 | 3 | 22.786 | 130.00 | $2.13 \mathrm{e}-05$ | 0.067 | $2.13 \mathrm{e}-05$ |
| 2337 | 4 | 1 | 1 | 0 | 1 | 4 | 25.938 | 150.00 | $2.84 \mathrm{e}-05$ | 0.035 | $2.84 \mathrm{e}-05$ |
| 2475 | 5 | 1 | 0 | 0 | 0 | 0 | 78.701 | 42.31 | 0 | 0.013 | 0 |
| 2552 | 10 | 1 | 1 | 0 | 1 | 10 | 26 | 94.00 | $7.10 \mathrm{e}-05$ | 0.044 | $7.10 \mathrm{e}-05$ |
| 2620 | 20 | 1 | 1 | 0 | 1 | 20 | 15 | 94.00 | $1.42 \mathrm{e}-04$ | 0.125 | $1.42 \mathrm{e}-04$ |
| 2865 | 7 | 4 | 2 | 0 | 0.5 | 3.5 | 68.734 | 158.75 | $2.49 \mathrm{e}-05$ | 0.028 | $1.76 \mathrm{e}-05$ |
| 2866 | 2 | 2 | 1 | 0 | 0.5 | 1 | 58.262 | 157.01 | $7.10 \mathrm{e}-06$ | 0.03 | $7.10 \mathrm{e}-06$ |
| 2942 | 9 | 5 | 2 | 0 | 0.4 | 3.6 | 30.485 | 203 | $2.55 \mathrm{e}-05$ | 0.07 | $1.81 \mathrm{e}-05$ |

Table A.2: Plate number, Fiber number, MJD of the observation, and ugriz colors of the 301 WDMS and WDMS candidate systems identified with SEGUE.

| System | Plate | Fiber | MJD | u | $\sigma_{u}$ | g | $\sigma_{g}$ | r | $\sigma_{r}$ | i | $\sigma_{i}$ | Z | $\sigma_{z}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $000250.64-045041.6$ | 2630 | 439 | 54327 | 19.846 | 0.042 | 19.728 | 0.021 | 19.464 | 0.018 | 18.569 | 0.015 | 17.903 | 0.022 |
| $000356.93-050332.7$ | 2630 | 173 | 54327 | 18.522 | 0.022 | 18.203 | 0.027 | 18.152 | 0.013 | 17.503 | 0.013 | 16.883 | 0.018 |
| $000453.93+265420.4$ | 2824 | 78 | 54452 | 19.935 | 0.046 | 19.596 | 0.025 | 19.436 | 0.017 | 18.846 | 0.023 | 18.345 | 0.043 |
| $000504.91+243409.6$ | 2822 | 180 | 54389 | 19.513 | 0.035 | 18.895 | 0.014 | 18.486 | 0.013 | 17.503 | 0.014 | 16.766 | 0.018 |
| $000531.09-054343.2$ | 2624 | 82 | 54380 | 17.282 | 0.016 | 16.727 | 0.013 | 16.599 | 0.013 | 15.807 | 0.013 | 15.098 | 0.012 |
| $000559.87-054416.0$ | 2624 | 60 | 54380 | 18.561 | 0.024 | 18.321 | 0.012 | 17.756 | 0.013 | 17.070 | 0.014 | 16.619 | 0.017 |
| $006651.91+284647.1$ | 2824 | 601 | 54452 | 19.271 | 0.033 | 18.665 | 0.020 | 18.247 | 0.015 | 17.146 | 0.016 | 16.470 | 0.014 |
| $000829.92+273340.5$ | 2824 | 1 | 54452 | 19.599 | 0.045 | 18.943 | 0.020 | 18.223 | 0.016 | 17.301 | 0.018 | 16.763 | 0.038 |
| $000935.50+243251.2$ | 2822 | 62 | 54389 | 20.293 | 0.051 | 18.966 | 0.017 | 17.776 | 0.012 | 16.856 | 0.018 | 16.337 | 0.016 |
| $003804.41+083416.9$ | 2312 | 576 | 53709 | 19.373 | 0.033 | 18.053 | 0.020 | 16.951 | 0.013 | 15.872 | 0.016 | 15.272 | 0.018 |
| $010341.59+003132.6$ | 2328 | 385 | 53728 | 19.354 | 0.032 | 19.114 | 0.025 | 18.822 | 0.024 | 18.130 | 0.017 | 17.628 | 0.032 |
| $010448.50-010516.7$ | 2313 | 241 | 53726 | 20.167 | 0.060 | 18.656 | 0.021 | 17.458 | 0.014 | 16.207 | 0.012 | 15.554 | 0.010 |
| $010704.58+005907.9$ | 2328 | 416 | 53728 | 21.780 | 0.220 | 19.851 | 0.030 | 18.626 | 0.013 | 17.748 | 0.011 | 17.264 | 0.020 |
| $01123.90+000935.2$ | 2328 | 594 | 53728 | 19.022 | 0.029 | 18.475 | 0.030 | 17.890 | 0.023 | 17.068 | 0.018 | 16.512 | 0.017 |
| $011932.38-090219.1$ | 2864 | 615 | 54467 | 19.909 | 0.046 | 19.280 | 0.019 | 18.421 | 0.016 | 17.582 | 0.011 | 17.088 | 0.017 |
| $013000.74+385205.4$ | 2336 | 7 | 53712 | 20.128 | 0.039 | 19.030 | 0.017 | 17.935 | 0.011 | 17.203 | 0.013 | 16.762 | 0.016 |
| $014143.68-093811.7$ | 2865 | 170 | 54497 | 19.663 | 0.037 | 19.377 | 0.022 | 18.931 | 0.015 | 18.072 | 0.019 | 17.435 | 0.022 |
| $014147.33-094200.3$ | 2865 | 165 | 54497 | 21.690 | 0.176 | 19.990 | 0.025 | 18.795 | 0.014 | 17.581 | 0.018 | 16.914 | 0.018 |

Table A.2: continued.

| System (SDSSJ) | Plate | Fiber |  | u | $\sigma_{u}$ | g |  |  | $\sigma_{r}$ |  | $\sigma_{i}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 014232.59-083528 | 2865 | 525 | 54497 | 19.501 | 0.037 | 18.819 | 0.024 | 8.082 | 0.013 | 7.040 | 0.013 | 6.348 | 016 |
| 020351.29+004025.0 | 2866 | 636 | 54478 | 20.343 | 0.050 | 19.430 | 0.023 | 18.682 | 0.017 | 17.625 | 0.019 | 16.990 | 0.017 |
| 1145.57+071831.1 | 2321 | 460 | 53711 | 19.816 | 0.035 | 19.468 | 0.025 | 19.081 | 0.023 | 18.161 | 0.022 | 17.457 | 0.014 |
| $3438.48+244535.6$ | 2399 | 75 | 53764 | 21.155 | 0.108 | 20.012 | 0.021 | 18.851 | 0.016 | 18.040 | 0.015 | 17.524 | 0.017 |
| $3526.43+280026.6$ | 2444 | 22 | 54082 | 19.963 | 0.044 | 19.689 | 0.152 | 19.110 | 0.308 | 18.365 | 0.386 | 17.875 | 0.307 |
| 04+273654.0 | 2 | 149 | 54082 | 20.013 | 0.051 | 19.312 | 0.016 | 19.214 | 0.015 | 18.63 | . 22 | 17.961 | . 021 |
| $024942.92+335032.5$ | 23 | 256 | 53768 | 20.400 | 0.054 | 19.459 | 0.018 | 18.277 | 0.012 | 17.504 | 0.010 | 17.028 | 0.015 |
| $025347.51+335221.0$ | 2378 | 172 | 53759 | 19.802 | 0.040 | 18.947 | 0.013 | 17.972 | 0.009 | 17.099 | 0.008 | 16.518 | 0.016 |
| $25555.87+352830.2$ | 2378 | 538 | 53759 | 18.370 | 0.023 | 17.559 | 0.014 | 16.519 | 0.009 | 15.550 | 0.008 | 14.992 | . 013 |
| 20138.24+050218.9 | 2307 | 140 | 53710 | 19.111 | 0.026 | 18.388 | 0.023 | 18.048 | 0.013 | 17.272 | 0.017 | 16.606 | 0.016 |
| $247.65+372125.9$ | 2443 | 185 | 54082 | 20.634 | 0.071 | 19.589 | 0.014 | 18.444 | 0.012 | 17.749 | 0.012 | 17.367 | 0.018 |
| 716.44+384822.8 | 2441 | 564 | 54065 | 20.642 | 0.075 | 19.039 | 0.126 | 17.861 | 0.316 | 16.698 | 0.201 | 16.056 | 0.122 |
| 0900.89+384835.2 | 2443 | 04 | 54082 | 20.318 | 0.049 | 19.873 | 0.016 | 19.424 | 0.014 | 18.339 | 0.013 | 17.551 | 0.018 |
| $30956.31+411049.2$ | 2397 | 255 | 53763 | 24.598 | 1.009 | 18.405 | 0.030 | 16.976 | 0.014 | 15.777 | 0.012 | 14.979 | 0.009 |
| 31200.17+401336.9 | 2417 | 259 | 53766 | 21.550 | 0.134 | 20.016 | 0.018 | 19.102 | 0.013 | 18.401 | 0.015 | 17.937 | 0.021 |
| 1657.47+395931.9 | 2397 | 69 | 53763 | 20.682 | 0.064 | 18.898 | 0.013 | 17.871 | 0.011 | 17.135 | 0.009 | 16.633 | 0.012 |
| $1803.98+423034.4$ | 2397 | 582 | 53763 | 18.409 | 0.025 | 17.199 | 0.013 | 16.252 | 0.008 | 15.185 | 0.011 | 14.507 | 0.012 |
| 2030.52+044243.5 | 2334 | 261 | 53730 | 18.450 | 0.026 | 18.213 | 0.017 | 17.918 | 0.012 | 16.988 | 0.015 | 16.257 | 0.014 |
| $40.00+415307.5$ | 2417 | 63 | 5376 | 21.078 | 0.135 | 20.582 | 0.076 | 19.490 | 0.024 | 18.345 | 0.013 | 17.674 | 0.018 |
| 4913.69+085810.8 | 2697 | 95 | 89 | 20.481 | 0.056 | 19.828 | 0.029 | 18.942 | 0.019 | 17.994 | 0.018 | 17.345 | . 22 |
| 41716.58+055522.4 | 2826 | 225 | 54389 | 20.108 | 0.043 | 19.913 | 0.017 | 19.585 | 0.016 | 18.846 | 0.016 | 18.253 | 26 |
| 42053.72+064922.4 | 2826 | 526 | 54389 | 20.922 | 0.071 | 19.755 | 0.019 | 18.655 | 0.012 | 17.165 | 0.012 | 16.231 | . 013 |
| 044046.91-050413.0 | 2942 | 333 | 54521 | 19.703 | 0.044 | 19.348 | 0.014 | 19.144 | 0.017 | 18.267 | 0.017 | 17.548 | 0.018 |
| 4218.26-044820.2 | 2942 | 323 | 54521 | 19.958 | 0.051 | 19.141 | 0.016 | 18.420 | 0.013 | 17.398 | 0.013 | 16.787 | . 015 |
| 044547.53-044559.1 | 2942 | 460 | 545 | 20. | 0.097 | 19.265 | 0.015 | 18.295 | 0.0 | 17.776 | 0.017 | 86 | 19 |
| $2+21490$ | 2681 | 52 | 54397 | 19. | 0.030 | 18.546 | 0.013 | 17.652 | . 07 | 16.62 | 0.009 | .916 | . 013 |
| $054544.63+822205.9$ | 2540 | 249 | 54110 | 19.615 | 0.037 | 17.431 | 0.013 | 16.438 | 0.013 | 15.76 | 0.016 | 15.385 | 15 |
| 055956.76+224704.6 | 2887 | 270 | 54521 | 20.923 | 0.089 | 18.873 | 0.012 | 17.880 | 0.007 | 17.338 | 0.012 | 16.970 | 0.019 |
| $063139.13+822827.8$ | 2548 | 1 | 54152 | 19.286 | 0.031 | 19.084 | 0.020 | 18.819 | 0.018 | 17.956 | 0.018 | 17.333 | 0.026 |
| 63805.21+835526.9 | 2548 | 2 | 54152 | 19.537 | 0.044 | 19.321 | 0.021 | 19.475 | 0.021 | 18.896 | 0.020 | 18.220 | . 038 |
| $147.70+3640$ | 2682 | 201 | 54401 | 20.483 | 0.049 | 18.816 | 0.010 | 17.874 | 0.009 | 17.171 | 0.012 | 65 | . 013 |
| 16 | 270 | 372 | 544 | 19. | 0.041 | 19.096 | 0.011 | 18.670 | 0.011 | 17.703 | 0.0 | 41 | . 18 |
| $23.99+840724.1$ | 2548 | 611 | 54152 | 19.98 | 0.050 | 19.4 | 0.021 | 19.17 | 0.017 | 18.4 | 0.0 | 17.942 | . 30 |
| 064812.76+381005.9 | 2682 | 519 | 54401 | 19.733 | 0.033 | 18.988 | 0.010 | 17.964 | 0.012 | 17.220 | 0.010 | 16.803 | 0.015 |
| 070322.17+664908.0 | 2337 | 419 | 53740 | 19.973 | 0.044 | 18.642 | 0.019 | 17.512 | 0.011 | 16.366 | 0.016 | 15.712 | 0.020 |
| 070336.89+385142.2 | 2943 | 263 | 54502 | 20.845 | 0.056 | 19.940 | 0.013 | 19.009 | 0.010 | 17.965 | 0.012 | 17.369 | 0.016 |
| $70628.57+383650.2$ | 2943 | 04 | 54502 | 20.217 | 0.049 | 19.412 | 0.016 | 18.507 | 0.011 | 17.554 | 0.015 | 16.984 | 0.016 |
| $1309.72+401249.4$ | 2943 | 15 | 54502 | 19.897 | 0.040 | 19.082 | 0.013 | 18.342 | 0.011 | 17.401 | 0.012 | 16.825 | 0.015 |
| 016.98+303824.6 | 2677 | 60 | 54180 | 20.78 | 0.067 | 18.810 | 0.011 | 17.672 | 0.011 | 16.441 | 0.016 | 15.820 | 0.013 |
| $072130.60+374228.3$ | 2946 | 439 | 54506 | 20.467 | 0.054 | 19.791 | 0.020 | 19.455 | 0.017 | 18.363 | 0.015 | 17.697 | 0.023 |
| $072156.68+364048.5$ | 2946 | 247 | 54506 | 19.526 | 0.033 | 17.865 | 0.010 | 16.697 | 0.007 | 15.959 | 0.018 | 15.557 | 0.020 |
| 072222.66+385702.9 | 2946 | 322 | 54506 | 19.223 | 0.031 | 17.533 | 0.018 | 16.269 | 0.011 | 15.521 | 0.017 | 15.101 | 0.014 |
| 072251.06+385944.6 | 2946 | 376 | 54506 | 19.997 | 0.048 | 19.068 | 0.021 | 18.269 | 0.013 | 17.002 | 0.010 | 16.231 | 0.014 |
| 2434.72+321609.4 | 2677 | 535 | 54180 | 18.815 | 0.023 | 18.066 | 0.012 | 17.434 | 0.009 | 16.259 | 0.011 | 15.558 | 0.016 |
| $2635.37+322554.3$ | 2695 | 568 | 54409 | 19.701 | 0.031 | 19.212 | 0.015 | 18.677 | 0.011 | 17.811 | 0.013 | 17.276 | 0.015 |
| 3003.87+405450.1 | 2683 | 20 | 54153 | 19.633 | 0.032 | 18.495 | 0.014 | 17.399 | 0.018 | 16.19 | 0.013 | 15.475 | 0.019 |
| 073059.83+144052.0 | 2713 | 203 | 54397 | 19.035 | 0.021 | 18.155 | 0.013 | 17.289 | 0.007 | 16.070 | 0.009 | 15.349 | 0.016 |
| 073445.66+155448.9 | 2713 | 598 | 54397 | 18.226 | 0.017 | 17.432 | 0.009 | 16.667 | 0.007 | 15.544 | 0.013 | 14.867 | 0.015 |
| 073455.91+410537.4 | 2683 | 507 | 54153 | 17.698 | 0.017 | 17.403 | 0.010 | 17.220 | 0.019 | 16.423 | 0.019 | 15.796 | 0.018 |
| $073534.33+650648.8$ | 2944 | 287 | 54523 | 20.067 | 0.037 | 19.499 | 0.015 | 19.087 | 0.013 | 18.058 | 0.012 | 17.343 | 0.017 |
| $73717.69+412620.1$ | 2683 | 557 | 54153 | 17.891 | 0.020 | 17.590 | 0.018 | 17.104 | 0.012 | 16.495 | 0.012 | 15.877 | 0.014 |
| $3948.55+181813.9$ | 2915 | 392 | 54497 | 20.424 | 0.051 | 19.584 | 0.019 | 18.515 | 0.014 | 17.83 | 0.013 | 17.354 | 0.019 |
| 74027.89+184819.8 | 2915 | 384 | 54497 | 20.163 | 0.045 | 19.556 | 0.016 | 18.745 | 0.010 | 17.885 | 0.010 | 17.413 | 0.018 |
| 074211.87+182227.6 | 2915 | 475 | 54497 | 19.419 | 0.026 | 18.998 | 0.013 | 18.961 | 0.014 | 18.199 | 0.012 | 17.570 | 0.018 |
| $074521.86+171520.6$ | 2915 | 43 | 54497 | 20.852 | 0.097 | 19.462 | 0.013 | 18.602 | 0.009 | 17.821 | 0.011 | 17.192 | 0.017 |
| 074758.75+222942.3 | 2916 | 267 | 54507 | 19.748 | 0.040 | 19.120 | 0.015 | 18.682 | 0.017 | 17.667 | 0.017 | 17.038 | 0.018 |
| 074845.71+180240.4 | 2890 | 35 | 54495 | 16.741 | 0.017 | 16.337 | 0.026 | 15.616 | 0.069 | 14.965 | 0.042 | 14.518 | 0.029 |
| 075051.85+085020.1 | 2945 | 314 | 54505 | 19.101 | 0.027 | 18.085 | 0.010 | 17.219 | 0.009 | 16.177 | 0.012 | 15.604 | 0.013 |
| 5153.17+653104.6 | 2944 | 107 | 54523 | 20.955 | 0.077 | 19.975 | 0.017 | 18.871 | 0.014 | 18.014 | 0.016 | 17.442 | 0.0 |

Table A.2: continued.

| System (SDSSJ) | Plate | Fiber | MJD | u | $\sigma_{u}$ |  | $\sigma_{g}$ |  | $\sigma_{r}$ |  | $\sigma_{i}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 075314.67+190926.0 | 2729 | 459 | 54419 | 20.164 | 0.056 | 19.508 | 0.017 | 18.647 | 0.017 | 17.804 | 0.012 | 286 | 020 |
| 075356.37+233118.9 | 2891 | 516 | 54507 | 18.535 | 0.021 | 18.019 | 0.015 | 17.436 | 0.010 | 16.442 | 0.011 | 15.829 | 0.019 |
| 75359.48+175445.5 | 2729 | 158 | 54419 | 20.194 | 0.058 | 19.701 | 0.018 | 19.450 | 0.016 | 18.505 | 0.014 | 17.699 | 0.019 |
| 5426.29+240721.3 | 2916 | 568 | 54507 | 20.417 | 0.052 | 19.921 | 0.017 | 19.192 | 0.021 | 17.999 | 0.017 | 17.275 | 0.019 |
| 134.24+093643.0 | 2940 | 610 | 54508 | 18.716 | 0.095 | 17.457 | 0.075 | 16.894 | 0.062 | 15.404 | 0.019 | 14.783 | 0.018 |
| 2816.5 | 2549 | 438 | 523 | 20.271 | 0.077 | 19.699 | 0.023 |  | . 015 | 17.85 | 0.017 | 295 | 21 |
| 081327.92+3732 | 2670 | 275 | 54 | 18.919 | 0.024 | 18.073 | 0.015 | 16. | 016 | 16. | 0.014 | . 625 | 0.017 |
| 081523.77+832651.2 | 2549 | 436 | 54523 | 20.096 | 0.063 | 19.576 | 0.018 | 18.751 | 0.015 | 18.001 | 0.019 | 17.525 | 0.026 |
| 2807.91-052045.5 | 2828 | 294 | 54438 | 20.292 | 0.055 | 19.571 | 0.015 | 18.620 | 0.014 | 17.721 | 0.013 | 17.179 | 16 |
| 2835.00+241547.6 | 2330 | 191 | 53738 | 20.503 | 0.066 | 20.050 | 0.021 | 19.378 | 0.020 | 18.448 | 0.024 | 17.959 | 0.023 |
| 903.53+231651.0 | 2315 | 214 | 53741 | 19.780 | 0.038 | 18.825 | 0.021 | 17.759 | 0.017 | 16.547 | 0.013 | 15.830 | 18 |
| 83025.47-053638.7 | 2828 | 203 | 54438 | 20.03 | 0.046 | 19.411 | 0.017 | 18.834 | 0.012 | 17.883 | 0.013 | 17.259 | 017 |
| 3255.20-043046.2 | 2807 | 153 | 54433 | 19.5 | 0.326 | 17.762 | 0.064 | 16.909 | 0.020 | 15.64 | 0.010 | 14.968 | 0.016 |
| 83348.00+531632.1 | 2331 | 258 | 53742 | 20.725 | 0.069 | 19.959 | 0.030 | 19.353 | 0.021 | 18.493 | 0.019 | 17.868 | 0.033 |
| 33630.34-041018.9 | 2828 | 597 | 54438 | 19.884 | 0.043 | 19.247 | 0.014 | 18.505 | 0.013 | 17.404 | 0.011 | 16.750 | . 018 |
| 3807.99+530254.3 | 2331 | 88 | 53742 | 19.366 | 0.038 | 19.397 | 0.023 | 18.922 | 0.018 | 18.330 | 0.020 | 17.807 | 0.029 |
| 4221.35+544834.5 | 2331 | 562 | 53742 | 20.702 | 0.072 | 20.089 | 0.023 | 19.909 | 0.023 | 19.167 | 0.023 | 18.451 | 0.040 |
| 4514.23+540311.6 | 2316 | 596 | 53757 | 19.754 | 0.036 | 18.720 | 0.018 | 17.736 | 0.018 | 16.821 | 0.015 | 16.273 | 0.014 |
| $18.66+055911.7$ | 2317 | 318 | 54152 | 19.529 | 0.035 | 18.042 | 0.016 | 16. | 0.013 | 15.930 | 0.017 | 15.373 | . 015 |
| 4852.36+050135.6 | 2332 | 210 | 54 | 20.022 | 0.035 | 19. | 0.0 | 19.297 | 0.020 | 18.72 | 0.01 | 18 | . 24 |
| 84854.42+823437.2 | 2541 | 60 | 54481 | 19.6 | 0.041 | 18.748 | 0.014 | 17.791 | 0.013 | 16.613 | 0.014 | 15.944 | . 017 |
| 5024.05+054757.8 | 2317 | 161 | 54152 | 18.070 | 0.023 | 16.323 | 0.016 | 15.071 | 0.011 | 14.270 | 0.015 | 13.848 | 0.014 |
| 085110.25+024731.8 | 2913 | 310 | 54526 | 20.592 | 0.059 | 19.689 | 0.017 | 18.647 | 0.014 | 17.464 | 0.011 | 16.751 | 0.021 |
| 5202.07+115400.1 | 2667 | 535 | 54142 | 18.760 | 0.023 | 18.093 | 0.024 | 17.424 | 0.011 | 16.693 | 0.008 | 6.214 | , 14 |
| 23.75+071326. | 2332 | 579 | 54149 | 21.011 | 0.103 | 20.197 | 0.023 | 19.602 | 23 | 18.510 | 0.016 | 37 | 34 |
| 03+072033.5 | 2332 | 569 | 54149 | 19.985 | . 050 | 19.213 | 0.023 | 18.525 | 0.018 | 17.4 | 0.013 | 16.701 | 0.019 |
| 085548.16+022341.6 | 2913 | 133 | 54526 | 20.494 | 0.069 | 19.906 | 0.021 | 19.366 | 0.019 | 18.06 | 0.013 | 17.174 | 0.017 |
| 085558.37+832841.5 | 2541 | 558 | 54481 | 18.790 | 0.024 | 17.911 | 0.029 | 16.926 | 0.019 | 16.141 | 0.016 | 15.702 | 0.020 |
| 085631.57+030554.7 | 2913 | 151 | 54526 | 19.372 | 0.028 | 19.101 | 0.016 | 19.137 | 0.018 | 18.465 | 0.018 | 17.769 | 0.022 |
| 5634.83+373913.4 | 2400 | 492 | 53765 | 19.929 | 0.044 | 19.441 | 0.030 | 19.024 | 0.021 | 18.095 | 0.018 | 17.394 | 0.019 |
| $12.72+373757.3$ | 2380 | 1 | 53759 | 17.728 | 0.013 | 16.718 | 0.018 | 15.723 | 0.020 | 14.743 | 0.011 | 4.199 | 13 |
| 132.23+303605.3 | 2401 | 341 | 53 | 19.602 | 0.031 | 19.023 | 0.018 | 18.676 | 0.019 | 17.919 | , 01 | 52 | . 31 |
| 44.46+313743.5 | 2401 | 524 | 53 | 19. | . 03 | 18.897 | 0.02 | 18.000 | 0.0 | 17.3 | 0. | 16.877 | 21 |
| 091930.11+211904.7 | 2319 | 127 | 53763 | 20.664 | 0.068 | 19.332 | 0.017 | 18.371 | 0.014 | 16.83 | 0.019 | 15.755 | 0.018 |
| 092030.33+301831.2 | 2401 | 142 | 53768 | 20.921 | 0.082 | 19.705 | 0.022 | 18.572 | 0.016 | 17.555 | 0.018 | 16.955 | 0.017 |
| 2215.71+303954.5 | 2381 | 590 | 53762 | 17.733 | 0.017 | 17.113 | 0.017 | 16.340 | 0.016 | 15.190 | 0.014 | 14.504 | 0.020 |
| 3441.29+305026.0 | 2914 | 413 | 54533 | 20.030 | 0.049 | 19.389 | 0.020 | 18.911 | 0.024 | 17.832 | 0.016 | 17.073 | 0.019 |
| 4029.39+523324.7 | 2384 | 143 | 53763 | 18.653 | 0.035 | 17.814 | 0.031 | 16.843 | 0.013 | 15.954 | 0.017 | 15.399 | 0.017 |
| 035.24+520007.6 | 2404 | 50 | 53764 | 19.77 | 0.050 | 19.211 | 0.038 | 18.56 | 0.0 | 17.7 | 0.019 | 17.155 | 0.030 |
| 4103.00+523257.4 | 2404 | 141 | 53764 | 19.574 | 0.036 | 19.256 | 0.020 | 18.934 | 0.054 | 18.2 | 0.015 | 17.729 | 0.021 |
| 094402.18+614307.9 | 2403 | 167 | 53795 | 19.166 | 0.026 | 18.746 | 0.020 | 17.918 | 0.012 | 17.288 | 0.013 | 16.901 | 0.022 |
| $094637.33+631228.1$ | 2403 | 448 | 53795 | 20.044 | 0.053 | 19.885 | 0.033 | 19.478 | 0.024 | 18.655 | 0.023 | 18.098 | 0.033 |
| 095632.22-003341.4 | 2867 | 278 | 54479 | 20.010 | 0.040 | 19.127 | 0.029 | 18.232 | 0.023 | 16.917 | 0.027 | 16.047 | 0.030 |
| 55953.52-011504.4 | 2867 | 203 | 54479 | 20.318 | 0.052 | 19.695 | 0.020 | 19.575 | 0.022 | 18.741 | 0.016 | 18.073 | 0.028 |
| 0347.63+352958.2 | 2407 | 332 | 53771 | 20.108 | 0.049 | 19.665 | 0.025 | 19.353 | 0.019 | 18.423 | 0.018 | 17.816 | 0.025 |
| 20533.84+250149.4 | 2406 | 32 | 54084 | 20.080 | 0.044 | 19.425 | 0.025 | 18.627 | 0.024 | 17.68 | 0.017 | 17.065 | 0.020 |
| 100732.50+254334.6 | 2406 | 223 | 54084 | 20.185 | 0.041 | 19.403 | 0.020 | 18.639 | 0.020 | 17.443 | 0.026 | 16.676 | 0.017 |
| $100821.19+260213.9$ | 2406 | 495 | 54084 | 20.182 | 0.046 | 19.964 | 0.020 | 19.374 | 0.016 | 18.507 | 0.017 | 17.994 | 0.030 |
| 100828.18+263732.5 | 2386 | 416 | 54064 | 19.131 | 0.021 | 17.249 | 0.019 | 16.114 | 0.022 | 15.432 | 0.016 | 15.033 | 0.025 |
| $100900.48+360457.6$ | 2407 | 436 | 53771 | 20.039 | 0.042 | 19.510 | 0.015 | 18.537 | 0.014 | 17.749 | 0.017 | 17.269 | 0.019 |
| $101032.62+344527.9$ | 2407 | 149 | 53771 | 20.132 | 0.050 | 19.662 | 0.021 | 19.089 | 0.017 | 18.352 | 0.025 | 17.861 | 0.028 |
| 102102.25+174439.9 | 2868 | 311 | 54451 | 20.350 | 0.059 | 19.512 | 0.017 | 19.013 | 0.019 | 17.972 | 0.021 | 17.223 | 0.021 |
| 102205.96+080246.6 | 2869 | 289 | 54454 | 19.045 | 0.030 | 18.922 | 0.017 | 18.540 | 0.016 | 17.878 | 0.015 | 17.366 | 0.025 |
| 102256.25+095418.5 | 2869 | 327 | 54454 | 19.887 | 0.049 | 19.147 | 0.025 | 18.334 | 0.020 | 17.037 | 0.012 | 16.238 | 0.020 |
| $102438.46+162458.2$ | 2868 | 202 | 54451 | 19.887 | 0.046 | 19.041 | 0.018 | 18.341 | 0.019 | 17.230 | 0.016 | 16.523 | 0.016 |
| 102515.38+174937.6 | 2868 | 478 | 54451 | 19.935 | 0.041 | 19.704 | 0.025 | 19.746 | 0.023 | 18.870 | 0.034 | 18.157 | 0.029 |
| $102623.21+162938.5$ | 2868 | 86 | 54451 | 20.349 | 0.065 | 19.747 | 0.031 | 19.238 | 0.021 | 18.366 | 0.015 | 17.791 | 0.024 |
| $102843.97+443252.6$ | 2557 | 399 | 54178 | 19.254 | 0.036 | 17.781 | 0.015 | 16.652 | 0.016 | 15.640 | 0.019 | 15.100 | 0.020 |
| $\underline{102857.78+093129.8 ~}$ | 2854 | 573 | 54480 | 17.181 | 0.021 | 16.400 | 0.023 | 15.581 | 0.027 | 14.596 | 0.021 | 13.994 | 0.021 |

Table A.2: continued.

| J) | Plate | Fiber | MJD | u | $\sigma_{u}$ |  |  |  | $\sigma_{r}$ |  | $\sigma_{i}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 103432.27+442956.6 | 2567 | 485 | 54179 | 20.691 | 0.071 | 584 | 0.025 | 18.601 | 0.016 | 255 | 0.016 | .385 | 19 |
| $104751.79+483503.7$ | 2410 | 357 | 54087 | 20.211 | 0.064 | 19.591 | 0.033 | 19.412 | 0.029 | 18.590 | 0.024 | 18.099 | 0.033 |
| 105008.93+473748.0 | 2390 | 270 | 54094 | 19.933 | 0.035 | 18.718 | 0.011 | 17.634 | 0.019 | 16.731 | 0.018 | 16.229 | 0.018 |
| 542.59+470628.7 | 2410 | 250 | 54087 | 20.718 | 0.118 | 19.758 | 0.027 | 18.805 | 0.018 | 17.392 | 0.018 | 16.598 | 0.020 |
| 051.70-001207.7 | 2409 | 121 | 54210 | 20.051 | 0.035 | 18.952 | 0.017 | 18.017 | 0.024 | 16.941 | 0.018 | 16.313 | 0.012 |
| 105526.23+472923.0 | 2390 | 169 | 409 | 9.537 | 0.03 | 18.286 | 011 | 17.256 | 0.019 | 16.043 | 0.012 | 15.334 | . 017 |
| 105730.98+474614.3 | 2410 | 12 | 54087 | 20.8 | 0.087 | 19.922 | 0.036 | 19.016 | 0.025 | 18.049 | 0.020 | 17.528 | 0.029 |
| 110442.27-153936.2 | 2690 | 335 | 54211 | 20.065 | 0.052 | 17.909 | 0.014 | 16.919 | 0.018 | 16.386 | 0.013 | 16.047 | 0.018 |
| 110517.60+385125.7 | 2871 | 467 | 54536 | 19.054 | 0.022 | 18.443 | 0.019 | 18.083 | 0.016 | 17.320 | 0.014 | 16.736 | 0.016 |
| 10520.63+282408.7 | 2870 | 118 | 54534 | 20.865 | 0.067 | 19.475 | 0.018 | 18.634 | 0.018 | 17.255 | 0.036 | 16.198 | . 017 |
| 529.78-16471 | 2708 | 33 | 54561 | 19.513 | 0.045 | 19.407 | 0.020 | 19.186 | 0.017 | 18.440 | 0.018 | 17.900 | . 029 |
| $652.91+284245.4$ | 2870 | 631 | 54534 | 20.349 | 0.050 | 19.212 | 0.020 | 18.225 | 0.017 | 17.112 | 0.018 | 16.494 | . 056 |
| 10734.09-162414.4 | 2690 | 195 | 54211 | 17.747 | 0.020 | 17.614 | 0.028 | 16.916 | 0.012 | 16.273 | 0.011 | 15.823 | 0.019 |
| $10738.05+380051.3$ | 2871 | 169 | 54536 | 20.376 | 0.052 | 19.952 | 0.024 | 19.538 | 0.019 | 18.484 | 0.023 | 17.669 | 0.024 |
| 10741.47+283003.1 | 2870 | 29 | 54534 | 19.525 | 0.031 | 18.197 | 0.028 | 17.083 | 0.015 | 16.150 | 0.013 | 15.628 | 0.012 |
| 10749.80+290939.9 | 2870 | 607 | 54534 | 21.331 | 0.117 | 19.931 | 0.032 | 18.760 | 0.028 | 17.924 | 0.018 | 17.428 | 0.025 |
| 10758.94+275346.2 | 2870 | 6 | 54534 | 20.211 | 0.053 | 19.318 | 0.031 | 18.247 | 0.029 | 17.375 | 0.023 | 16.866 | 0.047 |
| 0834.66-154847.3 | 2708 | 501 | 54561 | 19.95 | 0.062 | 19.265 | 0.017 | 18.821 | 0.017 | 17.868 | 0.016 | 17.203 | . 021 |
| 4.22-145147.0 | 2708 | 447 | 54561 | 20.165 | . 061 | 19.817 | 0.022 | 19.232 | 0.018 | 18.556 | 0.018 | 18.081 | 0.026 |
| 25+392453.1 | 2871 | 610 | 54536 | 19.661 | 0.031 | 18.223 | 0.022 | 17.139 | 0.018 | 16.292 | 0.010 | 15.811 | 0.013 |
| $1251.20+190700.3$ | 2872 | 232 | 54533 | 19.996 | 0.035 | 19.462 | 0.020 | 19.062 | 0.018 | 18.341 | 0.019 | 17.811 | 0.025 |
| $1419.27+083829.0$ | 2413 | 136 | 54169 | 18.922 | 0.039 | 18.432 | 0.027 | 18.319 | 0.020 | 17.539 | 0.025 | 16.796 | . 029 |
| 111428.51+590209.1 | 2414 | 461 | 54526 | 20.116 | 0.047 | 19.649 | 0.049 | 19.164 | 0.019 | 17.945 | 0.019 | 17.012 | 0.025 |
| $1459.92+092411.1$ | 2413 | 172 | 54169 | 19.679 | 0.034 | 19.054 | 0.020 | 18.977 | 0.057 | 18.383 | 0.041 | 17.843 | . 025 |
| 111501.51-120321.9 | 2874 | 265 | 5456 | 20.198 | 0.049 | 19.664 | 0.020 | 19.522 | 0.018 | 18.763 | 0.018 | 18.103 | 20 |
| 615.73+590509.3 | 2414 | 65 | 54526 | 19.504 | . 038 | 18.770 | 0.030 | 17.85 | 0.019 | 16.99 | 0.018 | 16.503 | . 227 |
| 111710.54-125540.9 | 287 | 205 | 54561 | 20.270 | 0.048 | 19.668 | 0.019 | 19.239 | 0.015 | 18.456 | 0.017 | 17.915 | 0.022 |
| 111722.07-104556.1 | 2859 | 408 | 54570 | 17.926 | 0.023 | 17.842 | 0.017 | 17.403 | 0.011 | 16.502 | 0.012 | 15.887 | 0.015 |
| 111920.11-104810.6 | 2874 | 448 | 54561 | 19.827 | 0.044 | 18.867 | 0.016 | 17.793 | 0.012 | 16.857 | 0.011 | 16.339 | 0.011 |
| $1950.69+185351.0$ | 2872 | 70 | 54533 | 19.727 | 0.037 | 18.710 | 0.023 | 17.676 | 0.013 | 16.792 | 0.010 | 16.295 | . 020 |
| 012.71+19012 | 2872 | 71 | 54533 | 19.085 | 0.030 | 18.353 | 0.020 | 17.688 | 0.026 | 16.663 | 0.022 | 16.022 | . 035 |
| 67 | 2873 | 379 | 54505 | 20.5 | , 73 | 19.389 | 26 | 18.433 | 20 | 42 | . 012 | 16.595 | . 021 |
| 08.40-115559.3 | 2859 | 72 | 54570 | 18.58 | 0.0 | 17.991 | 0.02 | 17. | 0.01 | 16.322 | 0.01 | 15.510 | 21 |
| 112409.43+590935.8 | 2414 | 596 | 54526 | 20.397 | 0.046 | 19.358 | 0.015 | 18.525 | 0.018 | 17.297 | 0.013 | 16.553 | 0.018 |
| 112651.03-081640.1 | 2876 | 255 | 54581 | 20.041 | 0.059 | 18.960 | 0.020 | 17.922 | 0.013 | 17.048 | 0.011 | 16.503 | 0.017 |
| $112812.63+671738.3$ | 2873 | 513 | 54505 | 19.647 | 0.033 | 18.940 | 0.021 | 18.082 | 0.021 | 17.018 | 0.021 | 16.439 | . 017 |
| 13457.72+655408.7 | 2873 | 55 | 54505 | 18.231 | 0.023 | 18.138 | 0.015 | 18.124 | 0.019 | 17.416 | 0.024 | 16.672 | . 024 |
| 3546.87+675832.3 | 2873 | 561 | 54505 | 20.889 | 0.079 | 19.718 | 0.025 | 18.643 | 0.020 | 17.332 | 0.017 | 16.581 | 0.016 |
| $557.51+010310.4$ | 2877 | 521 | 54523 | 20.455 | 0.046 | 19.754 | 0.024 | 19.446 | 0.018 | 18.437 | 0.018 | 17.601 | 0.017 |
| $113600.68+001212.2$ | 2877 | 499 | 54523 | 20.048 | 0.057 | 20.028 | 0.022 | 19.704 | 0.021 | 19.050 | 0.016 | 18.571 | 0.038 |
| 113800.35-001144.4 | 2877 | 111 | 54523 | 19.135 | 0.025 | 18.849 | 0.020 | 18.868 | 0.021 | 18.162 | 0.023 | 17.535 | 0.027 |
| 114316.55+665813.1 | 2873 | 36 | 54505 | 20.272 | 0.047 | 19.778 | 0.025 | 19.112 | 0.020 | 18.181 | 0.023 | 17.574 | 0.022 |
| $120953.67+185815.7$ | 2918 | 44 | 54554 | 20.376 | 0.046 | 18.866 | 0.022 | 17.740 | 0.014 | 16.946 | 0.017 | 16.460 | 0.022 |
| $121033.60+185346.2$ | 2918 | 56 | 54554 | 20.410 | 0.054 | 19.903 | 0.033 | 19.471 | 0.021 | 18.600 | 0.018 | 18.057 | 0.024 |
| 21318.14+510247.4 | 2919 | 609 | 54537 | 18.867 | 0.030 | 18.468 | 0.017 | 18.317 | 0.020 | 17.586 | 0.021 | 17.059 | 0.018 |
| 1412.67+410132.8 | 2467 | 60 | 54176 | 20.222 | 0.061 | 19.303 | 0.020 | 18.431 | 0.012 | 17.688 | 0.015 | 17.218 | 0.025 |
| 122644.16+010302.5 | 2568 | 569 | 54153 | 20.433 | 0.049 | 19.083 | 0.018 | 18.039 | 0.015 | 16.710 | 0.013 | 15.941 | 0.015 |
| $123528.65+003042.2$ | 2895 | 498 | 54567 | 18.407 | 0.029 | 17.807 | 0.022 | 17.397 | 0.020 | 16.409 | 0.017 | 15.622 | 0.019 |
| 123847.53-021900.8 | 2922 | 339 | 54612 | 20.460 | 0.054 | 19.083 | 0.016 | 18.001 | 0.015 | 16.904 | 0.014 | 16.257 | 0.014 |
| $123922.33+005548.8$ | 2920 | 603 | 54562 | 19.569 | 0.033 | 19.274 | 0.026 | 19.207 | 0.021 | 18.398 | 0.017 | 17.789 | 0.023 |
| $124140.76+600711.4$ | 2446 | 345 | 54571 | 18.056 | 0.018 | 17.726 | 0.037 | 17.522 | 0.027 | 16.763 | 0.033 | 16.212 | 0.027 |
| 4232.45-064607.7 | 2689 | 370 | 54149 | 18.506 | 0.024 | 17.464 | 0.018 | 16.336 | 0.018 | 15.413 | 0.015 | 14.879 | 0.020 |
| 124250.39-085332.0 | 2707 | 245 | 54144 | 20.171 | 0.057 | 19.973 | 0.026 | 19.475 | 0.017 | 18.593 | 0.013 | 17.985 | 0.025 |
| 124356.79-064758.4 | 2707 | 444 | 54144 | 18.492 | 0.029 | 18.098 | 0.024 | 18.003 | 0.013 | 17.227 | 0.017 | 16.577 | 0.025 |
| $124511.47+584551.8$ | 2461 | 283 | 54570 | 20.811 | 0.065 | 19.327 | 0.018 | 18.210 | 0.018 | 17.422 | 0.028 | 16.971 | 0.022 |
| $124731.83+585158.1$ | 2461 | 251 | 54570 | 20.541 | 0.071 | 19.276 | 0.025 | 18.177 | 0.016 | 17.157 | 0.029 | 16.603 | 0.015 |
| $124752.00+483835.3$ | 2923 | 242 | 54563 | 19.544 | 0.027 | 17.310 | 0.024 | 16.305 | 0.021 | 15.759 | 0.037 | 15.460 | 0.022 |
| $124910.54+284333.7$ | 2472 | 55 | 54175 | 20.600 | 0.073 | 19.572 | 0.028 | 18.606 | 0.022 | 17.442 | 0.022 | 16.769 | 0.022 |
| $\underline{124945.14+495752.7}$ | 2923 | 464 | 54563 | 19.007 | 0.027 | 18.176 | 0.015 | 17.300 | 0.020 | 16.187 | 0.018 | 15.473 | 0.018 |

Table A.2: continued.

| System (SDSSJ) | Plate | Fiber | MJD | u |  |  |  |  | $\sigma_{r}$ |  | $\sigma_{i}$ | Z |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 125039.65+091634.6 | 2965 | 230 | 54594 | 21.339 | 0.114 | 19.461 | 0.031 | 18.255 | 0.018 | 17.187 | 0.026 | 6.660 | 0.021 |
| 125105.17+502727.5 | 2923 | 459 | 54563 | 20.171 | 0.039 | 19.665 | 0.017 | 19.125 | 0.028 | 18.101 | 0.015 | 17.540 | 0.021 |
| 125316.24+100744.1 | 2965 | 514 | 54594 | 19.752 | 0.047 | 18.506 | 0.024 | 17.343 | 0.013 | 16.139 | 0.016 | 15.512 | 0.013 |
| 125341.54+103413.9 | 2965 | 573 | 54594 | 18.274 | 0.034 | 17.843 | 0.017 | 17.788 | 0.021 | 16.974 | 0.019 | 16.347 | . 20 |
| $125903.39+193145.7$ | 2924 | 180 | 54582 | 20.787 | 0.077 | 19.663 | 0.020 |  | 0.015 | 17.921 | 0.019 | 17.591 | , 19 |
| 130012.49+190857.4 | 2924 | 114 | 54582 | 19.850 | 0.040 | 19.220 | 0.024 | 18.679 | 0.021 | 17.663 | 0.020 | 16.887 | 0.018 |
| 130804.66-004031.6 | 2926 | 289 | 54625 | 20.101 | 0.044 | 19.172 | 0.016 | 18.067 | 0.025 | 17.259 | 0.020 | 16.818 | 0.022 |
| 131208.10+002057.9 | 2926 | 483 | 54625 | 18.746 | 0.030 | 18.485 | 0.015 | 18.347 | 0.014 | 17.561 | 0.014 | 16.924 | 0.025 |
| 131247.93-003427.5 | 2926 | 150 | 54625 | 20.980 | 0.082 | 19.886 | 0.020 | 18.852 | 0.019 | 17.934 | 0.021 | 17.416 | 0.020 |
| 131632.04-003758.0 | 2926 | 17 | 54625 | 20.607 | 0.058 | 19.355 | 0.019 | 18.230 | 0.016 | 16.967 | 0.022 | 16.263 | 0.027 |
| 132040.28+661214.8 | 2460 | 315 | 54616 | 18.808 | 0.023 | 18.726 | 0.015 | 18.376 | 0.026 | 17.792 | 0.019 | 17.392 | 0.023 |
| $132142.39+664612.7$ | 2445 | 391 | 54573 | 18.429 | 0.021 | 18.097 | 0.050 | 17.262 | 0.016 | 16.401 | 0.016 | 15.854 | 0.022 |
| $132942.56+665539.8$ | 2460 | 500 | 54616 | 20.658 | 0.064 | 19.493 | 0.029 | 18.339 | 0.025 | 17.421 | 0.016 | 16.917 | 0.023 |
| $133732.33+082815.5$ | 2928 | 286 | 54614 | 20.802 | 0.080 | 19.922 | 0.027 | 19.130 | 0.019 | 18.020 | 0.017 | 17.313 | 0.021 |
| 133830.06+102034.6 | 2928 | 368 | 54614 | 20.359 | 0.057 | 19.738 | 0.016 | 19.211 | 0.018 | 18.338 | 0.019 | 17.782 | 0.024 |
| 133907.55+673333.9 | 2445 | 620 | 54573 | 17.938 | 0.026 | 17.144 | 0.023 | 16.241 | 0.010 | 15.706 | 0.018 | 15.394 | 0.011 |
| 134008.04+082248.4 | 2903 | 216 | 54581 | 18.418 | 0.023 | 17.796 | 0.020 | 17.362 | 0.016 | 16.121 | 0.017 | 15.389 | 0.020 |
| 134207.24+285707.9 | 2929 | 377 | 54616 | 20.471 | 0.061 | 19.406 | 0.021 | 18.216 | 0.015 | 17.099 | 0.018 | 16.512 | 0.019 |
| 134520.62+174805.3 | 2930 | 298 | 54589 | 19.439 | 0.033 | 18.874 | 0.025 | 18.276 | 0.014 | 17.207 | 0.021 | 16.588 | 0.023 |
| 134641.59+174357.4 | 2930 | 244 | 54589 | 21.070 | 0.080 | 19.836 | 0.036 | 18.698 | 0.021 | 17.682 | 0.021 | 17.036 | 0.020 |
| $134721.80+270724.9$ | 2929 | 63 | 54616 | 17.645 | 0.016 | 17.299 | 0.021 | 16.648 | 0.017 | 15.996 | 0.017 | 15.592 | 0.012 |
| $134841.61+183410.5$ | 2905 | 488 | 54580 | 17.702 | 0.013 | 17.310 | 0.017 | 17.194 | 0.013 | 16.470 | 0.019 | 15.879 | 0.014 |
| 135207.77+185033.8 | 2930 | 83 | 54589 | 20.632 | 0.064 | 19.469 | 0.016 | 18.438 | 0.013 | 17.254 | 0.024 | 16.628 | 0.016 |
| 135232. | 2929 | 623 | 54616 | 21.426 | 0.110 | 19.943 | 0.025 | 18.788 | 0.015 | 17.825 | 0.011 | 17.324 | 0.018 |
| 135643.56-085808.9 | 2716 | 399 | 54629 |  |  |  |  |  |  |  |  |  |  |
| 135930.96-101029.7 | 2716 | 211 | 54628 |  |  |  |  |  |  |  |  |  |  |
| $140923.26+371048.5$ | 2906 | 469 | 54577 | 16.598 | 0.013 | 15.859 | 0.013 | 14.879 | 0.013 | 14.323 | 0.013 | 13.962 | 0.023 |
| $141052.79+375435.6$ | 2931 | 526 | 54590 | 19.803 | 0.043 | 19.286 | 0.030 | 18.373 | 0.019 | 17.652 | 0.018 | 17.243 | 0.022 |
| $141635.70+360006.5$ | 2931 | 61 | 54590 | 18.983 | 0.023 | 18.156 | 0.025 | 17.201 | 0.021 | 16.240 | 0.024 | 15.763 | 0.021 |
| $141759.16+361542.8$ | 2931 | 32 | 54590 | 19.955 | 0.040 | 18.788 | 0.027 | 17.684 | 0.017 | 16.879 | 0.020 | 6.383 | . 22 |
| $105.31+572457$. | 2447 | 540 | 5449 | 16.879 | 0.044 | 16.8 | 0.034 | 16.2 | 0.021 | 15. | 0.021 | 155 | . 021 |
| 142405.07+553008.0 | 2462 | 59 | 54561 | 20.190 | 0.060 | 18.996 | 0.03 | 18.016 | 0.032 | 17.4 | 0.018 | 17.082 | 21 |
| 142444.36+443114.5 | 2932 | 244 | 54595 | 20.691 | 0.085 | 19.991 | 0.043 | 19.465 | 0.033 | 18.832 | 0.026 | 18.464 | 0.035 |
| 142503.62+073846.4 | 2933 | 285 | 54617 | 20.378 | 0.052 | 19.655 | 0.019 | 18.864 | 0.015 | 17.791 | 0.014 | 17.093 | 0.021 |
| $142541.80+442411.7$ | 2932 | 205 | 54595 | 21.235 | 0.088 | 19.977 | 0.020 | 18.888 | 0.020 | 17.804 | 0.016 | 17.166 | 0.016 |
| $142557.28+442554.1$ | 2932 | 202 | 54595 | 19.633 | 0.031 | 18.651 | 0.015 | 17.740 | 0.018 | 16.732 | 0.015 | 16.122 | 0.013 |
| 142631.93+091621.1 | 2933 | 340 | 54617 | 20.493 | 0.057 | 19.509 | 0.022 | 18.685 | 0.014 | 17.540 | 0.018 | 16.879 | 0.013 |
| 951.19+575949.0 | 2547 | 198 | 53917 | . 05 | . 042 | 19.431 | 0.01 | 18.749 | 0.020 | 17.75 | 0.019 | 17.074 | 0.022 |
| 143026.84+073450.0 | 2933 | 85 | 54617 | 18.493 | 0.026 | 18.279 | 0.027 | 18.063 | 0.015 | 17.18 | 0.016 | 16.498 | 0.023 |
| $143114.35+075707.0$ | 2933 | 146 | 54617 | 19.773 | 0.044 | 19.198 | 0.025 | 18.458 | 0.020 | 17.733 | 0.023 | 17.271 | 0.021 |
| $143143.83+565728.2$ | 2547 | 122 | 53917 | 20.590 | 0.062 | 19.918 | 0.020 | 19.803 | 0.021 | 19.033 | 0.018 | 18.232 | 0.030 |
| $143539.80+590529.5$ | 2539 | 524 | 53918 | 20.167 | 0.052 | 18.338 | 0.018 | 17.144 | 0.021 | 16.213 | 0.012 | 15.654 | 0.015 |
| $143604.00+571906.2$ | 2547 | 56 | 53917 | 21.126 | 0.105 | 19.911 | 0.019 | 18.837 | 0.015 | 18.191 | 0.013 | 17.745 | 0.022 |
| $143642.01+574146.3$ | 2547 | 110 | 53917 | 20.869 | 0.075 | 19.733 | 0.024 | 18.598 | 0.014 | 17.383 | 0.014 | 16.688 | 0.013 |
| $143746.69+573706.0$ | 2547 | 69 | 53917 | 18.962 | 0.024 | 18.517 | 0.025 | 18.113 | 0.013 | 17.057 | 0.011 | 16.354 | 0.017 |
| $143947.78+574115.4$ | 2547 | 26 | 53917 | 20.784 | 0.084 | 19.471 | 0.018 | 18.331 | 0.012 | 17.620 | 0.013 | 17.195 | 0.023 |
| 143957.92+573944.6 | 2539 |  | 53918 | 19.615 | 0.036 | 18.243 | 0.016 | 17.157 | 0.011 | 16.413 | 0.012 | 15.963 | 0.019 |
| 144258.47+001031.5 | 2934 | 354 | 54626 | 18.379 | 0.018 | 18.329 | 0.020 | 18.262 | 0.022 | 17.475 | 0.015 | 16.758 | 0.027 |
| 144600.37+000817.0 | 2934 | 473 | 54626 | 20.574 | 0.051 | 19.981 | 0.019 | 19.815 | 0.018 | 18.983 | 0.019 | 18.146 | 0.027 |
| 145305.77+001048.2 | 2934 | 640 | 54626 | 19.710 | 0.031 | 18.889 | 0.016 | 18.200 | 0.017 | 17.094 | 0.019 | 16.392 | 0.020 |
| 150438.86+321443.4 | 2935 | 187 | 54652 | 19.342 | 0.029 | 19.078 | 0.016 | 18.367 | 0.014 | 17.682 | 0.025 | 17.277 | 0.024 |
| 151744.70+062011.9 | 2927 | 135 | 54621 | 21.319 | 0.117 | 19.835 | 0.024 | 18.660 | 0.016 | 17.523 | 0.013 | 16.892 | 0.017 |
| 151852.44+074459.3 | 2739 | 525 | 54618 | 20.488 | 0.048 | 19.958 | 0.020 | 19.533 | 0.020 | 18.565 | 0.020 | 17.938 | 0.021 |
| 152002.84+081231.0 | 2739 | 571 | 54618 | 19.555 | 0.035 | 19.159 | 0.019 | 18.953 | 0.018 | 17.998 | 0.017 | 17.254 | 0.022 |
| $152033.43+063442.9$ | 2739 | 61 | 54618 | 19.475 | 0.035 | 18.960 | 0.016 | 18.572 | 0.041 | 17.591 | 0.034 | 16.923 | 0.026 |
| $152416.97+504749.0$ | 2449 | 408 | 54271 | 18.563 | 0.024 | 17.430 | 0.028 | 16.459 | 0.022 | 15.678 | 0.014 | 15.169 | 0.020 |
| $152425.21+504009.7$ | 2449 | 420 | 54271 | 17.436 | 0.014 | 17.312 | 0.015 | 17.267 | 0.014 | 16.597 | 0.018 | 16.059 | 0.019 |
| $152439.79+501147.4$ | 2449 | 468 | 54271 | 19.471 | 0.037 | 18.253 | 0.036 | 17.104 | 0.020 | 15.846 | 0.019 | 15.128 | 0.021 |
| 22852.32+492054.7 | 246 | 149 | 54272 | 20.30 | 0.0 | 19.553 | . 026 | 19.026 | . 023 | 17.999 | 0.017 | 17.29 | . 02 |

Table A.2: continued.

| System (SDSSJ) | Plate | Fiber | MJD | u | $\sigma_{u}$ | g | $\sigma_{g}$ | r | $\sigma_{r}$ | 1 | $\sigma_{i}$ | Z | $\sigma_{z}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 153009.49+384439.8 | 2936 | 13 | 54626 | 21.120 | 0.087 | 19.739 | 0.028 | 18.603 | 0.033 | 17.705 | 0.047 | 17.158 | 0.040 |
| $155808.49+264225.7$ | 2474 | 594 | 54564 | 19.820 | 0.031 | 19.177 | 0.018 | 18.473 | 0.016 | 17.314 | 0.017 | 16.557 | 0.013 |
| 155811.24+253803.2 | 2474 | 11 | 54564 | 20.940 | 0.060 | 19.207 | 0.020 | 18.082 | 0.021 | 17.268 | 0.022 | 16.832 | 0.022 |
| 162354.45+630640.4 | 2560 | 474 | 54205 | 19.811 | 0.043 | 19.114 | 0.020 | 18.478 | 0.021 | 17.377 | 0.014 | 16.693 | 0.019 |
| $162552.91+640024.9$ | 2560 | 406 | 54205 | 19.518 | 0.040 | 19.101 | 0.028 | 18.902 | 0.015 | 18.299 | 0.018 | 17.559 | 0.020 |
| 163022.96+632729.9 | 2560 | 507 | 54205 | 21.018 | 0.089 | 19.900 | 0.023 | 18.932 | 0.015 | 17.784 | 0.016 | 17.113 | 0.031 |
| 163544.74+620156.3 | 2560 | 57 | 54205 | 18.616 | 0.022 | 18.343 | 0.018 | 18.238 | 0.016 | 17.506 | 0.017 | 16.955 | 0.019 |
| 165240.74+134015.0 | 2817 | 450 | 54627 | 20.938 | 0.105 | 19.983 | 0.018 | 19.117 | 0.016 | 18.067 | 0.014 | 17.436 | 0.018 |
| 165329.97+134102.9 | 2817 | 522 | 54627 | 20.604 | 0.080 | 19.518 | 0.017 | 18.441 | 0.016 | 17.035 | 0.017 | 16.126 | 0.014 |
| 165447.75+131651.2 | 2817 | 568 | 54627 | 19.599 | 0.041 | 19.161 | 0.014 | 19.075 | 0.013 | 18.352 | 0.015 | 17.775 | 0.020 |
| 165459.27+131024.9 | 2817 | 578 | 54627 | 20.481 | 0.076 | 19.138 | 0.014 | 18.078 | 0.010 | 17.103 | 0.013 | 16.573 | 0.014 |
| $165717.36+131032.2$ | 2817 | 615 | 54627 | 21.002 | 0.104 | 19.861 | 0.030 | 19.003 | 0.024 | 18.036 | 0.012 | 17.529 | 0.023 |
| $172445.28+073324.7$ | 2818 | 310 | 54616 | 19.515 | 0.035 | 18.850 | 0.011 | 18.311 | 0.006 | 17.386 | 0.014 | 16.611 | 0.017 |
| $172552.45+632906.7$ | 2561 | 202 | 54597 | 21.220 | 0.145 | 19.785 | 0.023 | 18.760 | 0.014 | 17.713 | 0.013 | 17.188 | 0.025 |
| 173104.52+070345.0 | 2797 | 92 | 54616 | 18.262 | 0.024 | 17.738 | 0.007 | 17.375 | 0.005 | 16.478 | 0.016 | 15.837 | 0.017 |
| 173153.03+065233.6 | 2818 | 98 | 54616 | 21.084 | 0.099 | 19.635 | 0.018 | 18.712 | 0.008 | 17.907 | 0.010 | 17.365 | 0.016 |
| $173226.13+433311.2$ | 2820 | 170 | 54599 | 21.388 | 0.113 | 19.924 | 0.020 | 19.141 | 0.018 | 18.208 | 0.017 | 17.573 | 0.022 |
| $173338.91+634110.7$ | 2561 | 159 | 54597 | 19.877 | 0.041 | 19.571 | 0.021 | 19.173 | 0.014 | 18.269 | 0.022 | 17.589 | 0.020 |
| 173849.76+635042.0 | 2561 | 72 | 54597 | 20.158 | 0.044 | 19.625 | 0.016 | 19.076 | 0.020 | 18.248 | 0.018 | 17.638 | 0.023 |
| $183329.18+643151.7$ | 2552 | 481 | 54632 | 16.419 | 0.013 | 16.608 | 0.012 | 16.439 | 0.012 | 15.815 | 0.017 | 15.379 | 0.016 |
| 183453.07+413757.7 | 2798 | 466 | 54397 | 18.388 | 0.021 | 17.827 | 0.011 | 17.398 | 0.007 | 16.280 | 0.012 | 15.466 | 0.019 |
| $183809.61+415500.9$ | 2819 | 484 | 54617 | 20.091 | 0.038 | 19.023 | 0.012 | 18.530 | 0.014 | 17.927 | 0.014 | 17.391 | 0.019 |
| $184412.58+412029.4$ | 2798 | 632 | 54397 | 17.258 | 0.018 | 16.714 | 0.008 | 16.428 | 0.010 | 15.692 | 0.010 | 14.928 | 0.012 |
| 184436.94+410816.2 | 2819 | 35 | 54617 | 20.219 | 0.056 | 19.224 | 0.010 | 18.297 | 0.007 | 17.235 | 0.011 | 16.612 | 0.014 |
| 185256.00+183812.3 | 2833 | 155 | 54650 | 19.735 | 0.035 | 19.719 | 0.032 | 19.428 | 0.018 | 18.777 | 0.013 | 18.317 | 0.029 |
| 191910.86+375414.7 | 2800 | 437 | 54326 | 19.250 | 0.032 | 17.679 | 0.008 | 16.741 | 0.012 | 16.194 | 0.017 | 15.630 | 0.024 |
| 191911.33+370319.0 | 2800 | 257 | 54326 | 19.061 | 0.025 | 18.431 | 0.008 | 17.776 | 0.010 | 16.669 | 0.007 | 16.010 | 0.011 |
| $191916.88+621432.9$ | 2563 | 268 | 54653 | 20.764 | 0.095 | 19.914 | 0.022 | 19.052 | 0.020 | 18.027 | 0.012 | 17.300 | 0.018 |
| 192306.01+620310.7 | 2563 | 189 | 54653 | 20.390 | 0.065 | 19.162 | 0.014 | 18.063 | 0.016 | 17.264 | 0.015 | 16.811 | 0.022 |
| $201239.31+601710.3$ | 2564 | 499 | 54275 | 19.938 | 2.182 | 19.034 | 0.521 | 18.752 | 0.258 | 17.625 | 0.045 | 16.752 | 0.016 |
| $204647.27+021805.4$ | 2815 | 272 | 54414 | 17.189 | 0.015 | 17.076 | 0.011 | 16.684 | 0.013 | 15.770 | 0.011 | 15.139 | 0.017 |
| $220838.56+050609.8$ | 2323 | 247 | 54380 | 20.963 | 0.073 | 19.897 | 0.024 | 18.873 | 0.013 | 17.472 | 0.016 | 16.640 | 0.019 |
| $221343.64+072221.3$ | 2308 | 561 | 54379 | 18.590 | 0.026 | 18.291 | 0.019 | 17.514 | 0.014 | 16.453 | 0.015 | 15.834 | 0.014 |
| $221453.16+055423.1$ | 2323 | 76 | 54380 | 21.188 | 0.108 | 20.105 | 0.021 | 19.067 | 0.015 | 18.411 | 0.015 | 18.010 | 0.027 |
| $222822.73+391239.7$ | 2620 | 78 | 54397 | 19.134 | 0.025 | 18.419 | 0.008 | 17.659 | 0.011 | 16.718 | 0.015 | 16.171 | 0.018 |
| $224307.59+312239.1$ | 2627 | 388 | 54379 | 20.759 | 0.097 | 19.585 | 0.022 | 18.689 | 0.015 | 17.283 | 0.010 | 16.264 | 0.017 |
| $224819.40+304803.6$ | 2627 | 160 | 54379 | 21.231 | 0.089 | 19.888 | 0.015 | 18.893 | 0.011 | 17.492 | 0.016 | 16.758 | 0.016 |
| $225117.28+310939.8$ | 2621 | 597 | 54380 | 15.748 | 0.017 | 15.900 | 0.010 | 15.488 | 0.006 | 14.837 | 0.011 | 14.442 | 0.015 |
| $225145.03+302807.6$ | 2627 | 63 | 54379 | 21.247 | 0.098 | 19.958 | 0.016 | 18.795 | 0.011 | 17.818 | 0.014 | 17.246 | 0.019 |
| $225716.58+074534.3$ | 2325 | 379 | 54082 | 20.545 | 0.055 | 19.507 | 0.022 | 18.423 | 0.013 | 17.511 | 0.019 | 16.980 | 0.019 |
| $225847.57+071026.5$ | 2325 | 498 | 54082 | 20.321 | 0.051 | 19.748 | 0.022 | 19.281 | 0.019 | 18.196 | 0.016 | 17.343 | 0.025 |
| $230248.99+081052.5$ | 2325 | 601 | 54082 | 21.199 | 0.106 | 19.584 | 0.018 | 18.367 | 0.016 | 17.461 | 0.018 | 16.990 | 0.027 |
| $230833.71+224052.6$ | 2629 | 467 | 54087 | 20.001 | 0.038 | 19.565 | 0.015 | 18.807 | 0.018 | 18.187 | 0.021 | 17.798 | 0.026 |
| $231105.66+220208.6$ | 2629 | 177 | 54087 | 19.609 | 0.042 | 19.074 | 0.016 | 18.382 | 0.016 | 17.452 | 0.016 | 16.801 | 0.019 |
| $233856.89+074456.4$ | 2628 | 133 | 54326 | 19.523 | 0.034 | 19.201 | 0.019 | 18.409 | 0.017 | 17.340 | 0.012 | 16.692 | 0.016 |
| $233922.26+074400.3$ | 2628 | 88 | 54326 | 19.836 | 0.041 | 19.089 | 0.019 | 18.221 | 0.017 | 17.386 | 0.012 | 16.887 | 0.016 |
| $\underline{234106.82+083550.3 ~}$ | 2628 | 112 | 54326 | 20.202 | 0.051 | 19.508 | 0.018 | 19.133 | 0.015 | 18.151 | 0.015 | 17.426 | 0.020 |

Table A.3: Stellar parameters of the 277 WDMS systems identified with SEGUE. For the 84 binaries containing a DB, DC, or unclear white dwarf spectral type, only some parameters obtained for the secondary star are given. Also included are the 24 candidate systems.

| System | Type | $T_{\text {eff }}$ | $\sigma_{T_{\text {eff }}}$ | $\log g$ | $\sigma_{\log g}$ | $M_{\mathrm{wd}}$ | $\sigma_{M_{\mathrm{wd}}}$ | $d_{\mathrm{wd}}$ | $\sigma_{d_{\mathrm{wd}}}$ | Sp2 | $d_{\text {sec }}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |$\sigma_{d_{\text {sec }}}$

Table A.3: continued.

| System | Type | $T_{\text {eff }}$ | ${ }^{\sigma} T_{\text {eff }}$ | $\log g$ | $\sigma_{\log g}$ | $M_{\text {wd }}$ | $\sigma_{M_{\text {wd }}}$ | $d_{\text {wd }}$ | $\sigma^{d_{\text {wd }}}$ | Sp2 | $d_{\text {sec }}$ | $\sigma_{d_{\text {sec }}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SDSSJ000504.91+243409.6 | DA/dM | 13127 | 2160 | 8.16 | 0.34 | 0.71 | 0.22 | 304 | 70 | 4 | 350 | 103 |
| SDSSJ000531.09-054343.2 | DA/dM | 13127 | 657 | 7.91 | 0.14 | 0.56 | 0.08 | 129 | 11 | 4 | 167 | 49 |
| SDSSJ000559.87-054416.0 | DA/dM | 31128 | 921 | 7.89 | 0.21 | 0.59 | 0.12 | 692 | 99 | 2 | 553 | 132 |
| SDSSJ000651.91+284647.1 | DA/dM | 12976 | 688 | 7.83 | 0.21 | 0.51 | 0.12 | 343 | 44 | 3 | 420 | 83 |
| SDSSJ000829.92+273340.5 | DA/dM | 15782 | 1481 | 7.73 | 0.37 | 0.47 | 0.20 | 615 | 131 | 2 | 656 | 156 |
| SDSSJ000935.50+243251.2 | DA/dM | 14393 | 4221 | 8.58 | 0.68 | 0.98 | 0.32 | 347 | 162 | 2 | 479 | 114 |
| SDSSJ003804.41+083416.9 | DA/dM | 8673 | 255 | 7.73 | 0.59 | 0.45 | 0.35 | 216 | 69 | 3 | 223 | 44 |
| SDSSJ010341.59+003132.6 | DA/dM | 21535 | 1234 | 7.76 | 0.21 | 0.50 | 0.11 | 849 | 113 | 2 | 1159 | 276 |
| SDSSJ010448.50-010516.7 | cand |  |  |  |  |  |  |  |  | 3 | 339 | 67 |
| SDSSJ010704.58+005907.9 | cand |  |  |  |  |  |  |  |  | 1 | 1063 | 208 |
| SDSSJ011123.90+000935.2 | DA/dM | 15071 | 547 | 7.72 | 0.13 | 0.47 | 0.06 | 458 | 36 | 2 | 654 | 156 |
| SDSSJ011932.38-090219.1 | DA/dM | 15601 | 1500 | 8.44 | 0.35 | 0.89 | 0.20 | 497 | 126 | 2 | 629 | 150 |
| SDSSJ013000.74+385205.4 | DA:/dM |  |  |  |  |  |  |  |  | 1 | 805 | 158 |
| SDSSJ014143.68-093811.7 | DC/dM |  |  |  |  |  |  |  |  | 3 | 642 | 126 |
| SDSSJ014147.33-094200.3 | cand |  |  |  |  |  |  |  |  | 3 | 490 | 96 |
| SDSSJ014232.59-083528.4 | DA/dM | 9187 | 148 | 8.77 | 0.18 | 1.08 | 0.10 | 113 | 17 | 3 | 428 | 84 |
| SDSSJ020351.29+004025.0 | DA/dM | 10918 | 589 | 7.98 | 0.45 | 0.59 | 0.28 | 420 | 115 | 3 | 501 | 99 |
| SDSSJ021145.57+071831.1 | DA/dM | 19193 | 1301 | 8.09 | 0.26 | 0.67 | 0.16 | 700 | 123 | 3 | 758 | 149 |
| SDSSJ023438.48+244535.6 | WD/dM |  |  |  |  |  |  |  |  | 1 | 1141 | 223 |
| SDSSJ023526.43+280026.6 | DA/dM | 31128 | 1884 | 8.07 | 0.45 | 0.69 | 0.27 | 1344 | 401 | 2 | 1160 | 276 |
| SDSSJ023938.04+273654.0 | DA/dM | 12681 | 1145 | 7.91 | 0.38 | 0.56 | 0.23 | 468 | 107 | 4 | 774 | 228 |
| SDSSJ024942.92+335032.5 | DA/dM | 14065 | 3771 | 8.30 | 0.96 | 0.80 | 0.50 | 605 | 347 | 1 | 769 | 151 |
| SDSSJ025347.51+335221.0 | DA/dM | 33740 | 2650 | 8.59 | 0.41 | 1.00 | 0.21 | 756 | 241 | 2 | 618 | 147 |
| SDSSJ025555.87+352830.2 | DB/dM |  |  |  |  |  |  |  |  | 2 | 299 | 71 |
| SDSSJ030138.24+050218.9 | DA/dM | 11045 | 275 | 8.40 | 0.17 | 0.86 | 0.10 | 161 | 20 | 4 | 324 | 95 |
| SDSSJ030247.65+372125.9 | WD/dM |  |  |  |  |  |  |  |  | 1 | 1080 | 212 |
| SDSSJ030716.44+384822.8 | DA:/dM |  |  |  |  |  |  |  |  | 3 | 373 | 73 |
| SDSSJ030900.89+384835.2 | DA/dM | 18330 | 1516 | 8.12 | 0.33 | 0.69 | 0.21 | 788 | 175 | 4 | 589 | 173 |
| SDSSJ030956.31+411049.2 | DA:/dM |  |  |  |  |  |  |  |  | 3 | 216 | 43 |
| SDSSJ031200.17+401336.9 | cand |  |  |  |  |  |  |  |  | 1 | 1232 | 241 |
| SDSSJ031657.47+395931.9 | cand |  |  |  |  |  |  |  |  | 1 | 761 | 149 |
| SDSSJ031803.98+423034.4 | DA/dM | 8475 | 105 | 8.29 | 0.15 | 0.78 | 0.10 | 78 | 9 | 3 | 186 | 37 |
| SDSSJ032030.52+044243.5 | DA/dM | 19193 | 2046 | 8.13 | 0.43 | 0.70 | 0.27 | 303 | 86 | 4 | 268 | 79 |
| SDSSJ032140.00+415307.5 | DB/dM |  |  |  |  |  |  |  |  | 3 | 674 | 133 |
| SDSSJ034913.69+085810.8 | DA:/dM | 10427 | 761 | 9.29 | 0.33 | 1.30 | 0.10 | 137 | 44 | 3 | 574 | 113 |
| SDSSJ041716.58+055522.4 | DA/dM | 21785 | 2645 | 7.30 | 0.44 | 0.34 | 0.15 | 1421 | 404 | 3 | 1012 | 199 |
| SDSSJ042053.72+064922.4 | WD/dM |  |  |  |  |  |  |  |  | 5 | 173 | 89 |
| SDSSJ044046.91-050413.0 | DA/dM | 18120 | 1246 | 7.79 | 0.27 | 0.51 | 0.15 | 646 | 105 | 5 | 345 | 176 |
| SDSSJ044218.26-044820.2 | DA/dM | 12110 | 2701 | 7.89 | 0.62 | 0.54 | 0.39 | 464 | 167 | 3 | 464 | 91 |
| SDSSJ044547.53-044559.1 | cand |  |  |  |  |  |  |  |  | 0 | 1081 | 146 |
| SDSSJ044831.02+214909.8 | $\mathrm{DA} / \mathrm{dM}$ | 10548 | 639 | 8.73 | 0.41 | 1.06 | 0.19 | 150 | 47 | 3 | 311 | 61 |
| SDSSJ054544.63+822205.9 | cand |  |  |  |  |  |  |  |  | 0 | 515 | 69 |
| SDSSJ055956.76+224704.6 | cand |  |  |  |  |  |  |  |  | 3 | 1214 | 239 |
| SDSSJ063139.13+822827.8 | DA/dM | 24726 | 3614 | 7.74 | 0.59 | 0.50 | 0.33 | 986 | 337 | 3 | 754 | 149 |
| SDSSJ063805.21+835526.9 | DA/dM | 20566 | 1325 | 7.78 | 0.24 | 0.51 | 0.13 | 685 | 102 | 5 | 431 | 221 |
| SDSSJ064147.70+364058.9 | cand |  |  |  |  |  |  |  |  | 1 | 675 | 132 |
| SDSSJ064212.72+381638.4 | DA/dM | 10793 | 366 | 8.03 | 0.29 | 0.62 | 0.19 | 316 | 59 | 4 | 376 | 111 |
| SDSSJ064723.99+840724.1 | DA/dM | 12681 | 1596 | 7.69 | 0.50 | 0.44 | 0.28 | 579 | 160 | 3 | 1044 | 206 |
| SDSSJ064812.76+381005.9 | DA/dM | 19193 | 3292 | 8.00 | 0.61 | 0.62 | 0.38 | 726 | 271 | 1 | 709 | 139 |
| SDSSJ070322.17+664908.0 | WD/dM |  |  |  |  |  |  |  |  | 3 | 322 | 63 |
| SDSSJ070336.89+385142.2 | DA:/dM | 16717 | 12092 | 9.50 | 1.40 | 1.37 | 0.40 | 236 | 71 | 3 | 609 | 120 |
| SDSSJ070628.57+383650.2 | DB/dM |  |  |  |  |  |  |  |  | 2 | 648 | 154 |
| SDSSJ071309.72+401249.4 | DA/dM | 14228 | 2766 | 8.44 | 0.41 | 0.89 | 0.24 | 311 | 92 | 3 | 456 | 90 |
| SDSSJ072016.98+303824.6 | cand |  |  |  |  |  |  |  |  | 3 | 340 | 67 |
| SDSSJ072130.60+374228.3 | DA/dM | 11433 | 1040 | 8.54 | 0.38 | 0.95 | 0.21 | 307 | 87 | 4 | 493 | 145 |
| SDSSJ072156.68+364048.5 | DA:/dM |  |  |  |  |  |  |  |  | 1 | 400 | 78 |
| SDSSJ072222.66+385702.9 | DA:/dM |  |  |  |  |  |  |  |  | 1 | 306 | 60 |
| SDSSJ072251.06+385944.6 | DA:/dM |  |  |  |  |  |  |  |  | 4 | 264 | 78 |
| SDSSJ072434.72+321609.4 | DA/dM | 11699 | 1594 | 9.09 | 0.18 | 1.23 | 0.06 | 106 | 17 | 4 | 228 | 67 |

Table A.3: continued.

| SyStem |  | Type | $T_{\text {eff }}$ | $\sigma_{T} T_{\text {eff }}$ | $\log g$ | $\sigma_{\log g} g$ | $M_{\text {wd }}$ | $\sigma_{M_{\mathrm{wd}}}$ | $d_{\text {wd }}$ | $\sigma_{d_{\mathrm{wd}}}$ | Sp2 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |$d_{\text {sec }} \sigma_{d_{\text {sec }}}$

Table A.3: continued.

| System | Type | $T_{\text {eff }}$ | $\sigma_{T_{\text {eff }}}$ | $\log g$ | $\sigma_{\log g}$ | $M_{\text {wd }}$ | $\sigma^{M_{\mathrm{wd}}}$ | $d_{\text {wd }}$ | $\sigma_{d_{\text {wd }}}$ | Sp2 | $d_{\text {sec }}$ | $\sigma_{d_{\text {sec }}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SDSSJ100347.63+352958.2 | DA/dM | 18974 | 1669 | 8.13 | 0.31 | 0.70 | 0.20 | 780 | 166 | 3 | 887 | 175 |
| SDSSJ100533.84+250149.4 | DC/dM |  |  |  |  |  |  |  |  | 2 | 808 | 193 |
| SDSSJ100732.50+254334.6 | DC/dM |  |  |  |  |  |  |  |  | 4 | 378 | 111 |
| SDSSJ100821.19+260213.9 | DB/dM |  |  |  |  |  |  |  |  | 3 | 891 | 175 |
| SDSSJ100828.18+263732.5 | WD/dM |  |  |  |  |  |  |  |  | 0 | 408 | 55 |
| SDSSJ100900.48+360457.6 | DB/dM |  |  |  |  |  |  |  |  | 1 | 1071 | 210 |
| SDSSJ101032.62+344527.9 | DA/dM | 21289 | 2513 | 8.13 | 0.43 | 0.70 | 0.27 | 939 | 268 | 2 | 1168 | 278 |
| SDSSJ102102.25+174439.9 | DA/dM | 32972 | 2038 | 8.65 | 0.36 | 1.03 | 0.18 | 720 | 207 | 4 | 435 | 128 |
| SDSSJ102205.96+080246.6 | DA/dM | 22811 | 1240 | 7.84 | 0.19 | 0.55 | 0.10 | 663 | 81 | 2 | 780 | 186 |
| SDSSJ102256.25+095418.5 | DA/dM | 8282 | 165 | 8.26 | 0.36 | 0.76 | 0.23 | 157 | 39 | 4 | 280 | 82 |
| SDSSJ102438.46+162458.2 | DA/dM | 15422 | 1049 | 8.31 | 0.21 | 0.81 | 0.13 | 385 | 59 | 3 | 403 | 79 |
| SDSSJ102515.38+174937.6 | DA/dM | 22550 | 1290 | 7.84 | 0.21 | 0.54 | 0.11 | 857 | 112 | 4 | 638 | 188 |
| SDSSJ102623.21+162938.5 | DA/dM | 20331 | 2207 | 7.41 | 0.40 | 0.37 | 0.16 | 1197 | 303 | 3 | 717 | 141 |
| SDSSJ102843.97+443252.6 | DA/dM | 19193 | 1791 | 8.27 | 0.38 | 0.79 | 0.24 | 470 | 126 | 2 | 317 | 76 |
| SDSSJ102857.78+093129.8 | DA/dM | 18756 | 313 | 8.29 | 0.06 | 0.80 | 0.04 | 144 | 7 | 3 | 125 | 25 |
| SDSSJ103432.27+442956.6 | DC/dM |  |  |  |  |  |  |  |  | 4 | 346 | 102 |
| SDSSJ104751.79+483503.7 | DA/dM | 12681 | 1394 | 7.84 | 0.45 | 0.52 | 0.27 | 610 | 161 | 3 | 1048 | 206 |
| SDSSJ105008.93+473748.0 | WD/dM |  |  |  |  |  |  |  |  | 2 | 539 | 128 |
| SDSSJ105042.59+470628.7 | WD/dM |  |  |  |  |  |  |  |  | 4 | 384 | 113 |
| SDSSJ105051.70-001207.7 | DA/dM | 11433 | 700 | 8.49 | 0.34 | 0.92 | 0.19 | 260 | 65 | 3 | 369 | 73 |
| SDSSJ105526.23+472923.0 | DA:/dM | 10073 | 579 | 9.50 | 0.08 | 1.37 | 0.02 | 73 | 7 | 3 | 269 | 53 |
| SDSSJ105730.98+474614.3 | DA/dM | 15422 | 4502 | 7.46 | 1.62 | 0.36 | 0.87 | 1369 | 976 | 2 | 965 | 230 |
| SDSSJ110442.27-153936.2 | cand |  |  |  |  |  |  |  |  | 0 | 560 | 75 |
| SDSSJ110517.60+385125.7 | DA/dM | 10548 | 142 | 8.18 | 0.13 | 0.71 | 0.09 | 205 | 19 | 3 | 462 | 91 |
| SDSSJ110520.63+282408.7 | DC/dM |  |  |  |  |  |  |  |  | 6 | 107 | 49 |
| SDSSJ110529.78-164719.3 | DA/dM | 25891 | 1896 | 7.91 | 0.30 | 0.59 | 0.17 | 851 | 166 | 3 | 773 | 152 |
| SDSSJ110652.91+284245.4 | DA/dM | 12536 | 1486 | 8.20 | 0.39 | 0.73 | 0.25 | 436 | 115 | 3 | 396 | 78 |
| SDSSJ110734.09-162414.4 | DA/dM | 33740 | 1070 | 7.81 | 0.20 | 0.56 | 0.10 | 544 | 75 | 2 | 391 | 93 |
| SDSSJ110738.05+380051.3 | DA/dM | 8977 | 361 | 7.69 | 0.88 | 0.43 | 0.53 | 407 | 186 | 4 | 515 | 152 |
| SDSSJ110741.47+283003.1 | DA/dM | 9731 | 403 | 9.33 | 0.26 | 1.32 | 0.08 | 83 | 22 | 2 | 341 | 81 |
| SDSSJ110749.80+290939.9 | DA/dM | 12110 | 2146 | 7.39 | 1.01 | 0.33 | 0.53 | 1259 | 622 | 1 | 896 | 176 |
| SDSSJ110758.94+275346.2 | DA/dM | 10307 | 678 | 9.15 | 0.56 | 1.26 | 0.17 | 138 | 67 | 2 | 635 | 151 |
| SDSSJ110834.66-154847.3 | DA/dM | 12976 | 1622 | 7.83 | 0.46 | 0.51 | 0.27 | 452 | 119 | 3 | 573 | 113 |
| SDSSJ110854.22-145147.0 | DA/dM | 19640 | 3849 | 7.43 | 0.71 | 0.37 | 0.34 | 1328 | 520 | 2 | 1123 | 268 |
| SDSSJ111210.25+392453.1 | DA/dM | 9731 | 246 | 8.43 | 0.29 | 0.87 | 0.18 | 178 | 38 | 2 | 378 | 90 |
| SDSSJ111251.20+190700.3 | DA/dM | 12828 | 941 | 7.57 | 0.27 | 0.39 | 0.13 | 588 | 95 | 2 | 1017 | 242 |
| SDSSJ111419.27+083829.0 | DA/dM | 15422 | 624 | 7.97 | 0.13 | 0.60 | 0.08 | 356 | 30 | 4 | 452 | 133 |
| SDSSJ111428.51+590209.1 | DC/dM |  |  |  |  |  |  |  |  | 5 | 255 | 130 |
| SDSSJ111459.92+092411.1 | DA/dM | 10427 | 211 | 8.28 | 0.23 | 0.78 | 0.15 | 236 | 38 | 5 | 465 | 238 |
| SDSSJ111501.51-120321.9 | DA/dM | 10548 | 483 | 8.33 | 0.55 | 0.81 | 0.33 | 288 | 107 | 5 | 421 | 215 |
| SDSSJ111615.73+590509.3 | DA/dM | 13588 | 1465 | 8.55 | 0.18 | 0.96 | 0.11 | 268 | 39 | 2 | 519 | 124 |
| SDSSJ111710.54-125540.9 | DA/dM | 15964 | 1472 | 7.68 | 0.37 | 0.45 | 0.19 | 741 | 158 | 3 | 760 | 150 |
| SDSSJ111722.07-104556.1 | DB/dM |  |  |  |  |  |  |  |  | 3 | 303 | 60 |
| SDSSJ111920.11-104810.6 | DB/dM |  |  |  |  |  |  |  |  | 2 | 487 | 116 |
| SDSSJ111950.69+185351.0 | DC/dM |  |  |  |  |  |  |  |  | 2 | 451 | 107 |
| SDSSJ112012.71+190126.8 | DA/dM | 12976 | 2861 | 8.23 | 0.47 | 0.75 | 0.29 | 259 | 81 | 3 | 314 | 62 |
| SDSSJ112016.08+675750.6 | DA:/dM | 10073 | 635 | 8.13 | 0.92 | 0.68 | 0.54 | 419 | 224 | 3 | 404 | 80 |
| SDSSJ112308.40-115559.3 | DA/dM | 10073 | 215 | 9.12 | 0.25 | 1.25 | 0.08 | 64 | 14 | 5 | 117 | 60 |
| SDSSJ112409.43+590935.8 | DA/dM | 9081 | 292 | 7.80 | 0.61 | 0.49 | 0.37 | 341 | 115 | 4 | 309 | 91 |
| SDSSJ112651.03-081640.1 | DA/dM | 10670 | 620 | 9.11 | 0.49 | 1.25 | 0.26 | 168 | 99 | 2 | 504 | 120 |
| SDSSJ112812.63+671738.3 | DA/dM | 11565 | 625 | 7.91 | 0.31 | 0.55 | 0.19 | 355 | 67 | 3 | 364 | 72 |
| SDSSJ113457.72+655408.7 | DC/dM |  |  |  |  |  |  |  |  | 4 | 358 | 105 |
| SDSSJ113546.87+675832.3 | WD/dM |  |  |  |  |  |  |  |  | 3 | 417 | 82 |
| SDSSJ113557.51+010310.4 | DA:/dM | 30071 | 3076 | 6.41 | 0.66 | 0.18 | 0.14 | 3523 | 1174 | 4 | 550 | 162 |
| SDSSJ113600.68+001212.2 | DA:/dM | 36154 | 3401 | 8.13 | 0.49 | 0.74 | 0.28 | 1420 | 465 | 2 | 1356 | 323 |
| SDSSJ113800.35-001144.4 | DA/dM | 16336 | 834 | 8.01 | 0.19 | 0.62 | 0.12 | 417 | 52 | 3 | 667 | 131 |
| SDSSJ114316.55+665813.1 | DA:/dM | 31488 | 2259 | 8.27 | 0.50 | 0.81 | 0.29 | 1093 | 378 | 3 | 642 | 126 |
| SDSSJ120953.67+185815.7 | DA/dM | 26801 | 3913 | 8.53 | 0.48 | 0.96 | 0.25 | 701 | 246 | 1 | 590 | 116 |
| SDSSJ121033.60+185346.2 | DA/dM | 17106 | 1701 | 7.89 | 0.40 | 0.56 | 0.24 | 722 | 175 | 3 | 827 | 163 |

Table A.3: continued.

| SyStem |  | Type | $T_{\text {eff }}$ | $\sigma_{T} T_{\text {eff }}$ | $\log g$ | $\sigma_{\log g}$ | $M_{\text {wd }}$ | $\sigma_{M_{\mathrm{wd}}}$ | $d_{\text {wd }}$ | $\sigma_{d_{\mathrm{wd}}}$ | Sp2 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |$d_{\text {sec }} \sigma_{d_{\text {sec }}}$

Table A.3: continued.

| System | Type | $T_{\text {eff }}$ | $\sigma^{T_{\text {eff }}}$ | $\log g$ | $\sigma_{\log g}$ | $M_{\text {wd }}$ | $\sigma_{M_{\mathrm{wd}}}$ | $d_{\text {wd }}$ | $\sigma_{d_{\mathrm{wd}}}$ | Sp2 | $d_{\text {sec }}$ | $\sigma_{d_{\text {sec }}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SDSSJ143746.69+573706.0 | DA/dM | 17912 | 846 | 8.12 | 0.19 | 0.69 | 0.12 | 392 | 50 | 4 | 323 | 95 |
| SDSSJ143947.78+574115.4 | DB/dM |  |  |  |  |  |  |  |  | 1 | 1004 | 197 |
| SDSSJ143957.92+573944.6 | DA/dM | 29727 | 3054 | 7.66 | 0.57 | 0.48 | 0.30 | 961 | 327 | 1 | 571 | 112 |
| SDSSJ144258.47+001031.5 | DB/dM |  |  |  |  |  |  |  |  | 4 | 351 | 103 |
| SDSSJ144600.37+000817.0 | DA/dM | 10670 | 425 | 7.97 | 0.39 | 0.58 | 0.25 | 448 | 108 | 5 | 440 | 225 |
| SDSSJ145305.77+001048.2 | DA/dM | 11565 | 569 | 8.55 | 0.19 | 0.95 | 0.11 | 236 | 36 | 4 | 279 | 82 |
| SDSSJ150438.86+321443.4 | DA/dM | 24163 | 3303 | 7.76 | 0.54 | 0.51 | 0.30 | 908 | 289 | 1 | 878 | 172 |
| SDSSJ151744.70+062011.9 | WD/dM |  |  |  |  |  |  |  |  | 3 | 466 | 92 |
| SDSSJ151852.44+074459.3 | DA/dM | 19868 | 2304 | 7.72 | 0.47 | 0.48 | 0.26 | 1054 | 290 | 4 | 580 | 171 |
| SDSSJ152002.84+081231.0 | DA/dM | 17505 | 789 | 8.06 | 0.17 | 0.65 | 0.11 | 477 | 55 | 4 | 437 | 129 |
| SDSSJ152033.43+063442.9 | DA/dM | 11302 | 480 | 8.48 | 0.25 | 0.91 | 0.15 | 203 | 38 | 4 | 366 | 108 |
| SDSSJ152416.97+504749.0 | DA/dM | 34926 | 1595 | 8.31 | 0.24 | 0.84 | 0.14 | 430 | 76 | 2 | 269 | 64 |
| SDSSJ152425.21+504009.7 | DA/dM | 19640 | 587 | 8.14 | 0.12 | 0.71 | 0.07 | 221 | 18 | 3 | 336 | 66 |
| SDSSJ152439.79+501147.4 | DA:/dM | 27425 | 3576 | 8.27 | 0.55 | 0.80 | 0.32 | 749 | 277 | 3 | 209 | 41 |
| SDSSJ152852.32+492054.7 | DA/dM | 9958 | 461 | 8.26 | 0.66 | 0.76 | 0.40 | 282 | 120 | 4 | 435 | 128 |
| SDSSJ153009.49+384439.8 | DA:/dM | 10073 | 883 | 8.50 | 1.16 | 0.92 | 0.49 | 356 | 245 | 2 | 669 | 159 |
| SDSSJ155808.49+264225.7 | DA/dM | 14560 | 4069 | 8.74 | 0.64 | 1.07 | 0.26 | 281 | 129 | 4 | 320 | 94 |
| SDSSJ155811.24+253803.2 | WD/dM |  |  |  |  |  |  |  |  | 1 | 745 | 146 |
| SDSSJ162354.45+630640.4 | DA/dM | 9731 | 289 | 8.63 | 0.35 | 1.00 | 0.19 | 180 | 48 | 4 | 335 | 99 |
| SDSSJ162552.91+640024.9 | DA/dM | 8773 | 169 | 8.31 | 0.27 | 0.79 | 0.17 | 155 | 30 | 6 | 212 | 98 |
| SDSSJ163022.96+632729.9 | WD/dM |  |  |  |  |  |  |  |  | 3 | 523 | 103 |
| SDSSJ163544.74+620156.3 | DA/dM | 17505 | 582 | 7.81 | 0.13 | 0.52 | 0.07 | 378 | 31 | 3 | 514 | 101 |
| SDSSJ165240.74+134015.0 | DA:/dM | 11173 | 5598 | 8.45 | 1.07 | 0.89 | 0.48 | 389 | 248 | 3 | 627 | 123 |
| SDSSJ165329.97+134102.9 | WD/dM |  |  |  |  |  |  |  |  | 4 | 260 | 76 |
| SDSSJ165447.75+131651.2 | DA/dM | 16910 | 855 | 7.87 | 0.20 | 0.55 | 0.11 | 514 | 63 | 4 | 547 | 161 |
| SDSSJ165459.27+131024.9 | DA/dM | 15601 | 2019 | 7.50 | 0.51 | 0.38 | 0.24 | 929 | 268 | 2 | 528 | 126 |
| SDSSJ165717.36+131032.2 | DA/dM | 22811 | 4411 | 7.81 | 0.84 | 0.53 | 0.49 | 1238 | 579 | 2 | 818 | 195 |
| SDSSJ172445.28+073324.7 | DA/dM | 13588 | 989 | 8.02 | 0.24 | 0.62 | 0.15 | 384 | 59 | 4 | 324 | 95 |
| SDSSJ172552.45+632906.7 | DA:/dM |  |  |  |  |  |  |  |  | 2 | 693 | 165 |
| SDSSJ173104.52+070345.0 | DA/dM | 14228 | 1186 | 8.02 | 0.30 | 0.62 | 0.18 | 214 | 40 | 4 | 224 | 66 |
| SDSSJ173153.03+065233.6 | WD/dM |  |  |  |  |  |  |  |  | 1 | 912 | 179 |
| SDSSJ173226.13+433311.2 | cand |  |  |  |  |  |  |  |  | 2 | 866 | 206 |
| SDSSJ173338.91+634110.7 | DA/dM | 27743 | 2595 | 7.71 | 0.39 | 0.50 | 0.20 | 1228 | 298 | 3 | 671 | 132 |
| SDSSJ173849.76+635042.0 | DA/dM | 14560 | 2153 | 8.50 | 0.39 | 0.93 | 0.22 | 394 | 114 | 3 | 704 | 139 |
| SDSSJ183329.18+643151.7 | DA/dM | 51068 | 2064 | 7.86 | 0.14 | 0.63 | 0.06 | 454 | 47 | 2 | 310 | 74 |
| SDSSJ183453.07+413757.7 | DA/dM | 9619 | 147 | 8.42 | 0.17 | 0.87 | 0.11 | 108 | 14 | 4 | 184 | 54 |
| SDSSJ183809.61+415500.9 | WD/dM |  |  |  |  |  |  |  |  | 4 | 493 | 145 |
| SDSSJ184412.58+412029.4 | DA/dM | 7554 | 28 | 7.45 | 0.12 | 0.33 | 0.05 | 75 | 5 | 6 | 58 | 27 |
| SDSSJ184436.94+410816.2 | DA/dM | 10670 | 939 | 8.13 | 0.73 | 0.68 | 0.45 | 378 | 169 | 3 | 421 | 83 |
| SDSSJ185256.00+183812.3 | DA:/dM |  |  |  |  |  |  |  |  | 2 | 1403 | 334 |
| SDSSJ191910.86+375414.7 | WD/dM |  |  |  |  |  |  |  |  | 1 | 414 | 81 |
| SDSSJ191911.33+370319.0 | DA/dM | 17912 | 1229 | 7.92 | 0.27 | 0.57 | 0.16 | 453 | 76 | 3 | 320 | 63 |
| SDSSJ191916.88+621432.9 | WD/dM |  |  |  |  |  |  |  |  | 3 | 583 | 115 |
| SDSSJ192306.01+620310.7 | DA:/dM | 14228 | 3640 | 8.36 | 0.95 | 0.84 | 0.48 | 516 | 298 | 1 | 717 | 140 |
| SDSSJ201239.31+601710.3 | DA/dM | 32222 | 192 | 7.79 | 0.05 | 0.55 | 0.02 | 332 | 12 | 5 | 236 | 121 |
| SDSSJ204647.27+021805.4 | DB/dM |  |  |  |  |  |  |  |  | 3 | 218 | 43 |
| SDSSJ220838.56+050609.8 | cand |  |  |  |  |  |  |  |  | 4 | 316 | 93 |
| SDSSJ221343.64+072221.3 | DB/dM |  |  |  |  |  |  |  |  | 3 | 272 | 54 |
| SDSSJ221453.16+055423.1 | cand |  |  |  |  |  |  |  |  | 1 | 1225 | 240 |
| SDSSJ222822.73+391239.7 | DA/dM | 23343 | 4002 | 7.48 | 0.57 | 0.40 | 0.26 | 760 | 252 | 3 | 358 | 70 |
| SDSSJ224307.59+312239.1 | DC/dM |  |  |  |  |  |  |  |  | 5 | 171 | 87 |
| SDSSJ224819.40+304803.6 | WD/dM |  |  |  |  |  |  |  |  | 4 | 346 | 102 |
| SDSSJ225117.28+310939.8 | DA/dM | 40565 | 1388 | 7.97 | 0.16 | 0.66 | 0.09 | 261 | 29 | 1 | 245 | 48 |
| SDSSJ225145.03+302807.6 | cand |  |  |  |  |  |  |  |  | 2 | 715 | 170 |
| SDSSJ225716.58+074534.3 | DA:/dM | 11433 | 8054 | 8.73 | 1.24 | 1.06 | 0.44 | 331 | 265 | 2 | 773 | 184 |
| SDSSJ225847.57+071026.5 | DA/dM | 8475 | 272 | 8.07 | 0.57 | 0.64 | 0.37 | 248 | 87 | 5 | 351 | 180 |
| SDSSJ230248.99+081052.5 | cand |  |  |  |  |  |  |  |  | 1 | 896 | 175 |
| SDSSJ230833.71+224052.6 | DC/dM |  |  |  |  |  |  |  |  | 1 | 1365 | 267 |
| SDSSJ231105.66+220208.6 | DA/dM | 10189 | 460 | 8.92 | 0.40 | 1.16 | 0.15 | 163 | 52 | 3 | 536 | 105 |



Figure A.1: Radial velocities of the Na absorption doublet for the 29 PCEBs.


Figure A.2: Radial velocities of the $\mathrm{H} \alpha$, emission line for the 28 PCEBs.

Table A.3: continued.

| System | Type | $T_{\text {eff }}$ | $\sigma_{T_{\text {eff }}}$ | $\log g$ | $\sigma_{\log g}$ | $M_{\mathrm{wd}}$ | $\sigma_{M_{\mathrm{wd}}}$ | $d_{\mathrm{wd}}$ | $\sigma_{d_{\mathrm{wd}}}$ | Sp2 | $d_{\text {sec }}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |$\sigma_{d_{\text {sec }}}$.

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# Curriculum Vitae 

| Name | Ada Nebot Gómez-Morán |
| :--- | :--- |
| Born | September 17, 1979 in Oviedo |
| Nationality | Spanish |
| Marital status | Single |

Sept. 1985-July 1993 Primary School at Colegio Público La Luna, Oviedo
Sept. 1993-July 1998 Secondary School at Instituto Alfonso II El Sabio, Oviedo
Oct. 1998-July 2002 1st degree in Physics at Universidad de Oviedo.
Oct. 2002-Feb. 2006 Diploma in Physics with concentration in Astrophysics at Universidad de La Laguna.

Since April 2006 PhD studies in astrophysics at the Technische Universität Berlin, supervisor: Axel Schwope


[^0]:    ${ }^{1}$ http://pleiadi.pd.astro.it/

[^1]:    ${ }^{2}$ Different mechanisms are involved in the broadening of spectral lines: i) Natural broadening: electrons stay in a certain level a finite time before they spontaneously decay, and each level has a certain energy given by Heisenberg uncertainty principle, ii) Thermal doppler broadening, iii) Collisional broadening or Stark effect (pressure broadening): line shifting or splitting under the action of an electric field, iv) Zeeman effect: under a magnetic field lines split and if we don't have enough resolution the lines will appear to be one broad line, v) Turbulent broadening, and vi) Rotational broadening. In hot white dwarfs due to the high densities the lines are broadened mostly becuase of the Stark effect.

[^2]:    ${ }^{3} \mathrm{http}$ ://www.astro.umontreal.ca/ bergeron/CoolingModels/

[^3]:    a) Maxted et al. (2007) b) Kawka et al. (2008) c) Fuhrmeister \& Schmitt (2003) d) Shimanskii et al. (2008) e) Sing et al. (2005) f) Vennes et al. (1999) g) Morales-Rueda et al. (2005) h) Schreiber et al. (2008)
    i) Rebassa-Mansergas et al. (2008) j) Shimanskii \& Borisov (2002) k) Saffer et al. (1993) l) Stauffer (1987)
    m) O’Brien et al. (2001) n) Maxted et al. (2004) o) Tappert et al. (2009) p) van den Besselaar et al. (2007)
    q) Fulbright et al. (1993) r) Nebot Gómez-Morán et al. (2009) s) Pyrzas et al. (2009) t) Nagel et al. (2006)
    u) Hillwig et al. (2002) v) Aungwerojwit et al. (2007) w) Shimansky et al. (2003) x) Kawka et al. (2002)
    y) Kawaler et al. (1995) z) O’Donoghue et al. (2003) a2) Drake et al. (2009) b2) Tappert et al. (2007)
    c2) Haefner et al. (2004) d2) Gänsicke et al. (2004) e2) Maxted et al. (2009) f2) Maxted et al. (1998) g2) Maxted et al. (2006)

[^4]:    ${ }^{1}$ DR 1 is the first data release of the SDSS, the most recent one is the seventh. The DR 7 includes $11663 \mathrm{deg}^{2}$ of imaging data with five-band photometry for 357 million distinct objects, and spectroscopy over $9380 \mathrm{deg}^{2}$ with around 1.6 million spectra of galaxies $(930000)$, quasars (120000) and stars (460000).

[^5]:    ${ }^{2}$ http://www.sdss.org/dr7/tutorials/flags/index.html\#clean
    ${ }^{3}$ Plate pairs orientend towards the GP: 2555/2565, 2556/2566, 2678/2696, 2680/2698, 2812/2833, 2887/2912

[^6]:    ${ }^{4}$ http://www.sdss.org/dr7/start/aboutdr7.html

[^7]:    ${ }^{5}$ http://www.galex.caltech.edu/

[^8]:    ${ }^{6}$ http://das.sdss.org/wdcat/dr4/table11_dr4.wd.dat

[^9]:    ${ }^{7}$ The KS-test compares two distributions without assuming an underlying distribution of the data and tries to

[^10]:    determine if the datasets differ significantly and if they come from the same distribution. The parameter D gives the maximum distance between the two comulative functions, $0<D<1$, so that when the two datasets come from the same distributions the value of D trends to zero. The probability gives the significance level of the KS-test at which the compared distributions are different.

[^11]:    ${ }^{8}$ http://www.astro.princeton.edu/ schlegel/dust/

[^12]:    ${ }^{1}$ The tachocline is the dividing zone between the radiative core and the convective envelope, where the $\alpha \omega$ dynamo is thought to have its anchor and differential rotation arises.

[^13]:    ${ }^{2}$ We make the reader note that the plot does not contain information on time in the x -axis, but that it is just a sequence.

[^14]:    ${ }^{1}$ IRAF is distributed by the National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy, Inc., under contract with the National Science Foundation, http://iraf.noao.edu

[^15]:    ${ }^{1}$ IRAF is distributed by the National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy, Inc., under contract with the National Science Foundation, http://iraf.noao.edu
    ${ }^{2}$ http://www.sdss.org/dr7/algorithms/sdssUBVRITransform.html

[^16]:    ${ }^{3} \mathrm{http}: / / \mathrm{ftp} . j$ jach.hawaii.edu/ukirt/skl/dM.spectra/

